

THE COSMOLOGICAL CONSTANT

$$\underbrace{R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + g_{\mu\nu} \Lambda}_{\text{STRUCTURE OF SPACE-TIME}} = \underbrace{\frac{8\pi G}{c^4} T_{\mu\nu}}_{\text{MATTER + ENERGY ATTRACTIVE}}$$

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{8\pi G}{c^4} T_{\mu\nu} - \underbrace{g_{\mu\nu} \Lambda}_{\text{REPULSIVE}}$$

WITHOUT Λ THE UNIVERSE CONTRACTS

EINSTEIN PUT Λ IN, TO MAKE IT STATIC

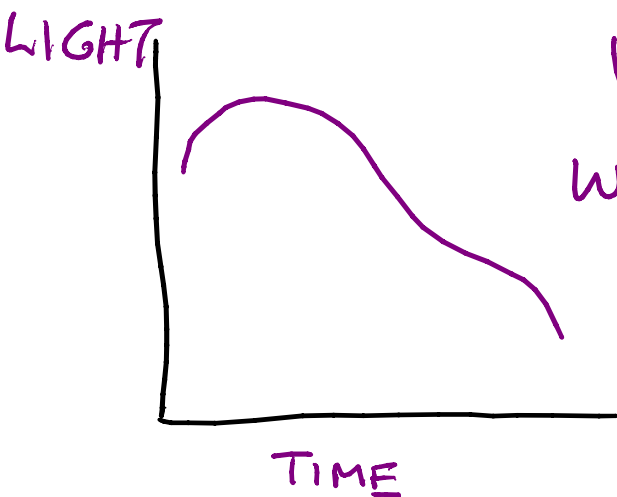
$$\Lambda = 8\pi \left(\frac{G}{c^4} \right) \rho_{\text{VAC}} = K \rho_{\text{VAC}}$$

ENERGY DENSITY OF VACUUM

UNTIL 1998 MOST COSMOLOGISTS WOULD
HAVE SAID $\Lambda = 0$

PERLMUTTER et al STUDIED TYPE IA
SUPERNOVAE \rightarrow WHITE DWARF PULLS
IN MATERIAL FROM COMPANION
LIGHT GENERATED $\sim 10^{11}$ STARS

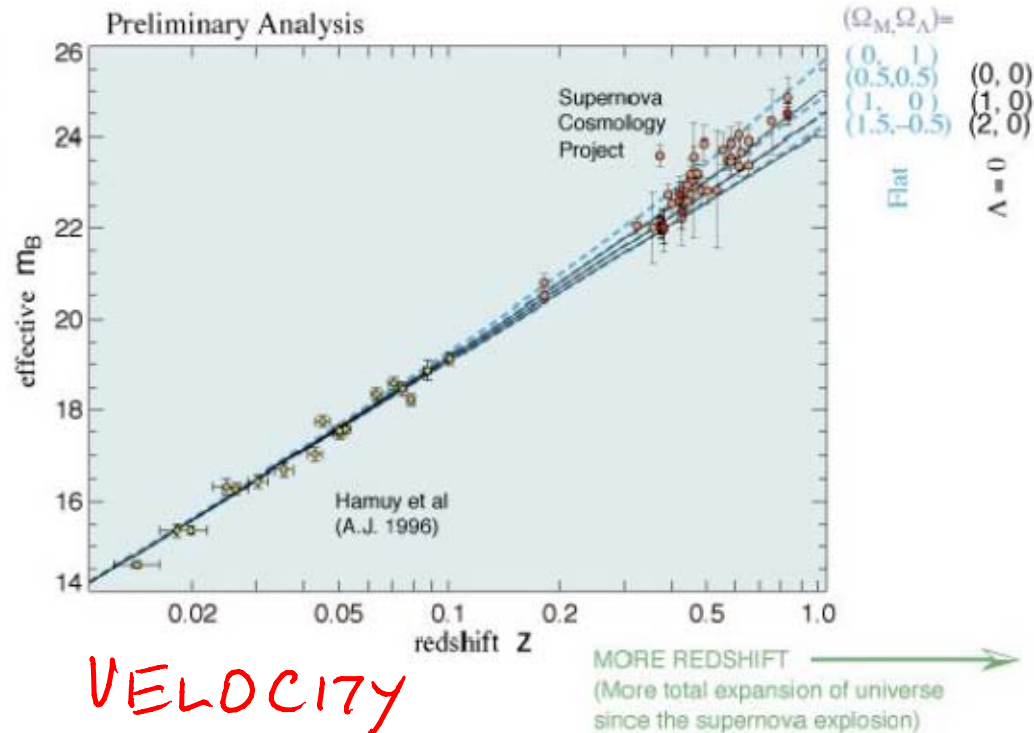
THEY OCCUR EVERY FEW HUNDRED YEARS
IN A TYPICAL GALAXY



VARIATION OF LIGHT OUTPUT
WITH TIME \rightarrow ABSOLUTE BRIGHTNESS
STANDARD CANDEL
DISTANCE SCALE

DISTANCE

↑
FAINTER
(Farther)
(Further back in time)

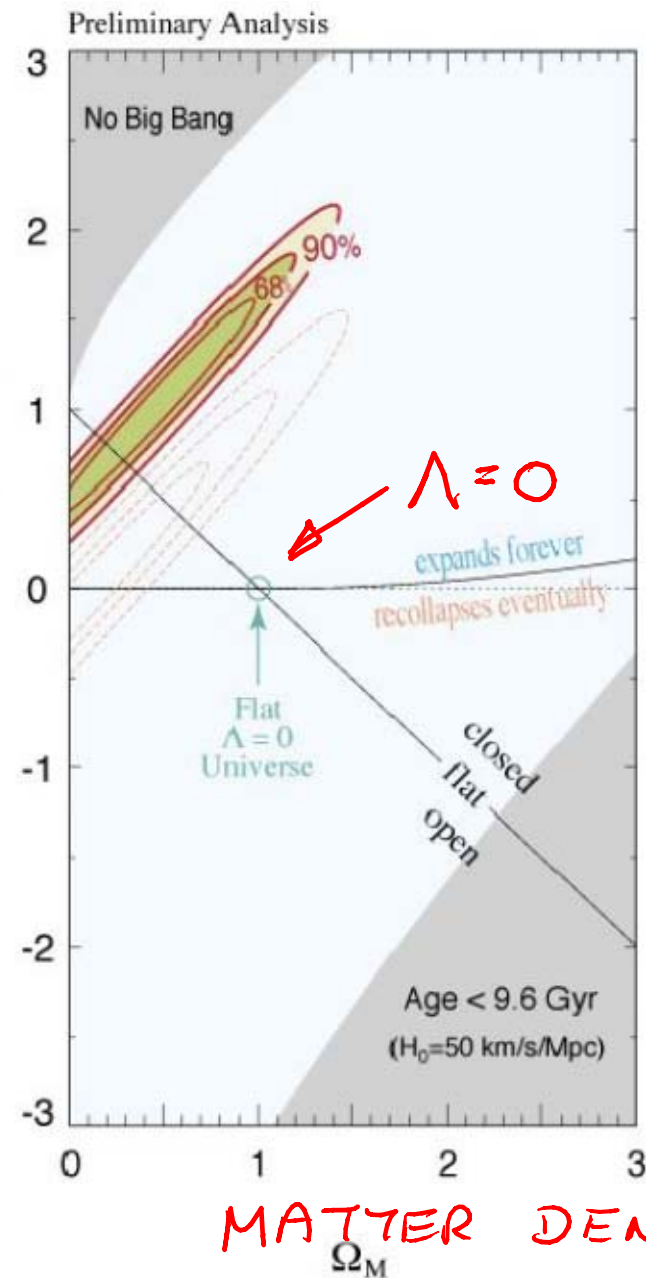


VELOCITY

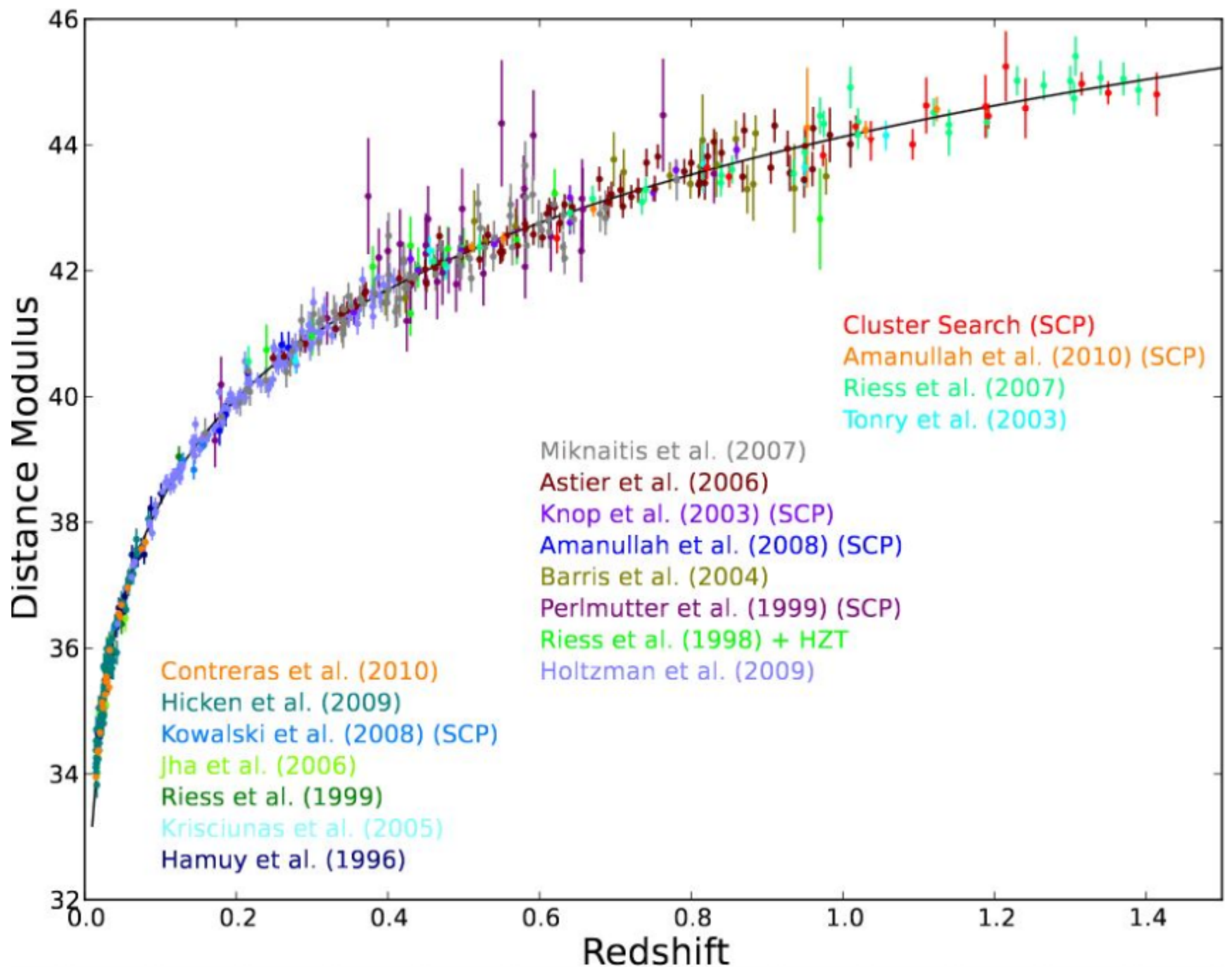
$$\Omega = \frac{\rho}{\rho_c}$$

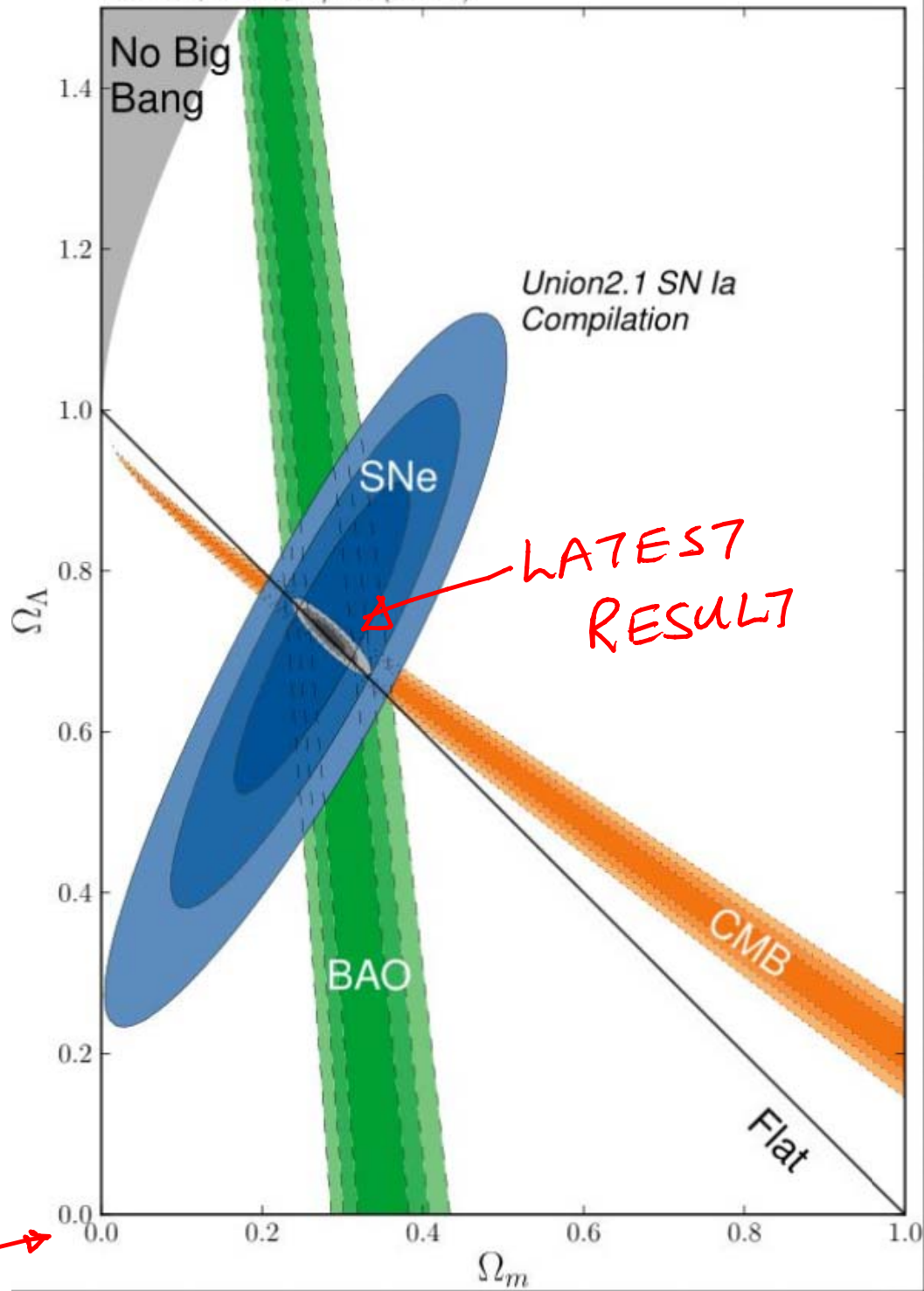
DARK ENERGY DENSITY

$$\Omega_\Lambda = \Lambda / (3H_0^2)$$



MATTER DENSITY





$\Lambda = 0 \rightarrow$

THE BRIGHTNESS (MAGNITUDE) MEASURES
HOW FAR AWAY THE SUPERNOVA IS
BUT THE LIGHT SET OUT AEONS AGO.

IS THIS DISTANCE

- 1) BETWEEN OUR POSITION AEONS AGO, AND GALAXY'S POSITION AEONS AGO?
- 2) BETWEEN OUR CURRENT POSITION, AND GALAXY'S POSITION AEONS AGO?
- 3) BETWEEN OUR CURRENT POSITION AND CURRENT POSITION OF GALAXY

THINK OF A MAP WITH A DISTANCE SCALE

1cm = 100 MILES

IF THE EARTH'S SURFACE SWELLS UNIFORMLY

→ IT IS JUST A SCALE CHANGE 1cm = 200 MILES

GALAXIES DO NOT MOVE UNDER THEIR OWN POWER!

THEY ARE JUST CARRIED APART BY THE EXPANSION OF SPACE → SCALE CHANGE

WE MEASURE DISTANCE BETWEEN CURRENT LOCATIONS

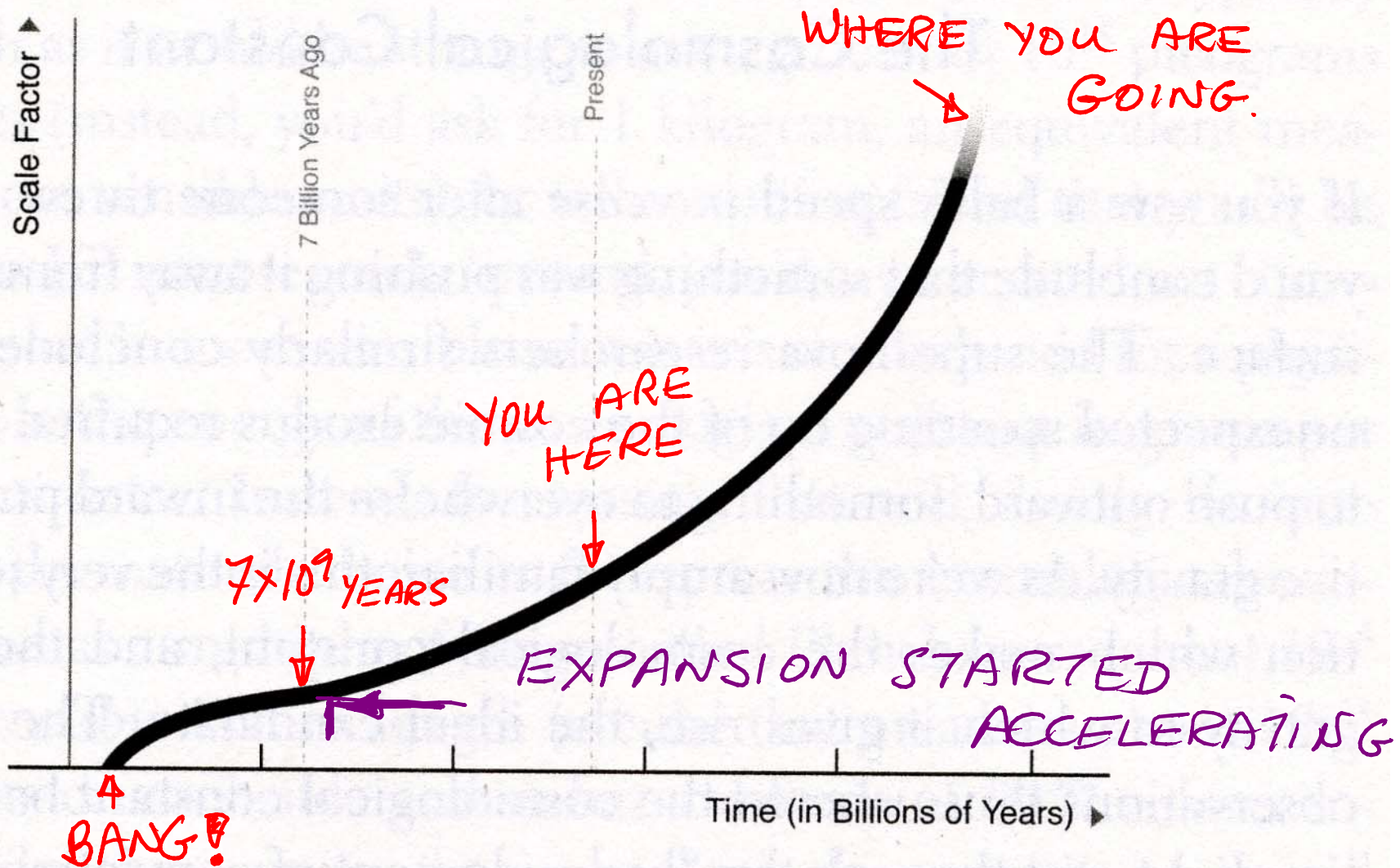


Figure 6.2 The scale factor of the universe over time, showing that cosmic expansion slowed down until about 7 billion years ago, when it began to speed up.

THE UNIVERSE'S EXPANSION STARTED ACCELERATING
WHEN THE PRESSURE OF Λ OVERCAME THE
RETARDATION FROM THE RETARDING FORCE
CAUSED BY GRAVITATIONAL ATTRACTION
OF MATTER IN THE UNIVERSE

PERLMUTTER Λ cd DETERMINED THAT THE
ENERGY DENSITY (DARK ENERGY) CAUSING
THE ACCELERATION IS 10^{-29} grams/cc

$$\text{PLANK MASS} = 10^{-5} \text{ g}$$

$$\text{PLANK LENGTH} = 10^{-33} \text{ cm}$$

$$\left. \begin{array}{l} 1 \text{ PLANK MASS} / 1 \text{ PLANK VOLUME} \\ = 1 \end{array} \right\}$$

IN THESE UNITS

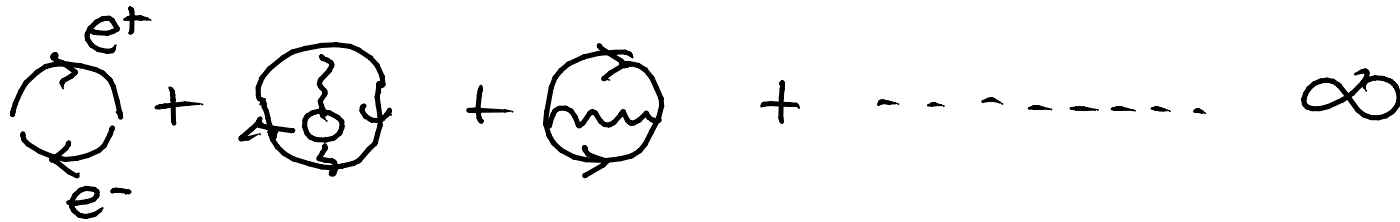
$$\Lambda = 10^{-123}$$

IS THAT ZERO?

NO!

10^{-123} IS A SMALL NUMBER, WE EXPECT
EITHER EXACTLY ZERO, OR ENORMOUS

QUANTUM FIELD THEORY SAYS VACUUM
HAS ENERGY DUE TO FLUCTUATIONS



QUANTUM FIELD THEORY SAYS WE HAVE
 ∞ ENERGY IN ANY VOLUME

IF CUT THIS CALCULATION OFF AT PLANK
LENGTH

→ I.E. QUANTUM GRAVITY COMES
INTO PLAY

→ STILL HAVE 10^{94} gms/cc

QUANTUM FIELD THEORY $\rightarrow 10^{94}$ gms/cc

\rightarrow ALL STARS IN ALL GALAXIES IN 1 CC

\rightarrow THIS IS $1 M_p / L_p^3 = 1$ CF 10^{-123} EXP

QFT IS OUT BY A FACTOR OF 10^{123}

IN PHYSICS A VALUE OF \equiv ZERO CAN ONLY BE DUE TO SOME SYMMETRY

FOR EXAMPLE GAUGE SYMMETRY REQUIRES PHOTON MASS EXACTLY ZERO \rightarrow WHICH IT IS.

SO PHYSICISTS EXPECTED $\Lambda = 0$ DUE TO SOME SYMMETRY.

BUT IT IS NOT ZERO, 10^{-123} \rightarrow WHY??

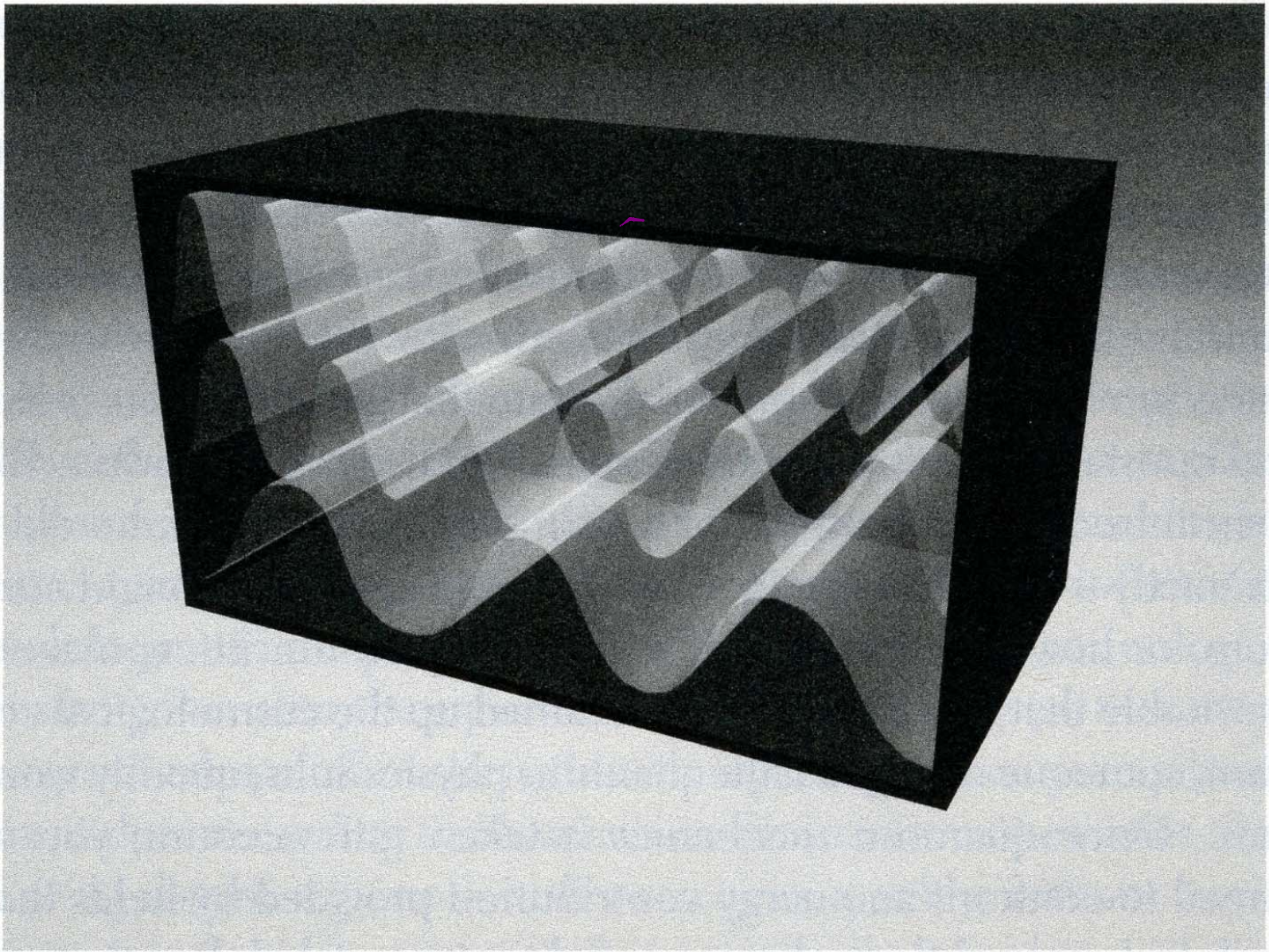


Figure 6.3 *There are infinitely many wave shapes in any volume and hence infinitely many distinct quantum jitters. This yields the problematic result of an infinite energy contribution.*

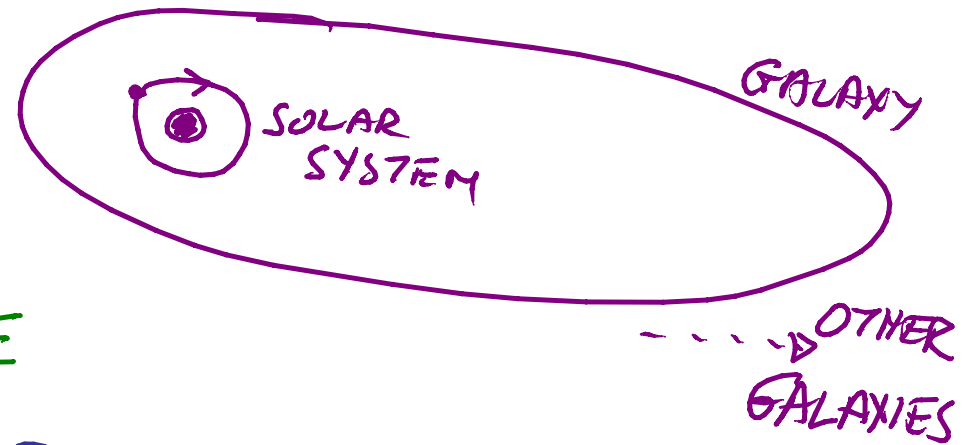
ANTHROPIC PRINCIPLE

SINCE THE TIME OF COPERNICUS WE HAVE
REPEATEDLY LEARNED THAT WE ARE
NO WHERE SPECIAL

BUT WE DO PLAY SOME
KIND OF SPECIAL ROLE

WE ARE OBSERVERS. AND WE CAN ONLY
EXIST UNDER SPECIAL CONDITIONS

GREEN → IF YOU ONLY LOOK FOR FISH IN
THE SAHARAH, YOU MIGHT TRY TO
UNDERSTAND WHY FISH HAVE BECOME EXTINCT.



IF WE DON'T THINK ABOUT OBSERVER BIAS
WE CAN BECOME HOPELESSLY CONFUSED

EG. → WHY IS THE EARTH 93×10^6 MILES FROM
THE SUN? NO REASON!

NEWTON'S LAWS ALLOWS PLANETS TO BE
ANY DISTANCE FROM THE SUN.

WE JUST HAPPEN TO LIVE HERE

IF THERE WERE NO OTHER PLANETS
WE MIGHT PUZZLE OVER 93×10^6

BUT THERE ARE OTHER PLANETS

→ NO PUZZLE

MAYBE THIS PRINCIPLE ALSO WORKS FOR THE
UNIVERSE

MAYBE THERE IS NO FUNDAMENTAL REASON

FOR $m_e = 0.00056 m_p$ ---- $\Lambda = 1.38 \times 10^{-123}$

EXCEPT THAT THEY HOLD IN A UNIVERSE

WHERE WE CAN EVOLVE. NO FUNDAMENTAL
LAW DETERMINES VALUES OF FUNDAMENTAL
CONSTANTS.

THIS REASONING IS DEVOID OF LOGIC IF
ONLY ONE UNIVERSE

CAN STILL DISCUSS

— DEEPER EXPLANATION

— LUCKY COINCIDENCE.

THIS ANTHROPIC ARGUMENT IS MUCH MORE
POTENT IF THERE ARE MANY UNIVERSES
OF ... MANY PLANETS AT ARBITRARY DISTANCES

DEPENDS ON!

- 1) OUR UNIVERSE IS PART OF A MULTIVERSE
→ VERY LARGE ENSEMBLE
- 2) AMONG THESE MANY UNIVERSES, THE
FUNDAMENTAL CONSTANTS CAN HAVE
WIDELY VARYING VALUES.
- 3) FOR MOST OF THE VARIATIONS IN THE
VALUES OF FUNDAMENTAL CONSTANTS
LIFE AS WE KNOW IT, COULD NOT EVOLVE.

STEVEN WEINBERG'S CALCULATION OF Λ (1987)

SEEMS FRUITLESS TO ATTEMPT TO CALCULATE

HOW Λ DETERMINES OUR EXISTENCE

→ TOO COMPLEX

HOWEVER STRUCTURE FORMATION (GALAXIES.....)

DETERMINE OUR EXISTENCE

STRUCTURE FORMATION DEPENDS ON GRAVITATIONAL

ATTRACTION Λ ACTS AGAINST THIS.

WEINBERG — $\Lambda >$ A FEW 100 TIMES CURRENT

VALUE WOULD STOP STRUCTURE

FORMATION

$$\Lambda_{\text{WEINBERG}} \sim 10^{-124}$$

ANTHROPIC ARGUMENT \rightarrow NEEDS A LARGE NUMBER OF UNIVERSES, SO THAT ONE HAS TO CONTAIN OUR VALUE OF Λ .

HOW LARGE?

ASSUME THAT IN PLANK MASS UNITS $0 < \Lambda < 1$
THE TICKS ON THE SCALE OF Λ MUST BE
AT LEAST AS SMALL AS WHAT WE OBSERVE
IE $10^{-121} \rightarrow 10^{121}$ UNIVERSES FOR $0 < \Lambda < 1$

NUMBER OF CELLS IN YOUR BODY 10^{13}

NUMBER OF SECONDS SINCE BIG BANG 10^{18}

NUMBER OF PHOTONS IN UNIVERSE 10^{88}

10^{121} IS A BIG NUMBER

GO BACK TO STRING THEORY

→ MANY POSSIBLE CALABI-YAU MANIFOLDS

→ THE "HOLES" IN THEM FILL WITH ENERGY

↳ I.E. THE EXTRA DIMENSIONS ARE FULL OF ENERGY

→ THIS ENERGY IS THE VALUE OF Λ

→ WE HAVE 10^{500} UNIVERSES EACH

WITH DIFFERENT VALUE OF Λ

→ WHEN INFLATION "STOPS" ENERGY

DENSITY IN UNIVERSE $\equiv \Lambda$

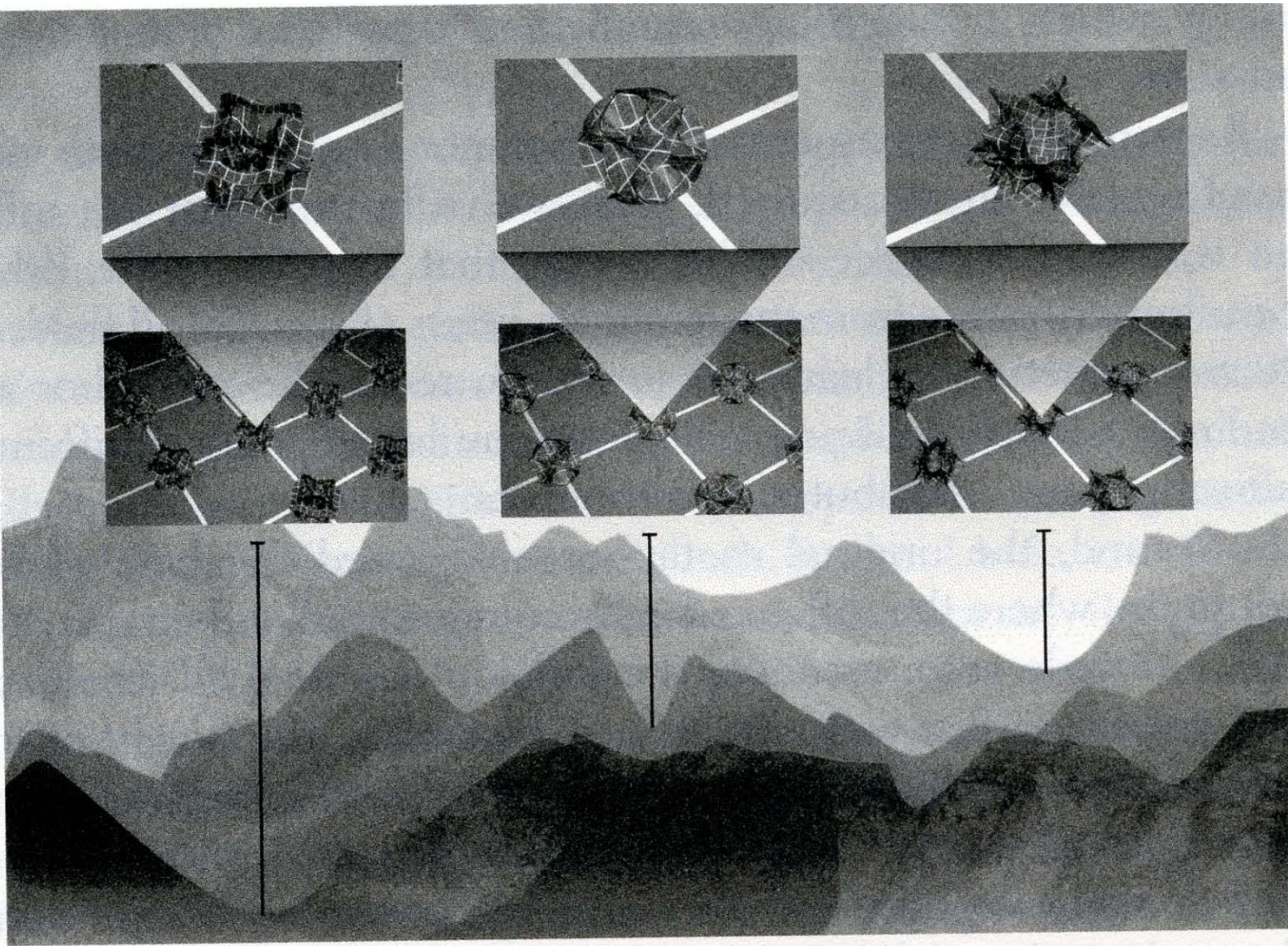
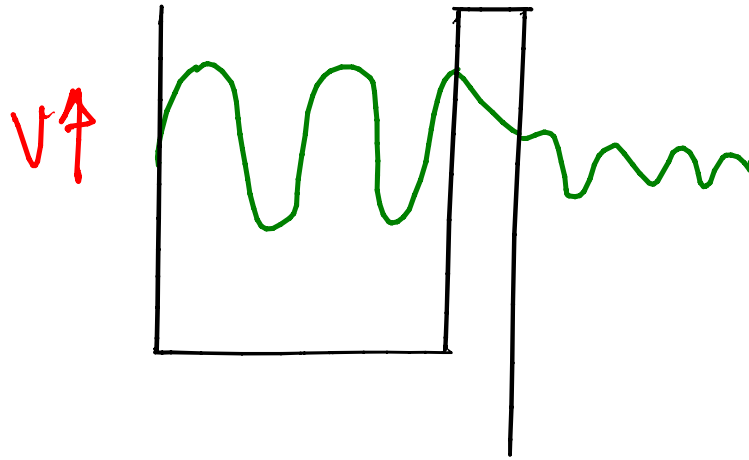


Figure 6.4 The string landscape can be visualized schematically as a mountainous terrain in which different valleys represent different forms for the extra dimensions, and altitude represents the cosmological constant's value.

EVERY POSSIBLE VALUE OF Λ ?

ELEMENTARY
QUANTUM
MECHANICS



PARTICLES CAN
"TUNNEL" THROUGH
POTENTIAL
BARRIER

SAME THING CAN HAPPEN FOR UNIVERSES

V ABOVE IS ANALOG OF Λ

UNIVERSE WITH GIVEN Λ CAN QUANTUM
MECHANICALLY TUNNEL TO LOWER Λ

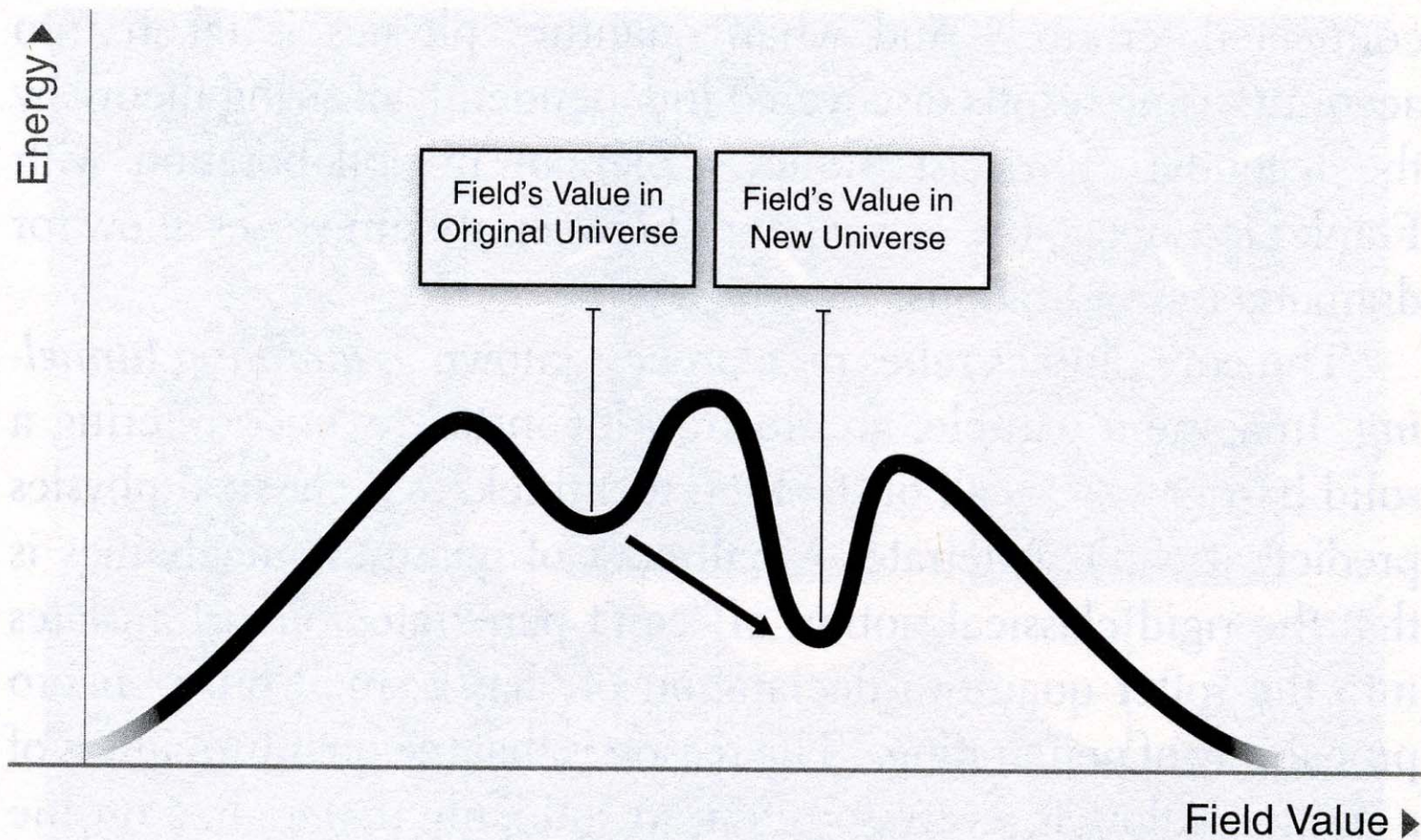


Figure 6.5 *An example of a field's energy curve that has two values—two troughs or valleys—where the field naturally comes to rest. A universe suffused with the higher-energy field value can quantum tunnel to the lower value. The process involves a small randomly located region of space in the original universe acquiring the lower field value; the region then expands, converting an ever-wider domain from the higher to the lower energy.*

← DIFFERENT KINDS
OF EXTRA
DIMENSIONS

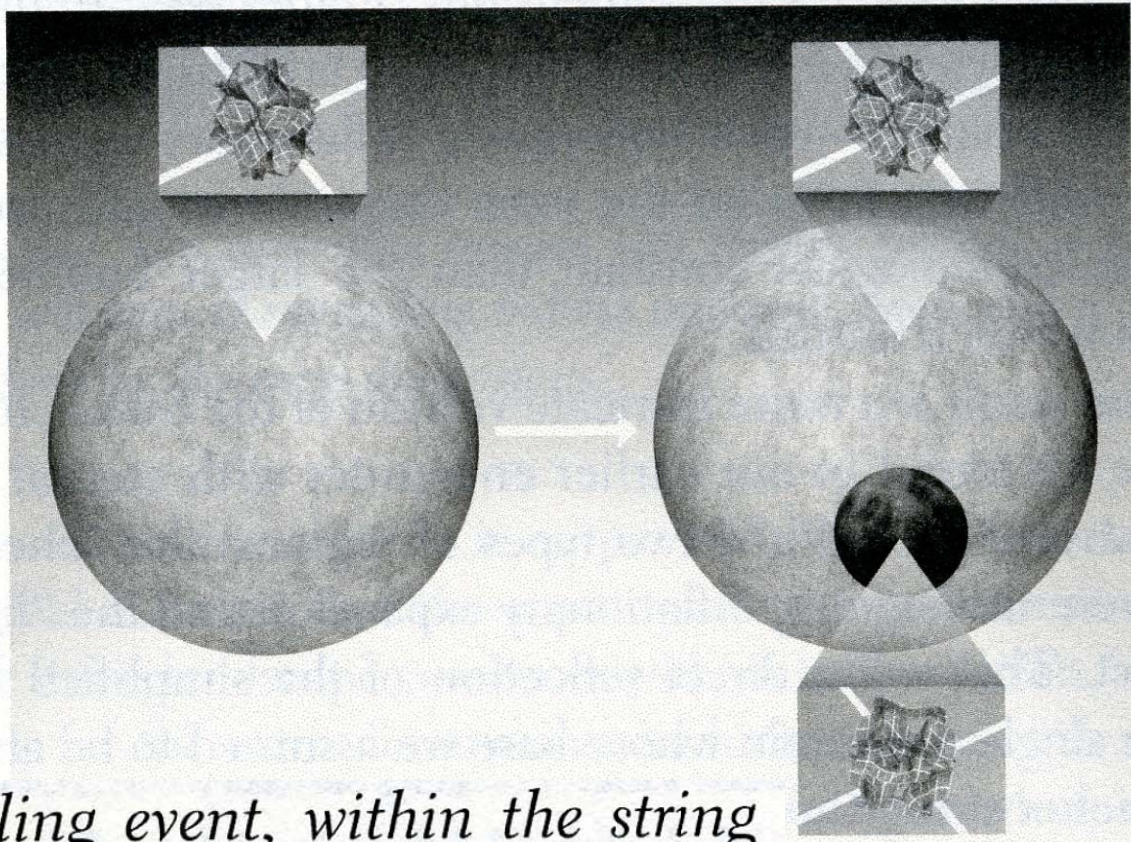
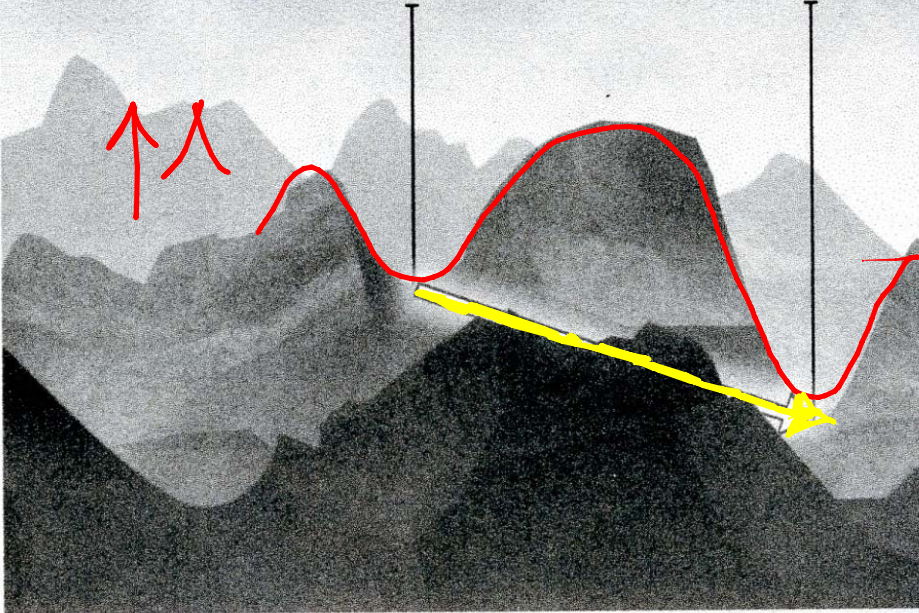
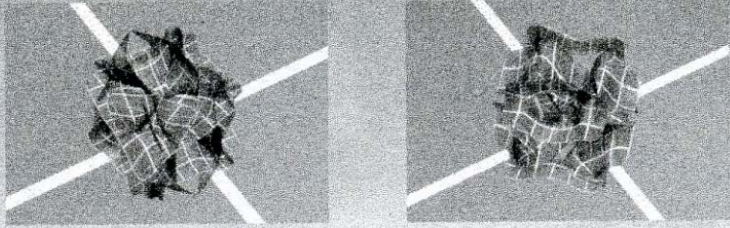


Figure 6.6 (a) A quantum tunneling event, within the string landscape. (b) The tunneling creates a small region of space—represented by the smaller and darker bubble—within which the form of the extra dimensions has changed.

TUNNELING DOES NOT OCCUR SIMULTANEOUSLY AT
ALL POINTS IN THE UNIVERSE

HAPPENS IN RANDOMLY DISTRIBUTED BUBBLES
WHICH THEN START TO EXPAND

IN NEW BUBBLE Λ IS SMALLER \rightarrow SLOWER
EXPANSION

BUBBLES INSIDE BUBBLES INSIDE BUBBLES ---
EVENTUALLY GET EVERY POSSIBLE KIND
OF EXTRA DIMENSIONS

IN OUR BUBBLE Λ SHOULD BE SMALL

ENOUGH FOR STRUCTURE FORMATION

\rightarrow BUT NOT MUCH SMALLER \rightarrow WHICH IT
IS.

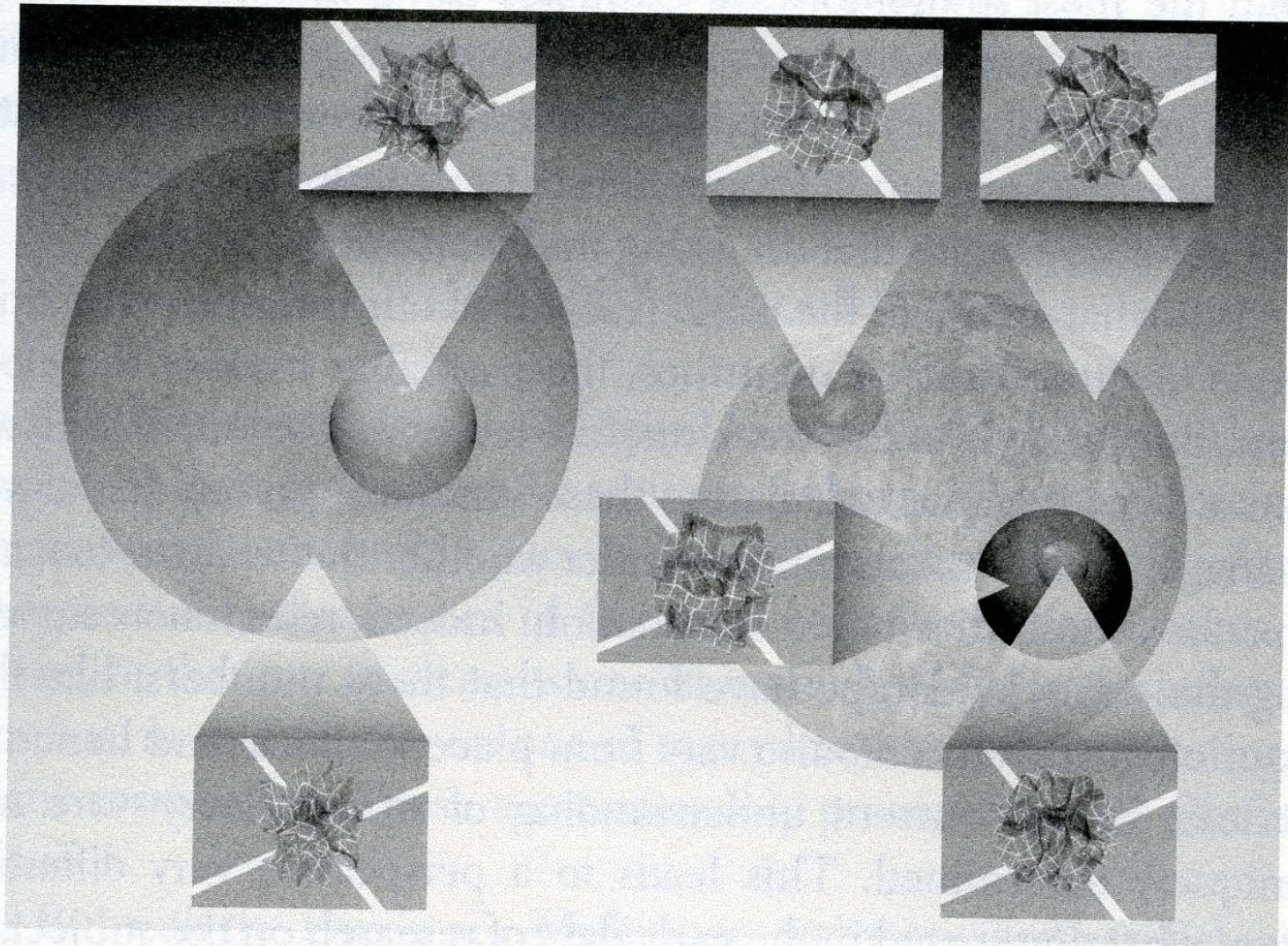


Figure 6.7 *The tunneling process can repeat, yielding a vast nested sequence of expanding bubble universes, each with a different form for the extra dimensions.*

IN EACH OF THIS INFINITY OF BUBBLES
ALL THE THINGS WE THOUGHT FUNDAMENTAL
ARE DIFFERENT

- # OF QUARK LEPTON GENERATIONS
- MASS OF ELECTRON
- α_{EM}
- α_{STRONG}
- G_N
- ⋮

CAN WE EVER KNOW IF OUR UNIVERSE IS
ACTUALLY FOUND IN STRING LANDSCAPE?

GREENE SAYS PEOPLE SEARCH " WITH BEST
COMBINATION OF RIGOROUS SCIENCE AND
ARTISTIC SENSIBILITY "

OR MAYBE YOU COULD SAY THAT ALL
THIS COMPLICATED MATHEMATICS HAS
LED NO WHERE AT ALL.

Is This Science?

In this chapter we've turned a logical corner. Until now, we've been exploring the implications for reality, writ large, of various developments in fundamental physics and cosmology research. I delight in the possibility that copies of the earth exist in the far reaches of space, or that our universe is one of many bubbles in an inflating cosmos, or that we live on one of many braneworlds constituting a giant cosmic loaf. These are undeniably provocative and alluring ideas.

But with the Landscape Multiverse, we've invoked parallel universes in a different way. In the approach we've just followed, the Landscape Multiverse is not merely broadening our view of what might be out there. Instead, an array of parallel universes, worlds that may be beyond our ability to visit or see or test or influence, now and perhaps always, are directly invoked to provide insight into observations we make here, in this universe.

Which raises an essential question: Is this science?