

Conservation Laws

"Everything which is not forbidden is compulsory"

Lewis Carroll?
Richard Feynman?
Murray Gell-Mann?
Swiss Proverb?
T. H. White?

...

Why? or Why not?

Particle (mass) J^{PC} \Rightarrow decay	Mean Lifetime (τ)	Decay Width	Decay Fraction	Comments / Conservation Laws
ρ^0 (769) 1^{--}	$4 \times 10^{-24} \text{s}$	151 MeV		
$\Rightarrow \pi^+\pi^-$		150 MeV	99%	
$\Rightarrow \pi^+\pi^-\gamma$		1.5 MeV	1%	$\sim \alpha$
$\Rightarrow e^+e^-$		7 KeV	4.5×10^{-5}	$\sim \alpha^2$ EM (electromagnetic)
$\Rightarrow \gamma$				momentum
$\Rightarrow \pi^0\pi^0$				Bose-Einstein (BE) statistics
$\Rightarrow \gamma\gamma$				Landau-Yang theorem (BE, J)
π^0 (135) 0^{-+}	$8 \times 10^{-17} \text{s}$	8 eV		lightest hadron
$\Rightarrow \gamma\gamma$		8 eV	98.8%	$\sim \alpha^2$ EM
$\Rightarrow e^+e^-\gamma$		$9 \times 10^{-2} \text{eV}$	1.2%	$\sim \alpha^3$ EM
$\Rightarrow e^+e^-e^+e^-$		$2 \times 10^{-4} \text{eV}$	3×10^{-5}	$\sim \alpha^4$ EM
$\Rightarrow e^+e^-$		$6 \times 10^{-7} \text{eV}$	8×10^{-8}	$\sim \alpha^4$ EM (See notes)
$\Rightarrow \gamma\gamma\gamma$			$< 3 \times 10^{-8}$	$\sim \alpha^3$, Charge Conjugation (C)

Notes

All data from the **Review of Particle Properties** (<http://pdg.lbl.gov/>)

Decay Width: Because of the Heisenberg uncertainty principle, any particle with a finite lifetime has a mass distribution of non-zero width. The total decay width ($\Gamma = \hbar/2\pi\tau$) is the Full Width at Half Maximum of the mass distribution. Each decay channel contributes to the total width, and the partial decay width ($\Gamma_i = \Gamma \cdot \text{BR}$) is the contribution to the total width due to a specific final state.

Decay Fraction: Decay branching fraction or branching ratio (BR) is the probability of a particle decaying into a specific final state. The sum of the branching ratios should add up to 100%. (Sometimes "branching ratio" refers to a ratio of branching fractions, but in particle physics "branching ratio" is usually synonymous with "branching fraction".)

$\pi^0 \Rightarrow e^+e^-$: Mediated by 2 virtual photons, not 1, since the pion has spin-0. The decay is also suppressed by an helicity factor of $(m_e/m_\pi)^2$.

Helicity is the normalized projection of a particle's spin on to its momentum, i.e. $\mathbf{J} \cdot \mathbf{p} / J \cdot p$. Helicity is not a relativistically invariant quantity since momentum is frame dependent, but helicity is conserved to the extent that the probability of the helicity remaining the same is typically $\beta = v/c$. (Note: This is true independent of whether parity is conserved.)

Energy, Angular Momentum, Baryon and Lepton Number

$\Delta^0(1232)^{3/2^+}$	$5 \times 10^{-24} \text{s}$	120 MeV		
$\Rightarrow N\pi$ ($p\pi^-$ or $n\pi^0$)		120 MeV	>99%	strong
$N^0(1440)^{1/2^+}$	$2 \times 10^{-24} \text{s}$	350 MeV		
$\Rightarrow N\pi$		220 MeV	65%	strong
$\Rightarrow N\pi\pi$		120 MeV	35%	strong
$n(940)^{1/2^+}$	887s	$7 \times 10^{-25} \text{eV}$		
$\Rightarrow p\pi^-$				strong, energy
$\Rightarrow pe^-$				J (angular momentum) & L
$\Rightarrow \pi^+e^-$		$< 2 \times 10^{-55} \text{eV}$		Baryon number (B) & lepton number (L)
$\Rightarrow pe^- \bar{\nu}_e$		$7 \times 10^{-25} \text{eV}$	~100%	weak
$p(938)^{1/2^+}$	$> 10^{25} \text{y}$	$< 10^{-54} \text{eV}$		lightest baryon
$\Rightarrow \pi^0 e^+$	$> 10^{33} \text{y}$	$< 10^{-62} \text{eV}$		B & L (e.g. Super-Kamiokande)
$e^-(0.511)^{1/2}$	$> 10^{23} \text{y}$			
$\Rightarrow \nu_e \gamma$	$> 10^{25} \text{y}$			electric charge (Q)
$d(np)1^+$	$> 10^{26} \text{y?}$			(D_20 in proton decay experiments)
$\Rightarrow \pi^0 \pi^+$	$> 2 \times 10^{30} \text{y}$			B (from Fe decays)
$\pi^- \Rightarrow \mu^- \nu_e$			<0.15%	L

Super-Kamiokande

Pictures from the ICRR (Institute for Cosmic Ray Research), The University of Tokyo.
(<http://www-sk.icrr.u-tokyo.ac.jp/doc/sk/index1.html>)

See

<http://www-sk.icrr.u-tokyo.ac.jp/doc/sk/photo/high.html>

Super-Kamiokande accident:

<http://www-sk.icrr.u-tokyo.ac.jp/doc/sk/photo/pmt-damage/index.html>