Subatomic Physics Detectors



Measuring energy

Calorimeters measure energy by absorbing particles. Most calorimeters measure the ionization energy deposited by all the charged particles in the "showers" produced as the particle is absorbed. The scale length of electromagnetic showers is the radiation length, X_0 (~2cm in Fe), relevant for both bremsstrahlung pair production; the scale length for hadronic showers is the mean hadronic interaction length, λ_I (0.2m in Fe).



Ionization observed is proportional to energy lost

 $N_{ions} \propto E$

This is statistical process

 $\sigma_{\rm N} = {\rm N}^{-1/2} \implies \sigma_{\rm E}/{\rm E} \propto {\rm E}^{-1/2}$ The resolution degrades rapidly if all the particles are not absorbed. i.e. The fluctuations in how much energy leaks out can be much bigger than the statistical uncertainty on measuring the energy that does not leak out.

Natural Radioactivity observed by a Germanium detector					
The common long-lived natural radioactive isotopes are Potassium-40, Uranium- 235, Uranium-238, and Thorium-232 (see http://hyperphysics.phy-astr.gsu.edu/hbase/nuclear/radser.html)					
Natural potassium (Z=19 protons) has 3 isotopes (N=20, 21, or 22 neutrons): (from http://ie.lbl.gov/education/parent/K_iso.htm)					
ZKA=N+Z	Natural Abundance	Half-life			
19K ³⁹	93.3%	stable			
${}_{19}K^{40}$	0.012%	1.25 x 10 ⁹ y			
${}_{19}K^{41}$	6.7%	stable			
Potassium-40 decays (from Table of Nucleides http://www2.bnl.gov/CoN/)					
Decay		%	$\Delta E (MeV)$		
β-	$_{19}$ K ⁴⁰ \Rightarrow $_{20}$ Ca ⁴⁰ +e ⁻ + $_{e}$	89.3	1312		
β+	$_{19}$ K ⁴⁰ \Rightarrow $_{18}$ Ar ⁴⁰ + e ⁺ +v _e	0.001	1505		
electron capture	$_{19}$ K ⁴⁰ + e ⁻ _{atomic} \Rightarrow $_{18}$ Ar ^{40*} + ν_{e}	10.7	1505		
	$(_{18}\mathrm{Ar}^{40*} \Longrightarrow _{18}\mathrm{Ar}^{40} + \gamma)$		(1461)		
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Unstable Isotopes

If particles can decay to a lower energy state, they will. Looking at some mass 40 isobars, predict which isotopes will undergo beta decays and by what process:

Isotope	Atomic Mass Excess	
$_{\rm Z} {\rm X}^{\rm A}$	$(M_X - A \cdot u)$	
17Cl ⁴⁰	– 27.558 MeV	
$_{18}{ m Ar}^{40}$	– 35.040 MeV	
${}_{19}K^{40}$	– 33.535 MeV	
${}_{20}Ca^{40}$	– 34.846 MeV	
$_{20}$ Sc ⁴⁰	– 20.526 MeV	

atomic mass unit (u) = (mass ${}^{12}C$ atom)/12 = 931.49432(28)MeV

Beta decay



Radiation Dose

A typical 70kg human body has 140g of potassium, and 17mg of K40, corresponding to a decay rate of 4.4kBq, and an annual dose of about 0.2mSv (out of a typical total of about 3.6mSv).

	SI Unit	Old Units
Activity:	Bequerel (Bq) = 1 decay/s	Curie (Ci)= 3.7x10 ¹⁰ Bq
Absorbed Dose	Gray (Gy) = 1 Joule/Kg	Rad = 0.01 Gy
Equivalent Dose	Sievert (Sv) = Gray x Q (Q = radiation weighting factor)	Rem = 0.01 Sv

The dose (D in μ Sv/hr) from nuclear gamma rays is approximately given by

$$D = 2A\frac{E}{R^2}$$

Where

A = the activity of the source (in MBq)

E = the total gamma energy emitted per disintegration (in MeV)

R = the distance from the source in metres

Typical doses from natural radiation are a few mSv/year (http://www.umich.edu/~radinfo/), but a few places have a natural background over 100 mSv/year (http://www.taishitsu.or.jp/radiation/index-e.html)

Photon Interactions



Pair production



In the high energy limit (E_{γ} >>2 m_e), the mean distance a photon will travel before pair producing is

$$X_{p} \sim 9/7 X_{0}$$

(Note: The reason the radiation length and the pair production length are almost the same is because bremsstrahlung and pair production are simply time and space rearrangements of the same process: a real photon coupling to an electron which is coupled via a virtual photon to a nucleus.)