

PHY 2408 : LONG PROBLEM SET 1

1- Calculate the cross section for the process

$e^+e^- \rightarrow Z \rightarrow \mu^-\mu^+$ in terms of the vector and axial couplings C_V and C_A , and given that the e^+e^- are unpolarized.

note: we did this in class but try to do it by yourself and if you get stuck, consult the notes

2- The forward-backward asymmetry that can be obtained from the process above can be written as: (see notes)

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} A_e A_\mu, \quad \text{with} \quad A_f = \frac{(c_V^f)^2 - (c_A^f)^2}{(c_V^f)^2 + (c_A^f)^2}$$

$$= \frac{2c_V^f c_A^f}{(c_V^f)^2 + (c_A^f)^2}$$

$\Rightarrow A_{FB} \propto C_V^2$ and

C_V is small for charged leptons

PROBLEM 2 Continued

(2)

now $\frac{c_V}{c_A} \propto \sin^2 \Theta_W$ so given that $A_{FB} \propto c_V^2$ and

c_V is small, the measurement of $\sin^2 \Theta_W$ will not be as accurate. We can do better with either incoming polarized beams, or by measuring the polarization of the outgoing particles which is possible with γ leptons.

- Let's start with polarized incoming beams. Assume that the electron beam is fully polarized but that the positron beam is unpolarized.

Show that
$$A_{LR} = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = A_e$$

with σ_L as the cross section for a left-handed electron beam, and σ_R is the same for a right-handed beam. The cross section is at the Z^0 resonance.

PROBLEM 3

Now we consider the process $e^+e^- \rightarrow Z \rightarrow \gamma^+\gamma^-$

The polarization of the γ leptons can be inferred using the momentum of the γ decay products.

- Show that the average tau polarization: $\frac{n_{\uparrow} - n_{\downarrow}}{n_{\uparrow} + n_{\downarrow}} = -A_{\tau}$

where n_{\uparrow} and n_{\downarrow} are the number of tau leptons produced in right-handed and left-handed helicity states.

→ this allows a measurement of $\sin^2\theta_w$ with a quantity that involves c_v (and not c_v^2)

→ the measurement is done as a function of $\cos\theta$: $P_{\tau}(\cos\theta)$

→ note that at lep, A_{FB} can be extracted using measurements away from the resonance, where its value is not small.