Hadronic Calorimeters



- Strong (nuclear) interaction cascade
- Similar to EM shower

 $\chi_0(EM) \rightarrow \lambda_I(had) \approx 35 \, g \, cm^{-2} \, A^{1/3}$

hadronic interaction length

 $\rightarrow \lambda_I > \chi_0$

hadronic calorimeter nearly always sampling calorimeters

Shower length

 $\sim 5\lambda \sim 4m@100~GeV$

 $\sim 13\lambda \sim 10m@1TeV$

- **Energy Resolution** •
 - shower fluctuations
 - leakage of energy
 - invisible energy loss mechanisms

Sampling Calorimeter



Hadronic Lateral Shower Profile



- Hadronic shower much broader than EM
 - Mean hadronic *p*_T versus MCS

$$\lambda_{I} \sim 16cm$$

 $\chi_{0} \sim 1.8cm$

Hadronic Shower Longitudinal Development



Lateral Scaling with Material



$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{A_0}{\sqrt{E}}\right)^2 + \left(\frac{A_1}{\sqrt{E}}\right)^2 + \left(A_2\ln E\right)^2 + \left(\frac{A_3\sqrt{N}}{E}\right)^2 + A_4$$



number of samples $N = \frac{E}{\Delta E} \subset \frac{energy}{energy}$ energy deposited in a sampling step $\sigma_E = \sigma_N \cdot \Delta E = \sqrt{N} \cdot \Delta E$ $\frac{\sigma_E}{E} = \sqrt{N} \frac{\Delta E}{E}$ $\frac{\sigma_E}{E} = \frac{\sqrt{\Delta E}}{\sqrt{E}}$ stochastic term $A_0 \sim \sqrt{\Delta E}$

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{A_0}{\sqrt{E}}\right)^2 + \left(\frac{A_1}{\sqrt{E}}\right)^2 + \left(A_2\ln E\right)^2 + \left(\frac{A_3\sqrt{N}}{E}\right)^2 + A_4$$

 $\frac{A_{\rm l}}{\sqrt{E}}$ counting statics in sensor system ion pairs in liquid argon $N = \overline{n} \cdot E$ mean # of photo-electrons in PM per unit of incident energy $\sigma_E = \frac{\sigma_N}{\overline{n}} = \frac{\sqrt{N}}{\overline{n}} = \frac{\sqrt{\overline{n}} \cdot \overline{E}}{\overline{n}}$ $\frac{\sigma_E}{\overline{E}} = \frac{1}{\sqrt{\overline{n}}} \cdot \frac{1}{\sqrt{E}}$ $A_{\rm l} = \frac{1}{\sqrt{\overline{n}}}$ this term is usually negligible

 A_2 shower leakage fluctuations – make calorimeter as deep as \$\$ allow

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{A_0}{\sqrt{E}}\right)^2 + \left(\frac{A_1}{\sqrt{E}}\right)^2 + \left(A_2\ln E\right)^2 + \left(\frac{A_3\sqrt{N}}{E}\right)^2 + A_4$$

- A_3 noise detector or electronics important for low level signal
 - liquid argon electronics
 - detector capacitance



 $A_3 \simeq \Delta E \cdot N$ increases with number of channels summed over

$$\left(\frac{\sigma}{E}\right)^2 = \left(\frac{A_0}{\sqrt{E}}\right)^2 + \left(\frac{A_1}{\sqrt{E}}\right)^2 + \left(A_2\ln E\right)^2 + \left(\frac{A_3\sqrt{N}}{E}\right)^2 + A_4$$

 A_4 inter - calibration uncertainty of channels - constant in E

- fractional channel to channel gain uncertainty
- spatial in-homogeneity of detector energy response
- dead space
- temperature variation
- radiation damage
- all these influence spatial variation of effective energy response

$$\sigma = k \cdot E$$
$$\frac{\sigma_E}{E} = k \quad \text{constant}$$

The em energy resolution of the ATLAS calorimeter



FIG. 9.30. The em energy resolution and the separate contributions to it, for the em barrel calorimeter, at $\eta = 0.28$ [Gin 95].



Energy (GeV)

· EFFECT OF SAMPLING + SHOWER TRACK LENGTH FLUCTUATIONS IN ELECTROMAGNETIC SHOWER

> MONTE CARLO SIMULATION



Sampling fluctuations in em and hadronic showers



FIG. 4.15. The energy resolution and the contribution from sampling fluctuations to this resolution measured for electrons and hadrons, in a calorimeter consisting of 1.5 mm thick iron plates separated by 2 mm gaps filled with liquid argon. From [Fab 77].

Sampling fluctuations in em calorimeters Determined by sampling fraction and sampling frequency



FIG. 4.8. The em energy resolution of sampling calorimeters as a function of the parameter $(d/f_{\rm samp})^{1/2}$, in which d is the thickness of an active sampling layer (e.g. the diameter of a fiber or the thickness of a scintillator plate or a liquid-argon gap), and $f_{\rm samp}$ is the sampling fraction for mips [Liv 95].

How to measure the effects of sampling fluctuations (2)



FIG. 4.14. Pulse height distributions for 30 GeV hadrons obtained with the ZEUS lead/plastic-scintillator prototype calorimeter. Diagram a) shows the distributions of E_{sum} , E_{diff} and $2E_A$, measured in the configuration depicted in Figure 4.13b. Diagram b) shows the same distributions measured in the same configuration, but with the black tape removed. See text for details. From [Dre 90].



· ENERGY RESOLUTION DEGRADATION DUE TO LONGITUDINAL OR LATERAL ENERGY LEAKAGE

· LONGIFRDINAL L95% = gotelnE + 39 an

~ 6 XINT

· LATERAL

R959 ~ 1 XINT



Calorimeter non-uniformity

Table 5: Principal Contributions to Energy Resolution inElectromagnetic and Hadronic Calorimeters

Mechanisms (add in quadrature)	Electromagnetic showers	Hadronic showers
Intrinsic shower fluctuations	Track-length fluctuations: $\sigma/E \ge 0.005/\sqrt{E}$ (GeV).	Fluctuations in the energy loss: $\sigma/E \approx 0.45/\sqrt{E}$ (GeV). Scaling weaker than $1/\sqrt{E}$ for high energies. With compensation for nuclea effects: $\sigma/E \approx 0.22/\sqrt{E}$ (GeV).
Sampling fluctuations	$\sigma/E \approx 0.04 \sqrt{\Delta E/E}$. Nature of readout may augment sampling fluctuations.	$\sigma/E \simeq 0.09 \sqrt{\Delta E/E}$
Instrumental effects	 Noise and pedestal width: σ/E ~ 1/E determine minimum detectable signal; limit low-energy performance. Calibration errors and non-uniformities: σ/E ~ constant and therefore limits high-energy performance. 	
Incomplete containment of shower	$\sigma/E \sim E^{-\alpha}, \alpha < 1/2$ (see subsec. 2.2, resp. 3.4). For leakage fraction \geq few %: non-linear response and non-Gaussian 'tail'.	

Semi-empirical model of hadron shower development

$$\frac{dE}{dS} = E_{INC} \left\{ \frac{Cx^{(\alpha_E - 1)}e^{-x}}{\Gamma(\alpha_E)} \right\} + E_{INC} \left(1 - C\right) \left\{ \frac{y^{(\alpha_H - 1)}e^{-y}}{\Gamma(\alpha_H)} \right\}$$

electromagnetic part

hadronic part

$$x \equiv \beta_E \frac{\left(S - S_0\right)}{\chi_0}$$
 radiation length
$$y \equiv \beta_H \frac{\left(S - S_0\right)}{\chi}$$
 interaction length

$$\alpha_{H} = \alpha_{E} = 0.62 + 0.32 \ln E$$

 $\beta_{H} = 0.91 - 0.02 \ln E$
 $\beta_{E} = 0.22$
 $C = 0.46$

 $S_0 \neq 0$ - significant amount of material in front of calorimeter (magnet coil etc.)

More Rules of Thumb for the Hobbyist

Shower maximum

 $t_{\max}(\lambda) \sim 0.2 \ln E(GeV) + 0.7$

95% Longitudinal containment

$$L_{95\%} \left(\lambda \right) \sim t_{\max} + 2.5 \lambda_{ATT}$$

$$\lambda_{ATT} \approx \lambda \left[E(GeV) \right]^{0.13}$$

95% Lateral containment

$$R_{95\%} \sim 1\lambda$$

Mixtures in sampling calorimeters
 active + passive material



Typical Calorimeter Resolutions

• Homogeneous EM (crystal, glass)

$$\frac{0.5\%}{\sqrt{E}} \rightarrow \frac{3.0\%}{\sqrt{E}} \oplus 0.5\%$$

CLEO, Crystal Ball, Belle, CMS.....

• Sampling EM (Pb/Scint, Pb/LAr)

$$\frac{8\%}{\sqrt{E}} \rightarrow \frac{15\%}{\sqrt{E}} \oplus 1\%$$
CDF, ZEUS, ALEPH, ATLAS.....

• Non-compensating HAD (Fe/Scint, Fe/LAr)

$$\frac{70\%}{\sqrt{E}} \to \frac{110\%}{\sqrt{E}} \oplus 5\%$$

CDF,ATLAS,H1, LEP = everyone

Compensating HAD (DU/Scint)

 $\frac{35\%}{\sqrt{E}} \oplus 1\%$ ZEUS, HELIOS

Invisible Energy in Hadronic Showers

'ELEMENTARY PROCESS' IN A HADRON SHOWER



Fig. 3.6 'Elementary physical process' in a hadron shower.

Difference in Response to Electrons and Hadrons





Fig. 7.1 Illustration of the meaning of the e/h and e/mip values of a calorimeter. Shown are distributions of the signal per unit deposited energy for the electromagnetic and non-em components of hadron showers. These distributions are normalized to the response for minimum ionizing particles ("mip"). The average values of the em and non-em distributions are the em response ("e") and non-em response ("h"), respectively [1]

The em shower fraction, f_{em} (1)



 $< f_{em} >$ is large, energy dependent and material dependent

The em shower fraction, f_{em} (2)



Fluctuations in fem are large and non-Poissonian

The em shower fraction, f_{em} (4)



 f_{em} fluctuations are different in π - and p-induced showers

Calibration problems for hadronic shower detection

 π^{o} production may take place anywhere in the absorber



Hadronic shower response and the *e/h* ratio

• The hadronic response is **not constant**

 $f_{\rm em}$, and therefore e/π signal ratio is a function of energy

- \rightarrow If calorimeter is linear for electrons, it is non-linear for hadrons
- Energy-independent way to characterize hadron calorimeters: e/h

e = response to the em shower component

h = response to the non-em shower component

 \rightarrow Response to showers initiated by pions:

$$R_{\pi} = f_{\rm em} \ e \ + \ \left[1 - f_{\rm em}\right] h \ \ o \ \ e/\pi = rac{e/h}{1 - f_{\rm em}\left[1 - e/h
ight]}$$

e/h is inferred from e/π measured at several energies ($f_{\rm em}$ values)

• Calorimeters can be

Undercompensating (e/h > 1)Overcompensating (e/h < 1)Compensating (e/h < 1)

Hadron showers: e/h and the e/ π signal ratio



FIG. 3.4. The relation between the calorimeter response ratio to em and non-em energy deposition, e/h, and the measured e/π signal ratios. See text for details.

Effect of e/h on Energy Resolution



Effect of e/h on Linearity





Available energy (GeV)

LINEARITY IN

Cu / Scina /U

COMPENSATING

HELIOS = FIRST CALORIMETER



3.14 Pulse height distributions of 5 GeV electrons, hadrons and muons measured with a lead scintillator (5mm Pb, 5mm Scint) calorimeter (a), and a depleted-uranium scintillator (3.2mm DU, 5mm Scint) calorimeter (b) (ZEUS).



.NB ph -> ENERGY CALIBRATED By U line





Fig. 3.26 The e/h-ratio versus beam momentum measured with the ZEUS prototype calorimeter at CERN.



Fig. 3.27 The energy resolution versus beam momentum for electrons and hadrons measured with the ZEUS prototype calorimeter at CERN.


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The compensation puzzle solved!

The e/h value is not determined by the absorber, but by active medium



Compensation in practice: Pb/scintillator calorimeters



FIG. 3.35. The e/π signal ratio, corrected for the effects of shower leakage, for lead/polystyrene-scintillator calorimeters, as a function of the thickness of the lead plates, for 2 mm thick scintillator plates. The inner (outer) error bars show the combined systematic and statistical uncertainty without (with) the shower leakage corrections. The line in the plot is a result of a linear fit to the experimental data [Suz 99].

Compensation in Fe/scintillator calorimeters?



FIG. 3.36. The e/h value for iron/plastic-scintillator calorimeters, as a function of the sampling fraction for mips (top horizontal scale), or the volume ratio of the amounts of passive and active material (bottom horizontal scale).

Compensation: Effect of slow neutrons on the signals



FIG. 3.22. Time structure of various contributions from neutron-induced processes to the hadronic signals of the ZEUS uranium/plastic-scintillator calorimeter [Bru 88].



FIG. 3.23. The ratio of the average ZEUS calorimeter signals from 5 GeV/c electrons and pions (a) and the energy resolutions for detecting these particles (b), as a function of the charge integration time [Kru 92].

Weighting to Correct for e/h



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Jet-Jet Mass Resolutions



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HIGH PI SINGLE JET MASS RESOLUTION FOR W RECONSTRUCTION IN W' -> WZ





Fig.8 a: Principle of operation of an ionization chamber. 8 b:current pulse shape in the ionization chamber(solid line). Dashed line : after clipping.



ZEUS Forward Calorimeter







LAr Calorimetry

- Five different detector technologies
- Calorimetry coverage to



LAr Calorimeter Technology Overview

Design Goals
Technology

• EM Calorimeters ($0 \le |\eta| \le 3.2$) and Presampler ($0 \le |\eta| \le 1.8$)

 $\frac{\sigma}{E} \le \frac{10\%}{\sqrt{E(\text{GeV})}} \oplus 0.7\% \oplus \frac{0.27}{E(\text{GeV})} \qquad \sigma_{\theta} \le \frac{40 \text{ mrad}}{\sqrt{E(\text{GeV})}} \qquad \sigma_{\vec{r}} \le \frac{8 \text{ mm}}{\sqrt{E(\text{GeV})}}$

Lead/Copper-Kapton/Liquid Argon Accordion Structure

• Hadronic Endcap (1.5 $\leq |\eta| \leq 3.2$) $\frac{50\%}{\sqrt{E(\text{GeV})}} \oplus 3\% \leq \frac{\sigma}{E} (\text{jets}) \leq \frac{100\%}{\sqrt{E(\text{GeV})}} \oplus 10\%$

Copper/Copper-Kapton/Liquid Argon *Plate* Structure

• Forward Calorimeter $(3 \le |\eta| \le 5)$ $\frac{\sigma}{E}(jets) \le \frac{100\%}{\sqrt{E(GeV)}} \oplus 10\%$

Tungsten/Copper/Liquid Argon *Paraxial Rod* Structure

LAr and Tile Calorimeters





Barrel Module Schematic with presampler

- 64 gaps /module
- 2.1 mm gap
- 2x3100 mm long



Half Barrel Assembly

- 2x16 modules
- I.R/O.R 1470/2000 mm
- •22-33 X_0
- 3 longitudinal samples
- $\Delta\eta \times \Delta\varphi$ 0.025 × 0.025
- presampler $|\eta| < 1.8$

Electromagnetic Endcap

 $1.4 < \eta < 3.2$



- 96 gaps /module outer wheel 32 gaps/module inner wheel
- 2.8 0.9 mm gap outer 3.1-1.8 mm inner

- 2x8 modules
- Diam. 4000 mm
- •22-37 X₀
- 3 longitudinal samples
 - $\Delta \eta \times \Delta \varphi \quad 0.025 \times 0.025 \\ |\eta| > 2.5 \rightarrow 0.1 \times 0.1$
- Front sampling of 6 X_0 for $|\eta| < 2.5$, η strips.

Accordion Structure



Prototype of EM endcap

Detail of Kaptons





ATLAS FCAL









Pictures of assembly process



LAr Forward Calorimeters



• FCAL C assembly into tube – Fall 2003



ATLAS HEC Structure



LEWECTROSTATIC TRANSFORMER

- MATCHES CAL PREAMP CAPACITANCE • REDUCES EFFECTIVE CAPACITANCE + NOISE

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TRANSFER

TIME



• Does not work in magnetic field. Long readout cables slow down signal

• Large capacitance, large noise



Fig. 1. Schematic representation of capacitance matching for a hadronic tower. High voltage connections are not shown. I_g is the ionization current in the gth gap. V and C are the dc voltage and capacitance per gap, respectively. The arrows show the directions of current flow. In (a) all N gaps are connected in parallel; matching is achieved with a ferrite-core transformer with turns ratio n = 3. (b) shows an electrostatic transformer with P parallel subtowers of S = 3 gaps in series (N = SP).



Fig. 2. Schematic view of two subsections of the tower with an electrostatic transformer of ratio S = 3. The absorbing signal tile is at dc ground. High voltages, decoupled by large resistances, are supplied to the half tiles, which are separated by thin insulating layers.

584

Hadronic Endcap Calorimeter (HEC)



Composed of 2 wheels per end Front wheel: 67 t 25 mm Cu plates Back wheel: 90 t 50 mm Cu plates









Electromagnetic Endcap



Hadronic Endcap



HEC – FCAL Assembly



Shaping, Pileup and Electronic Noise

Inelastic pp cross section 70 mbAverage luminosity of 1034 cm-2s-12835 active bunches over 3564 LHC clock cycles

23 inelastic events per crossing




Noise Level in LAr Calorimeters



Since the FCal is in the very forward region, these noise levels are OK

Test Beam Energy Resolution



Local constant and sampling term in the expected range

R.S. Orr ATLAS Liquid Argon Calorimetry 19 October 2001

Summary of HEC Testbeam Results



R.S. Orr ATLAS Liquid Argon Calorimetry 19 October 2001

Test Beam Single Particle Energy Resolution



 $\frac{\sigma_E}{E} = \frac{a}{\sqrt{E}} \oplus b$

Noise subtracted energy resolution

$$a = (28.5 \pm 1.0)\% \cdot \sqrt{GeV}$$

 $b = (3.5 \pm 0.1)\%$

$$a = (94.2 \pm 1.6)\% \cdot \sqrt{GeV}$$

 $b = (7.5 \pm 0.4)\%$

Lar Endcap Installed in ATLAS

