

Particle Detectors for Colliders

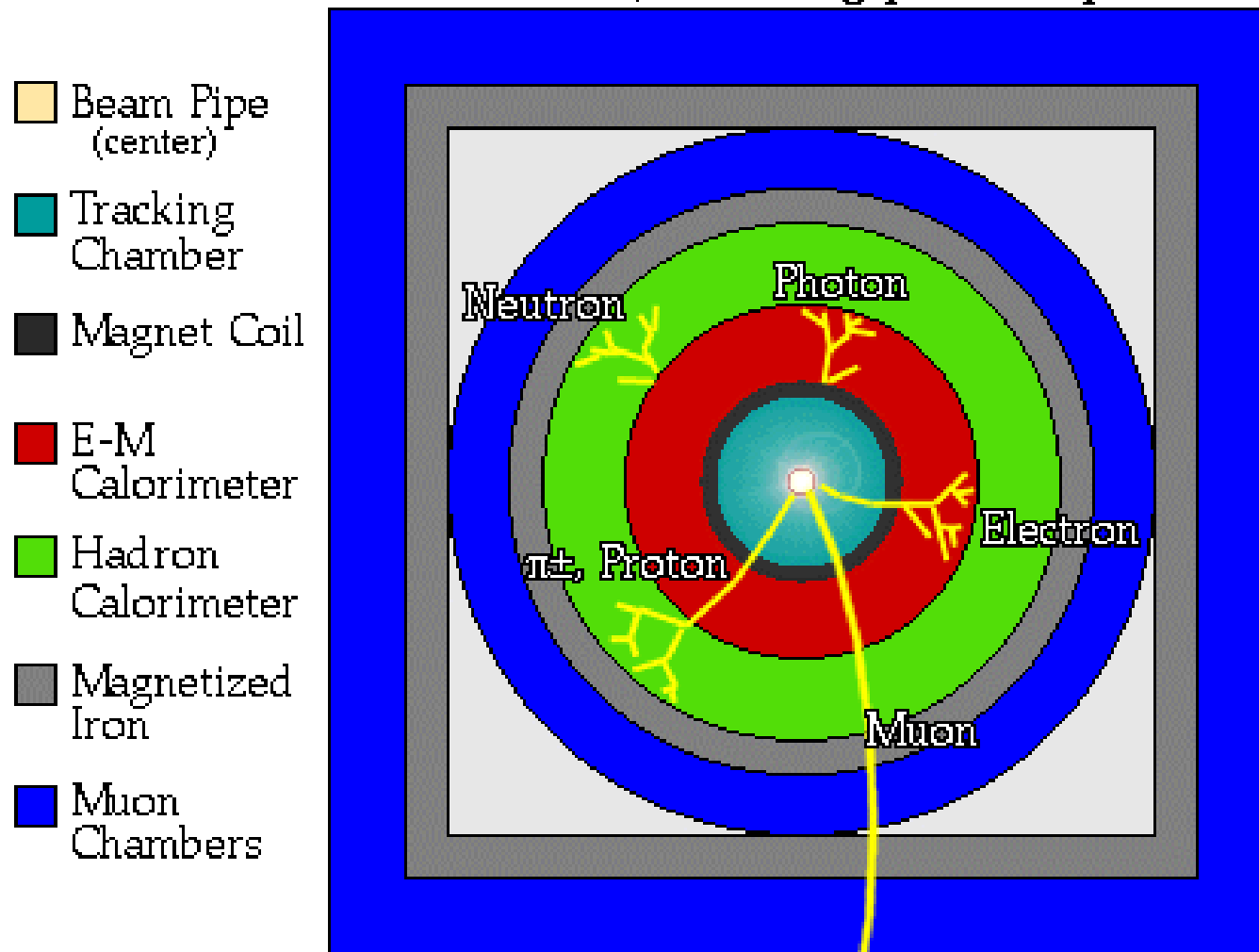
Semiconductor Tracking Detectors

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University of Toronto

Generic Detector

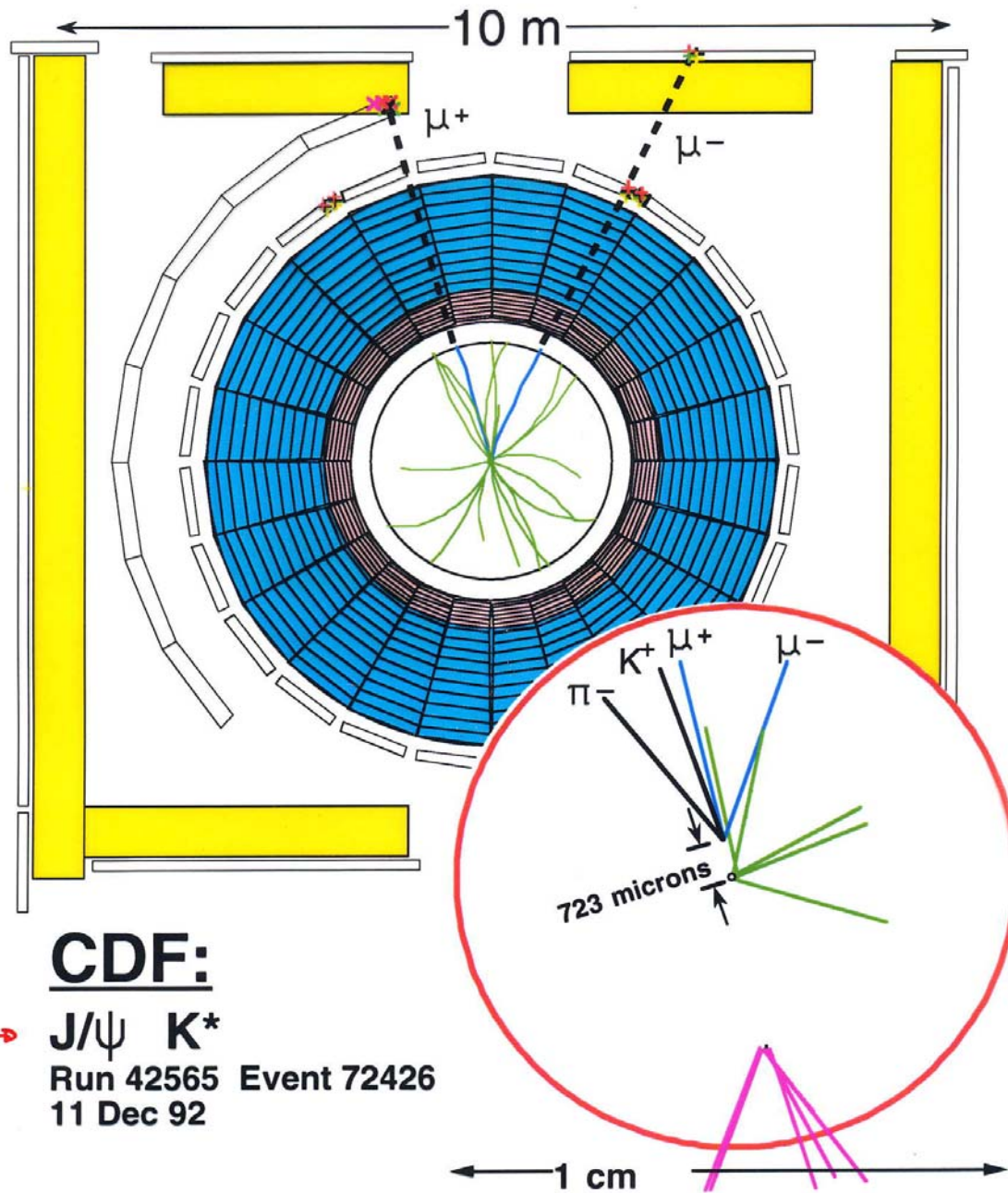
A detector cross-section, showing particle paths



► Layers of Detector Systems around Collision Point

Solid State Detectors

- Specifically
 - microstrip & pixel trackers
- Have become trackers of choice (if affordable)
 - high spatial resolution
 - radiation hard
 - rely on development of micro-electronics fabrication techniques
- Central to heavy flavour tagging, lifetimes
 - vertex detection
 - B flavour
 - Top
 - Higgs



CDF:

$B^0 \rightarrow$

$J/\psi K^*$

Run 42565 Event 72426
11 Dec 92

Top Quark Discovery at CDF

e + 4 jet event

40758_44414

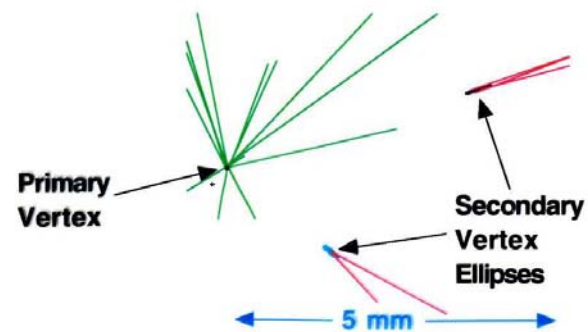
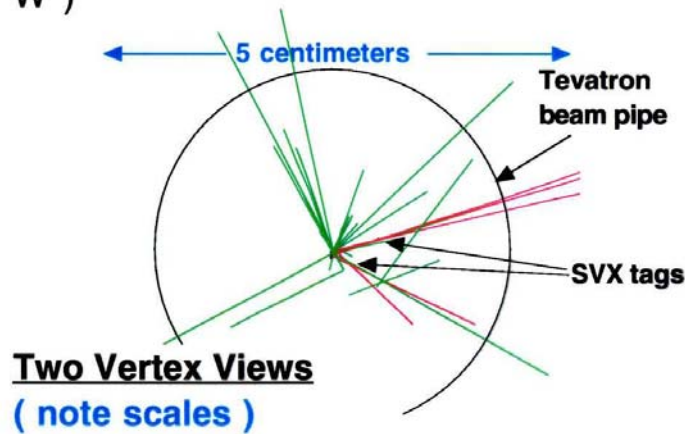
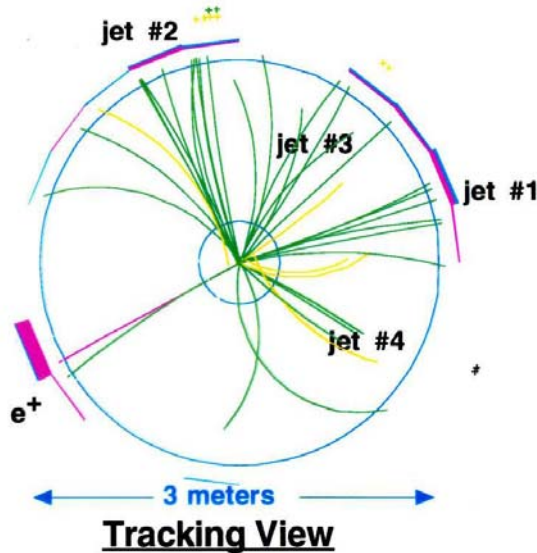
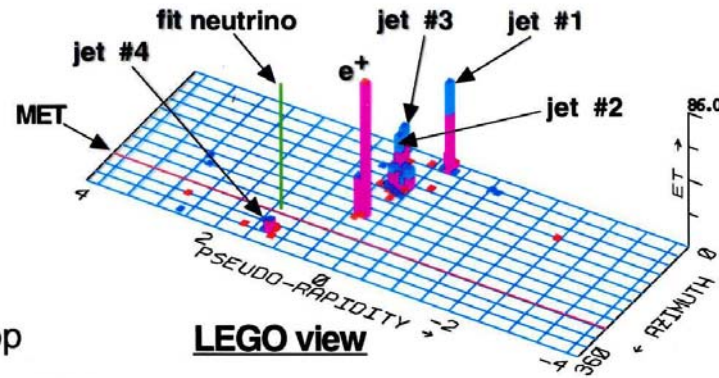
24-September, 1992

TWO jets tagged by SVX

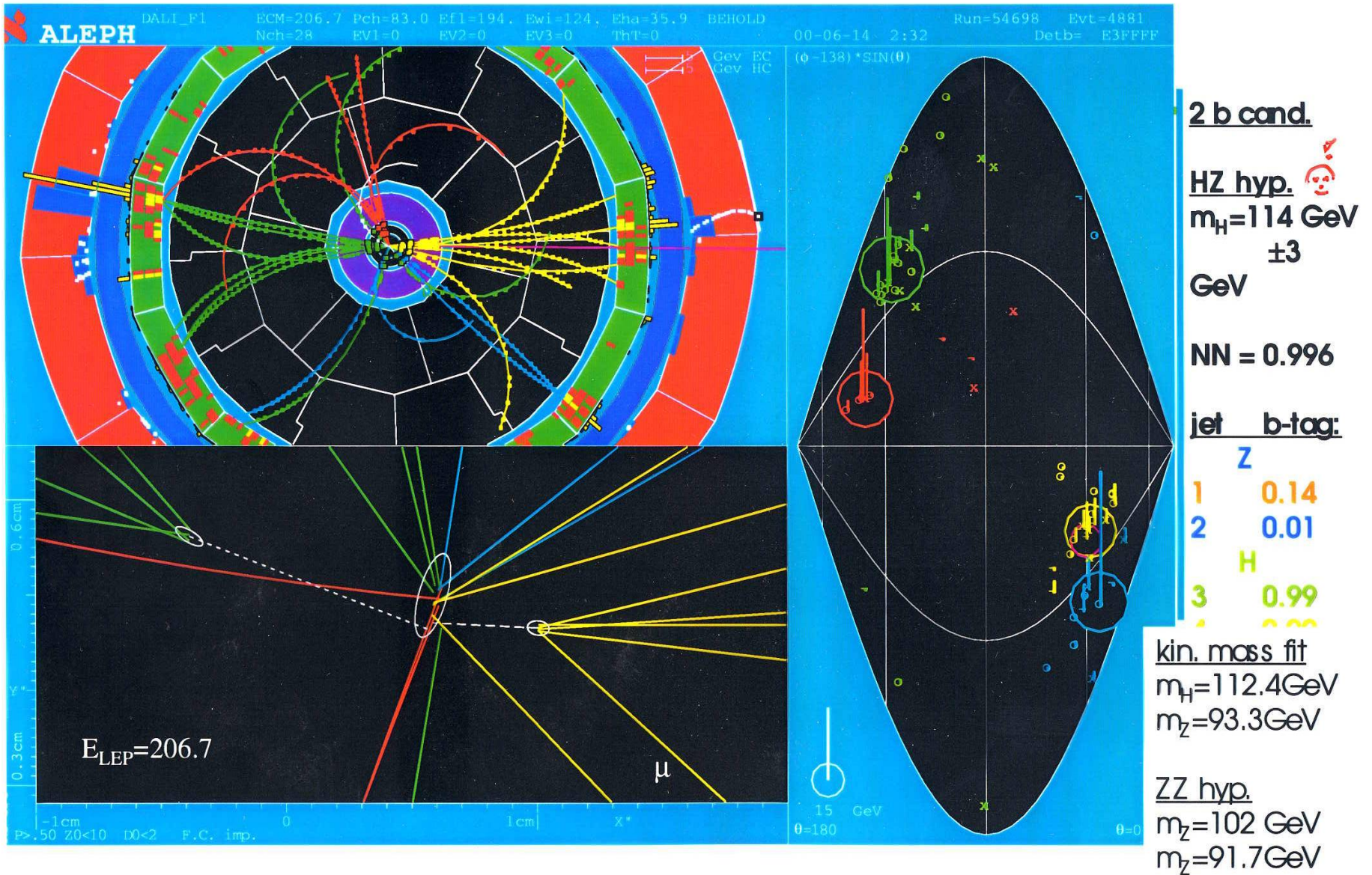
fit top mass is 170 +/- 10 GeV

e⁺, Missing E_t, jet #4 from top

jets 1,2,3 from top (2&3 from W)

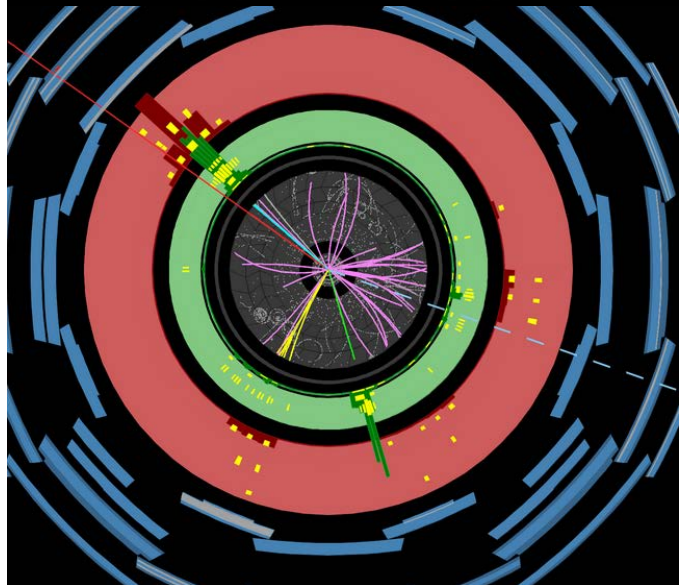


Utility of Si Tracker

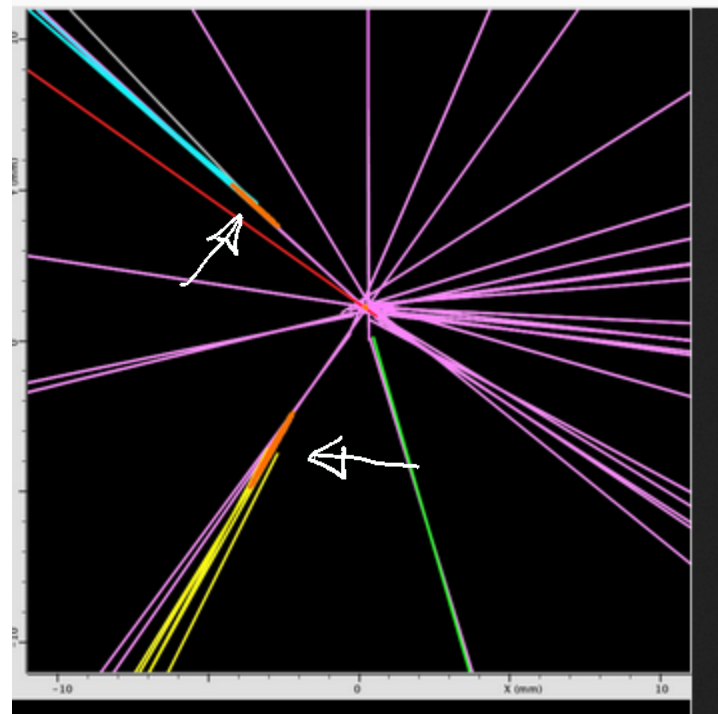


Run Number: 160958, Event Number: 9038972

Date: 2010-08-08 11:01:12 BST



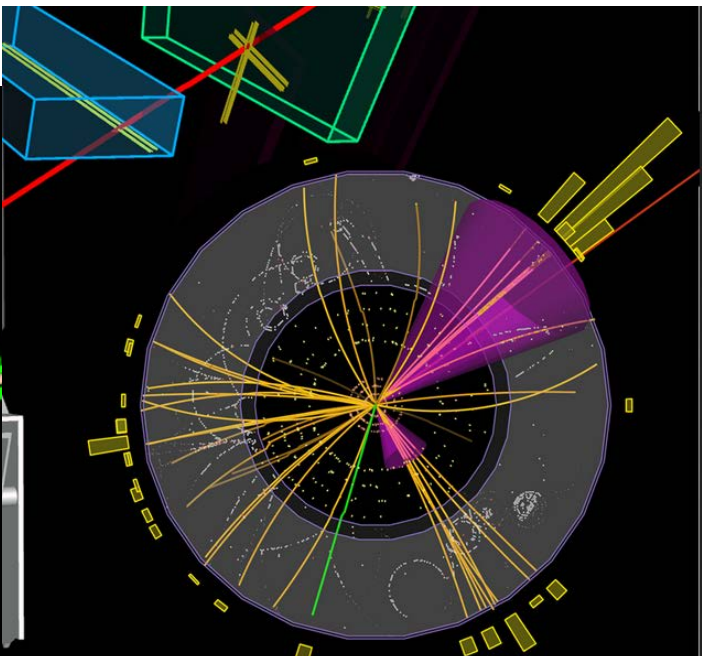
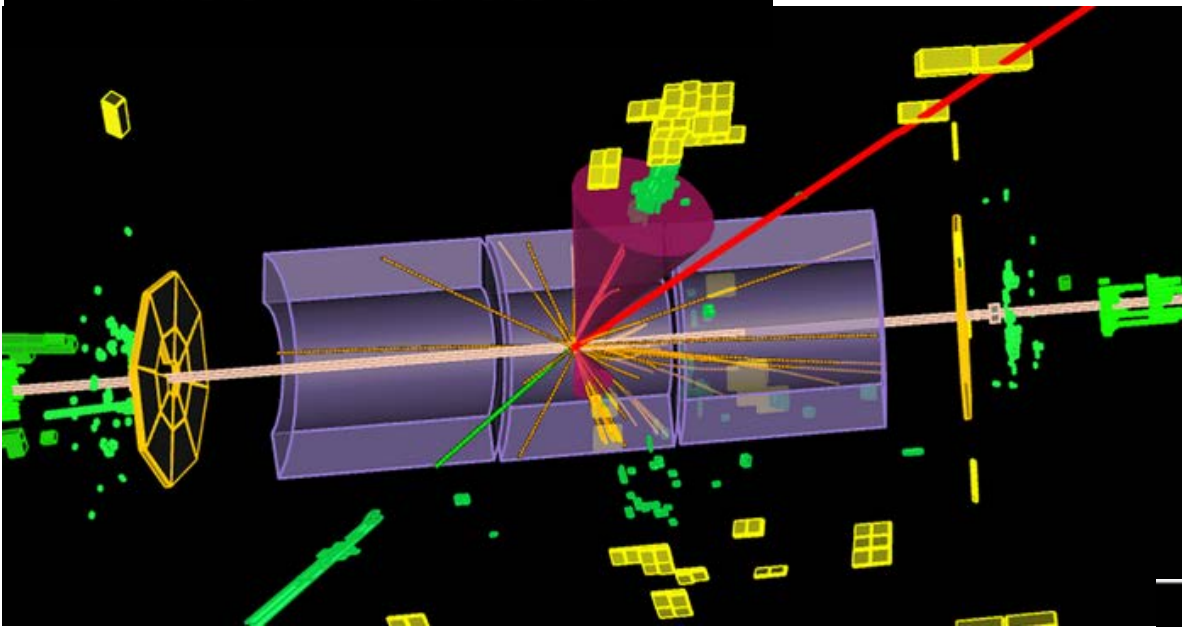
TOP PAIR
 $e\mu$ DIKEPTON



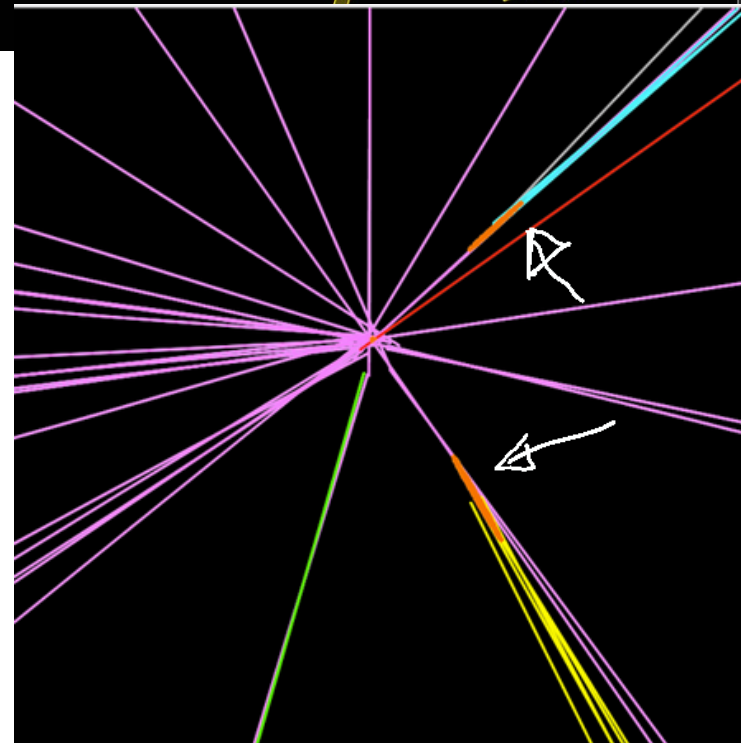
TWO TAGGED
B-JETS

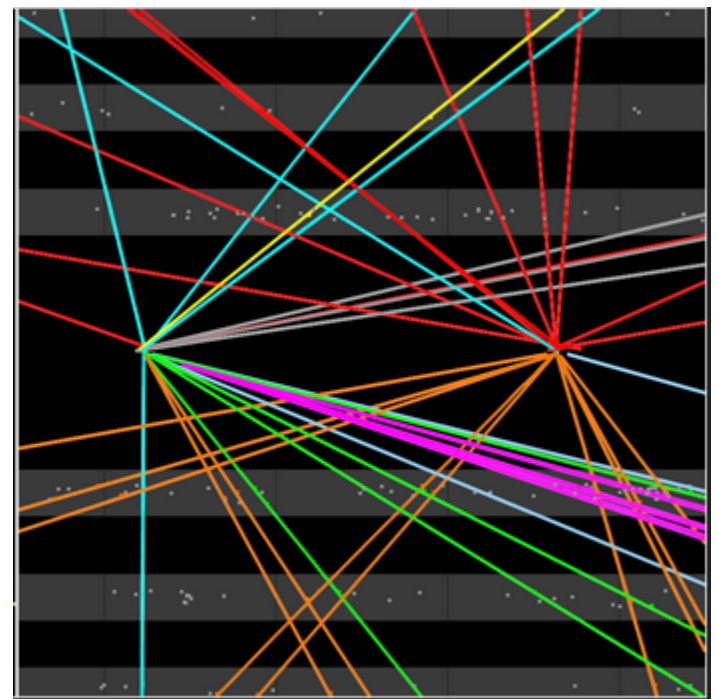
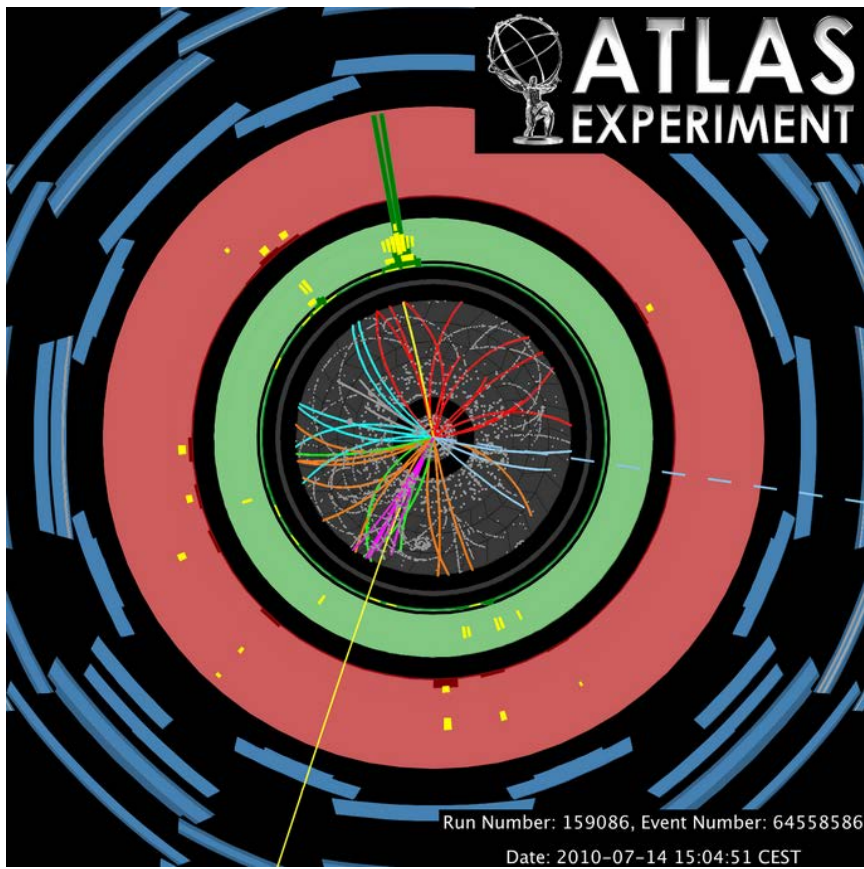
Run Number: 160958, Event Number: 9038972

Date: 2010-08-08 12:01:12 CEST



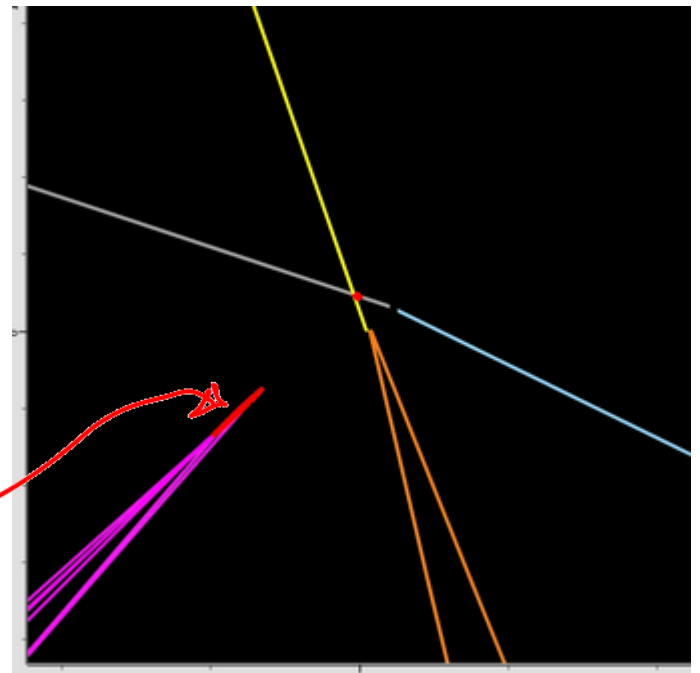
TOP PAIR $e\mu$ DILEPTON
TWO TAGGED B-JETS





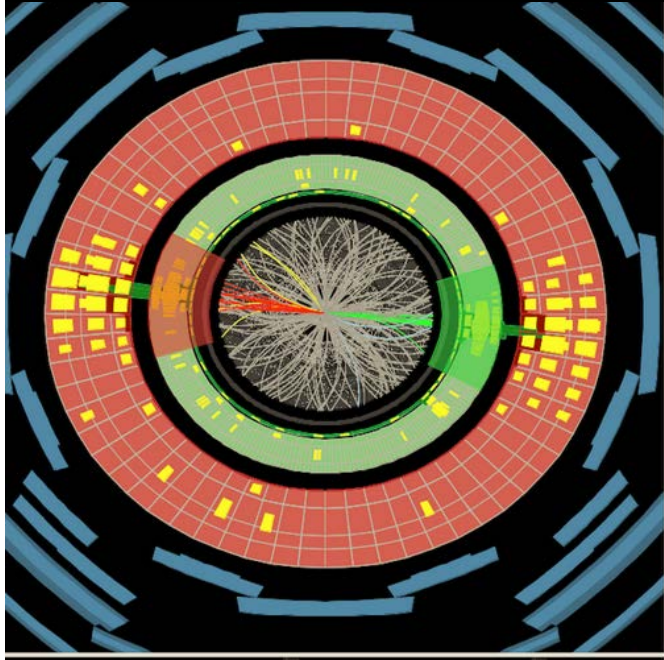
- IDENTIFY CORRECT PRIMARY
VERTEX

- TAG B-JET
SECONDARY VERTEX



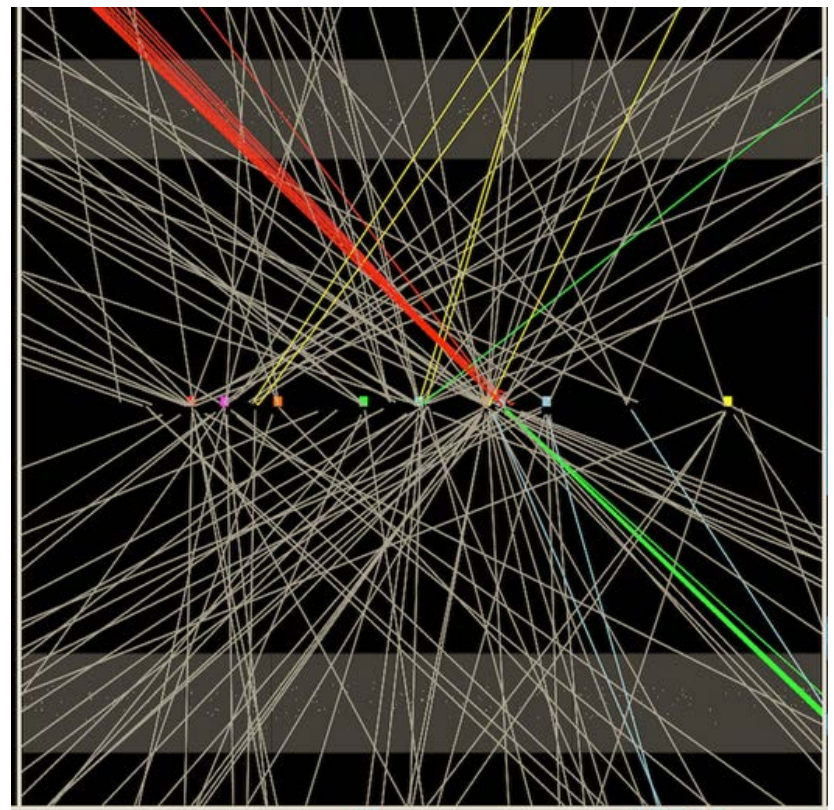
Run Number: 201269, Event Number: 80898559

Date: 2012-04-14 22:30:13 CEST



HIGH MASS DIJET

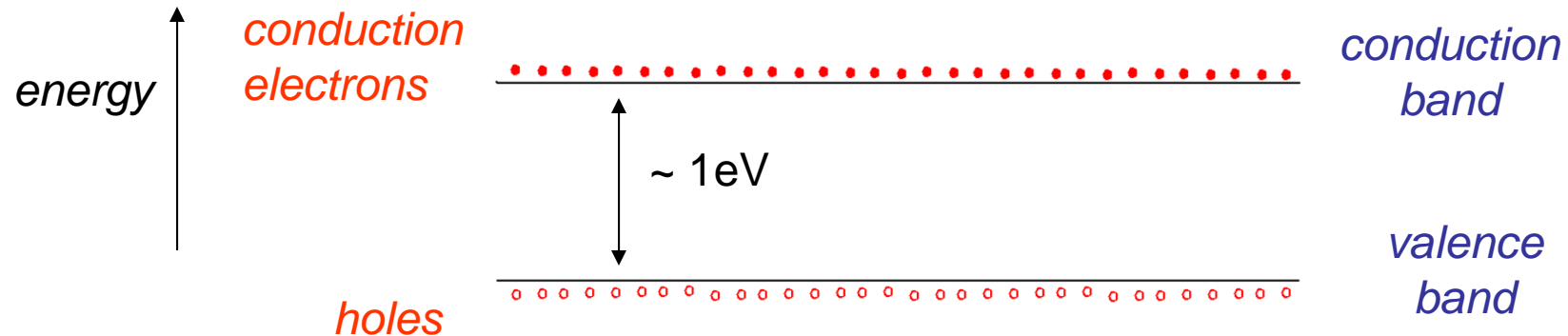
$$M_{JJ} = 4.23 \text{ TeV}$$



HIGH MULTIPLICITY
IDENTIFY CORRECT
PRIMARY VERTEX OUT
OF 9.

Semiconductors

- Have a large energy gap

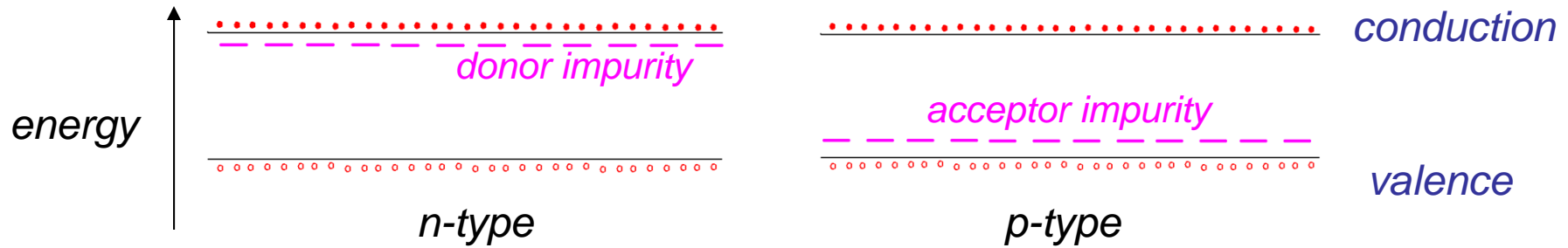


- Small number of charge carriers in conduction band
 - electrons thermally excited across the band gap

$$n_i = AT^{3/2} \exp\left(\frac{-E_g}{2kT}\right)$$

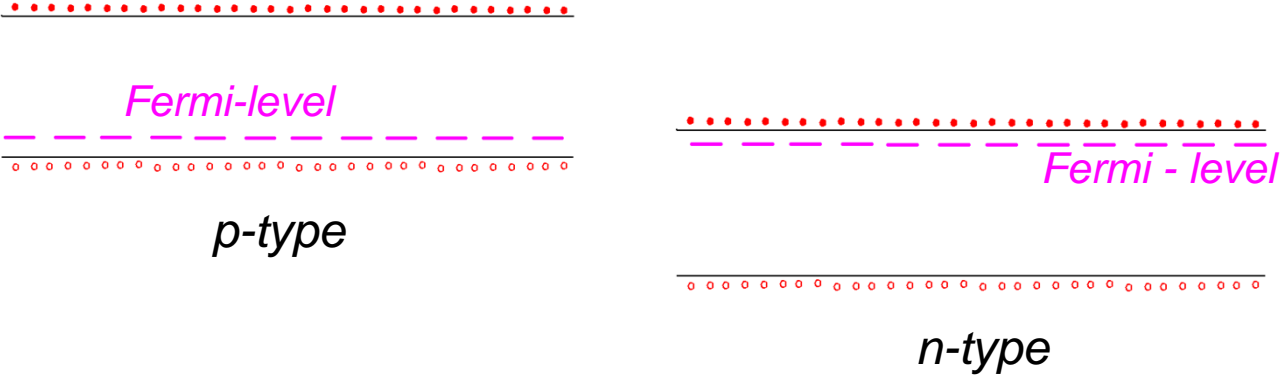
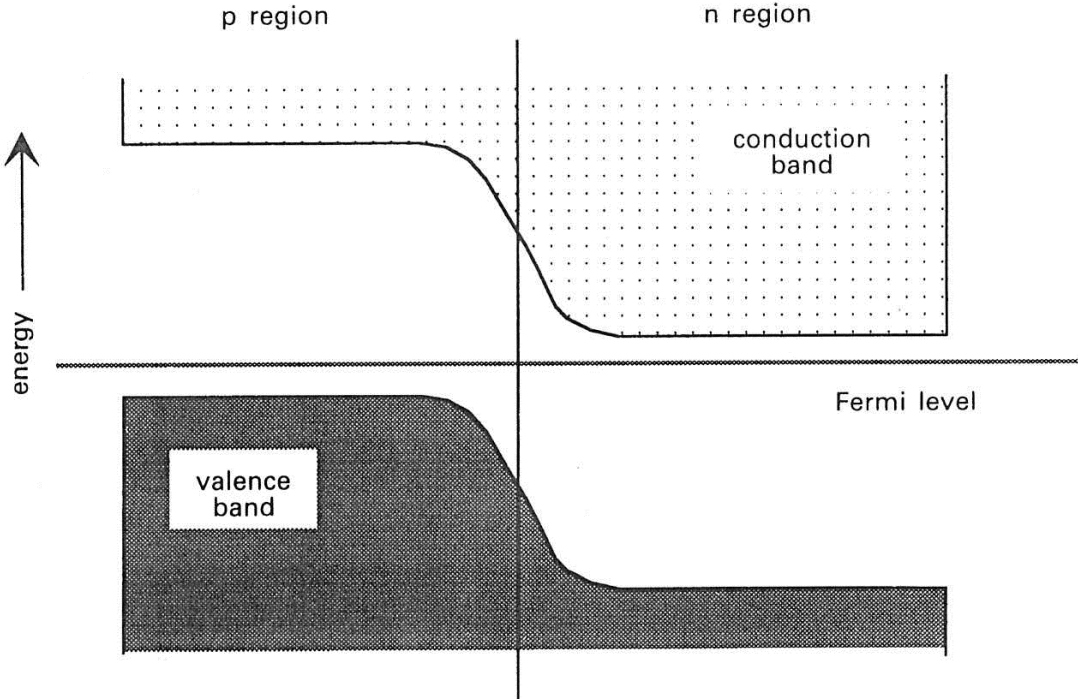
$n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ in pure silicon at room temp
increases with temperature

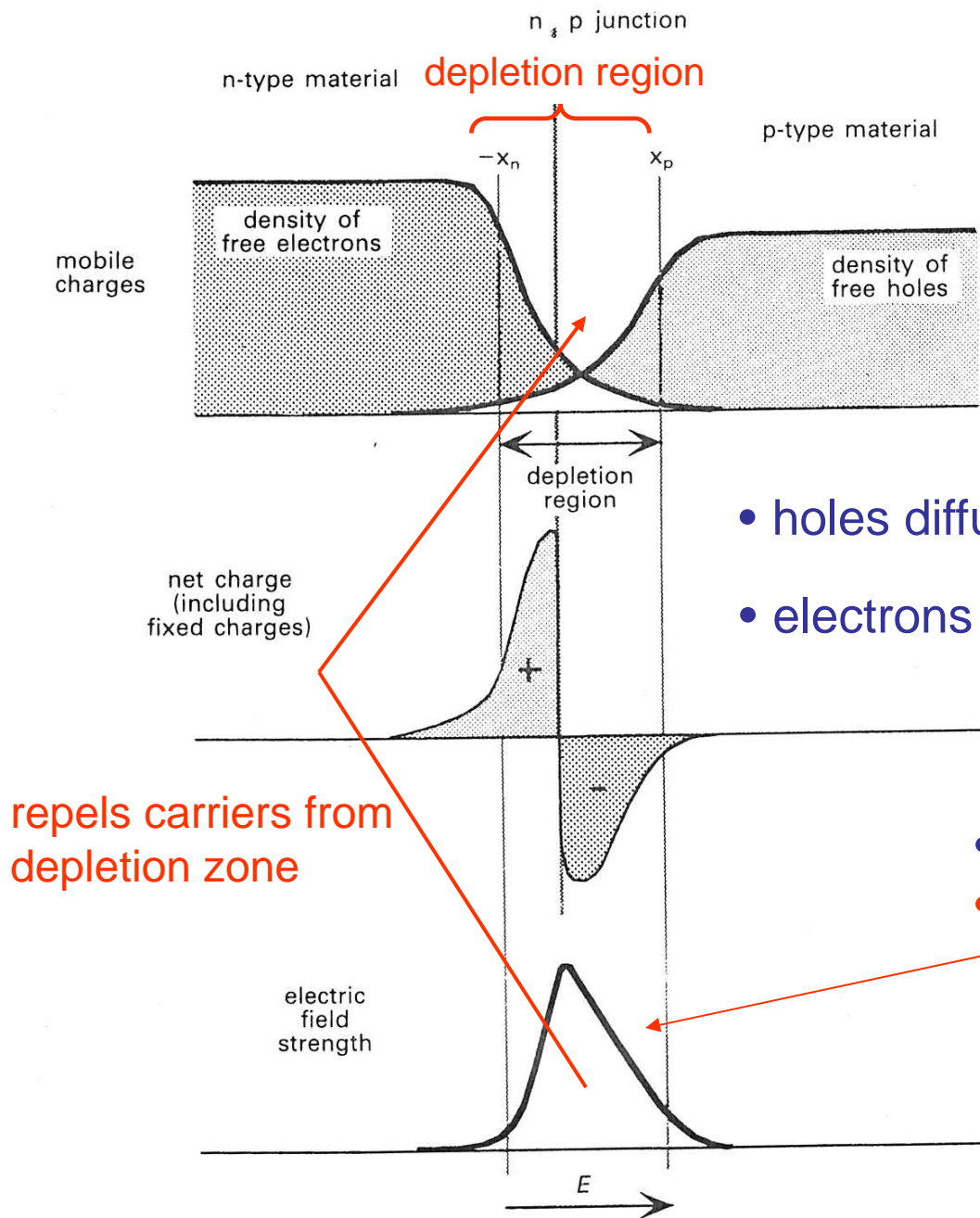
Doped Semiconductors



- In **n-type** , extra conduction **electrons** easily excited into conduction band
-increase conductivity
- In **p-type**, valence electrons excited into impurity band – **holes** in valence band conduct
 - n-type - electrons – majority carriers
 - **p-type** - **holes** – majority carriers

p-n Junction

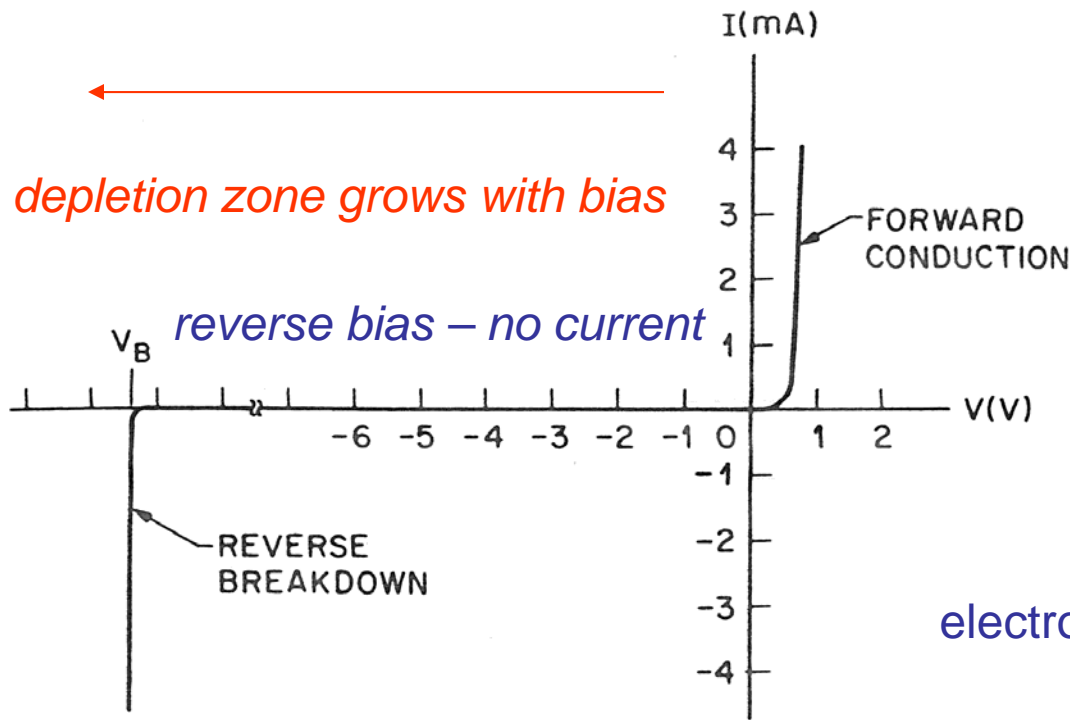




- Both n & p are initially electrically neutral

- holes diffuse into n-region - "fill" electrons
- electrons diffuse into p-region - "fill" holes

- charge buildup
- electric field



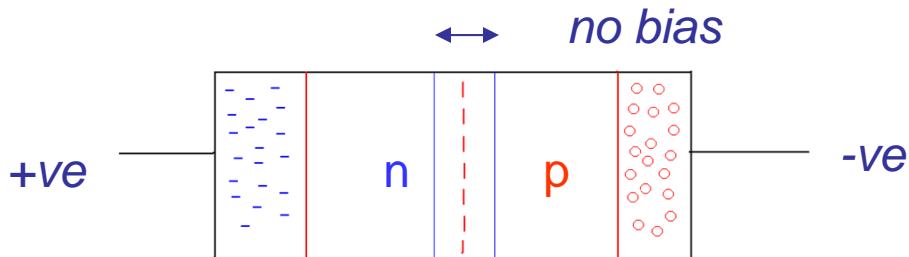
depletion zone grows with bias

reverse bias – no current

majority carrier current

electrons and holes have different mobility

$$\mu_H = \frac{1}{3} \mu_e$$



depletion zone with reverse bias

for $V_0 = 300V$ $d = 5\text{ mm}$ cf 75μ

need high resistivity Si for large bias voltage
- high purity or compensated

Depletion Zone as a Detector

- Reverse biased p-n junction – no majority carriers – no current
- Ionizing particle passing through depletion zone
- Liberates electron-hole pairs – current flows
- Intrinsic field not high enough to efficiently collect carriers – small signal
- Small depletion layer – large capacitance – large noise into electronics

- Depth of Depletion Zone

$$d = \left[2\epsilon\mu_e\rho(V_0 + V_B) \right]^{\frac{1}{2}}$$

$1.054 \times 10^{-12} \frac{F}{cm}$

dielectric constant

electron mobility

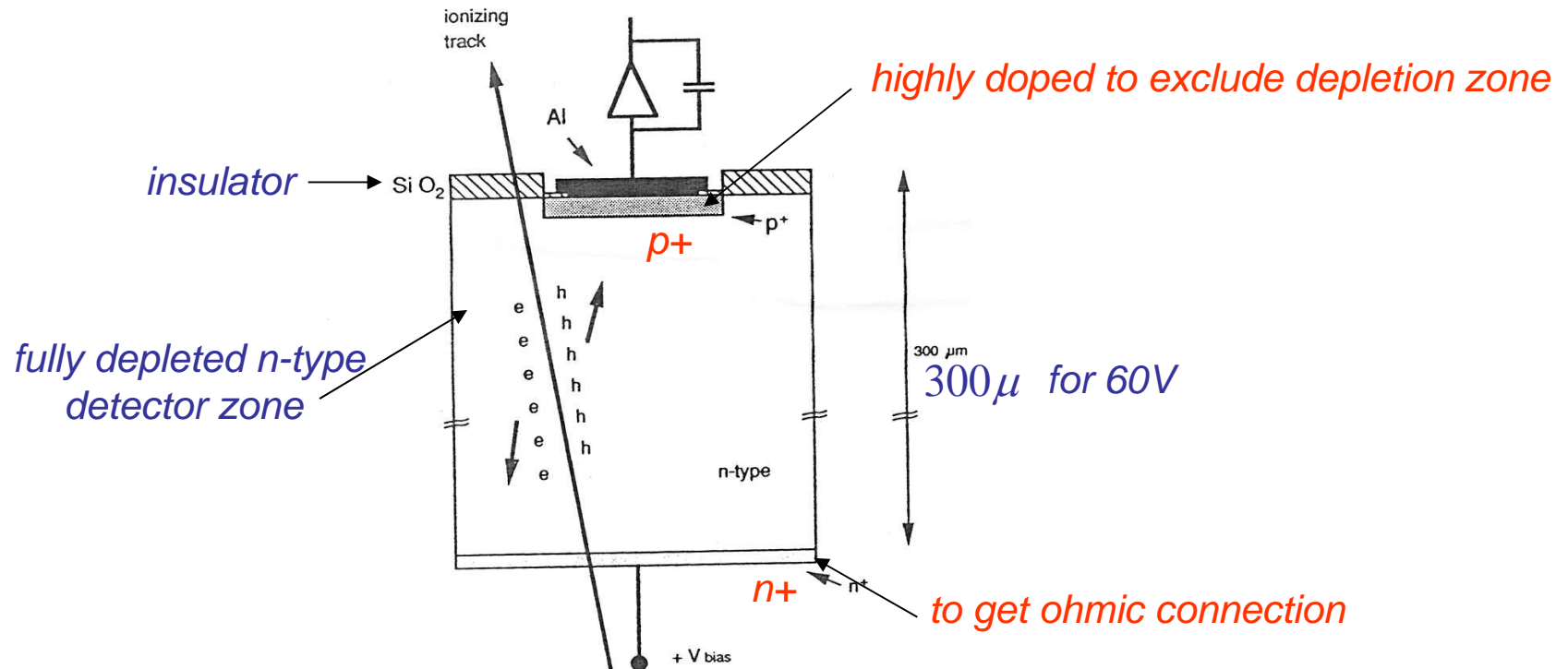
contact

$V_0 \approx 1V$

bias

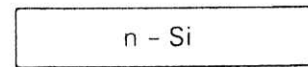
resistivity

Principle of micro-strip Detector

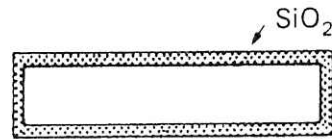


- 1 e-h pair / 3.6 eV - 10^2 e-h per micron - dense
- unlike gas – no multiplication of primary ionization 3×10^4 for 300 μ
- noise reduced by full depletion – reduce capacitance

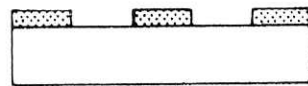
Fabrication



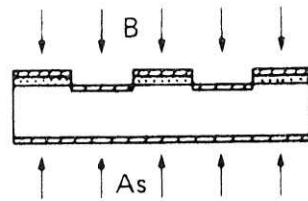
← n - Si WAFER



OXIDE PASSIVATION



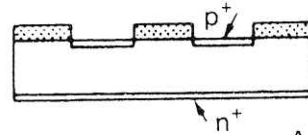
OPENING OF WINDOWS



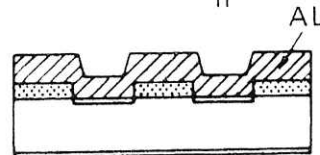
DOPING BY ION IMPLANTATION

B : 15 keV $5 \times 10^{14} \text{ cm}^{-2}$

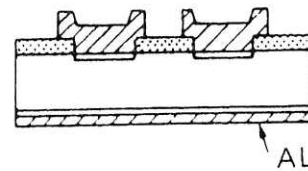
As : 30 keV $5 \times 10^{15} \text{ cm}^{-2}$



ANNEALING AT 600°C , 30 MIN



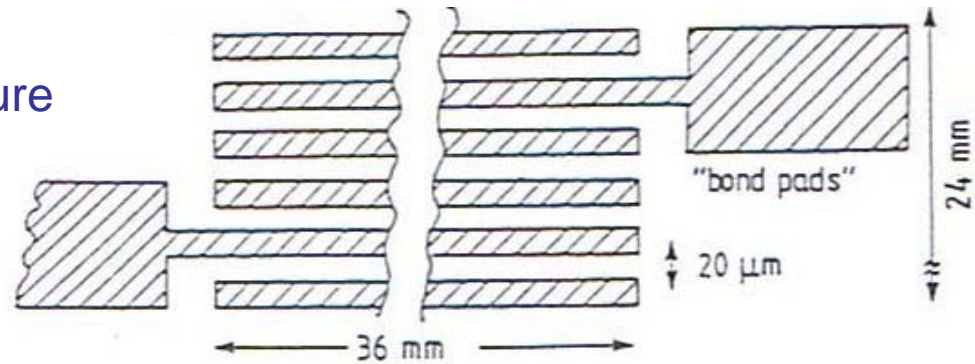
AL METALLIZATION



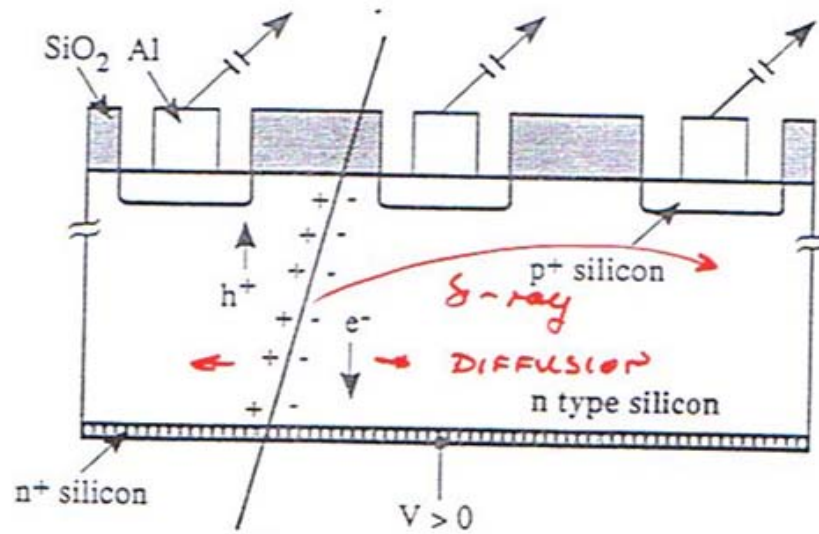
AL PATTERNING AT THE FRONT

AL - REAR CONTACT

- micro strip structure

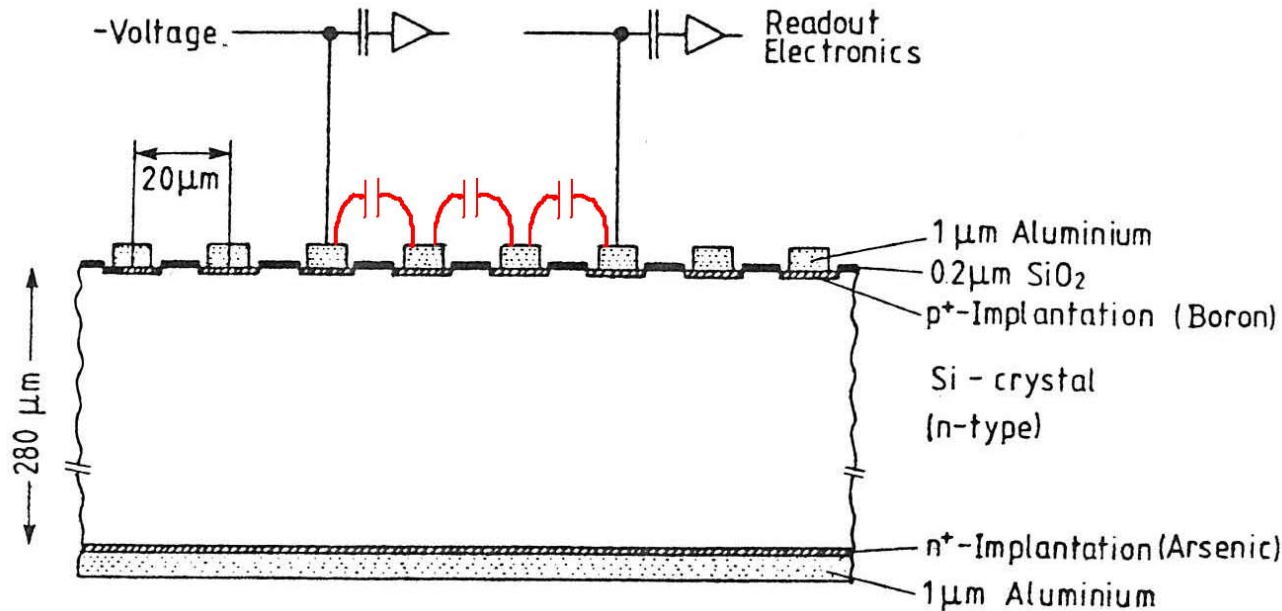


Strip pattern of the microstrip detector



- position resolution < 10 microns
- limited by diffusion and delta-rays

Capacitive Charge - Division

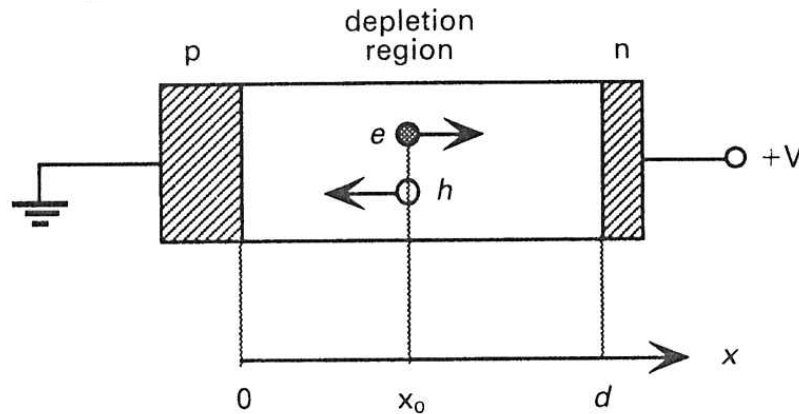


$$\sigma = \frac{\text{pitch}}{\sqrt{12}}$$

Cross-section of the microstrip detector with capacitive charge division

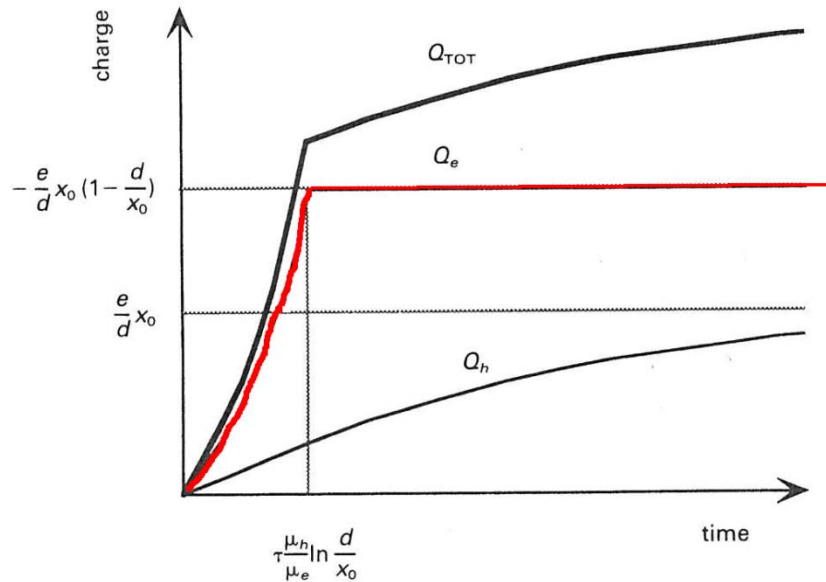
- many strips resulting from 20 µ pitch
 - ⇒ many electronics channels – many \$\$
- stray capacitive coupling of strips – read out every nth strip
 - ⇒ read out every 6th strip – effective 120 µ pitch -- $\sigma \sim 8 \mu$

Time Development of Signal



resistivity ρ

dielectric constant ϵ_s

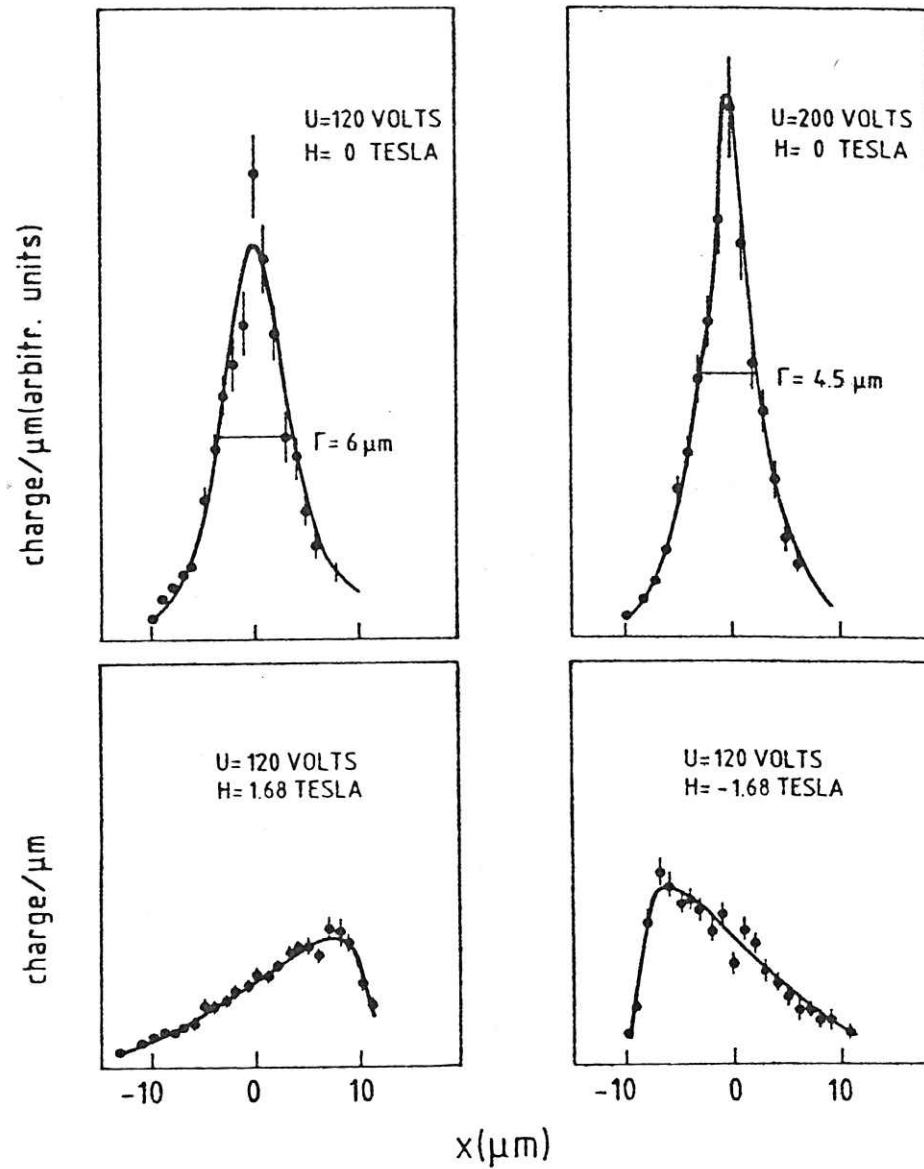


electrons dominate rise time

$$Q_e = \frac{e}{d} x_0 \left(1 - \exp \frac{\mu_e t}{\mu_h \tau} \right)$$

$$Q_h = \frac{e}{d} x_0 \left(1 - \exp \frac{\mu_h t}{\mu_h \tau} \right)$$

$$\tau = \epsilon_s \rho$$

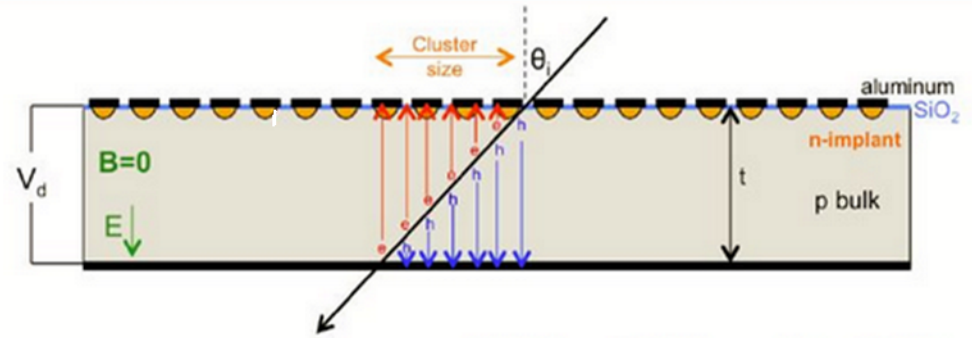
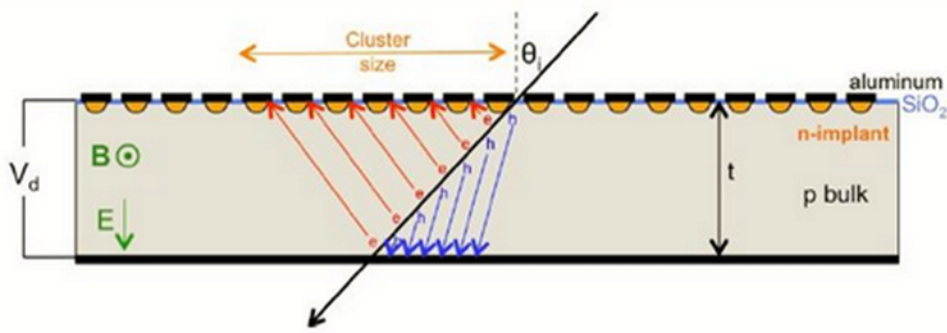


field off

- Effect of magnetic field on space resolution

field on

LORENTZ ANGLE IN B-FIELD



With Magnetic field

Without Magnetic field

$$\text{Cluster Size} \approx t \cdot \tan \theta_L$$

LORENTZ ANGLE

$$\tan(\theta_L) = \mu_H B = \mu_H / \mu_d B$$

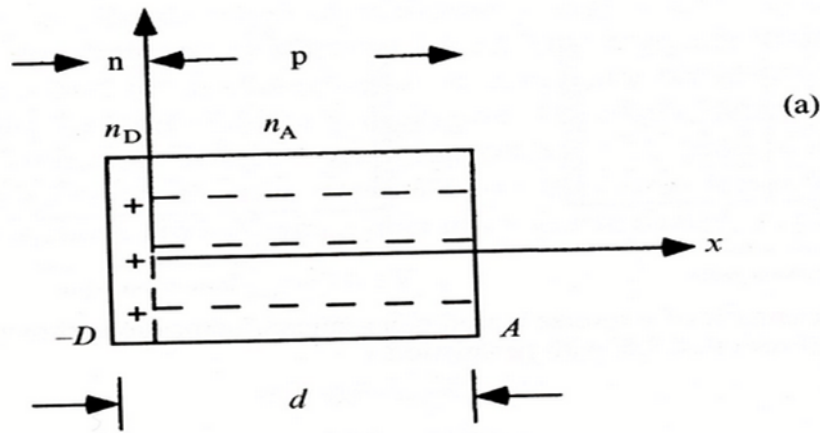
HALL MOBILITY

DRIFT MOBILITY
HALL FACTOR

$$\mu_d = \frac{v_s / E_c}{\left[1 + \left(\frac{E}{E_c} \right)^\beta \right]^{1/\beta}}$$

E_c, β - PARAMETERS - SEE ATLAS-INDET-2001-004

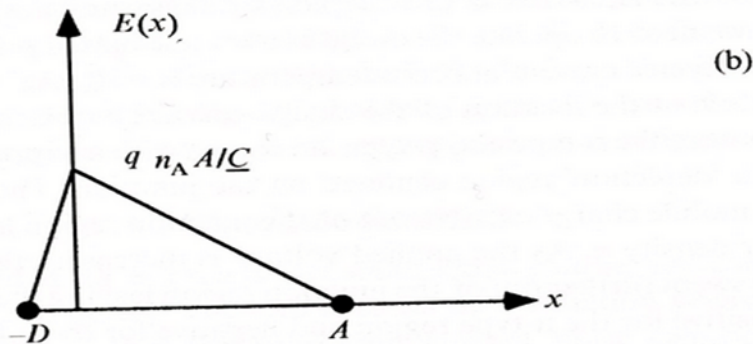
CALCULATING THE DEPLETION DEPTH



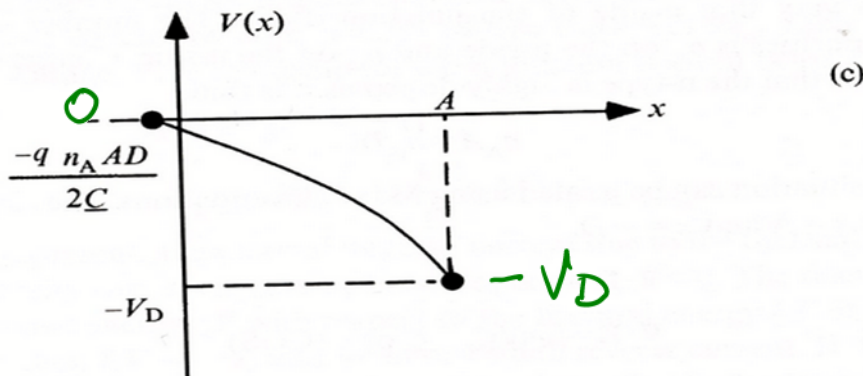
FULLY DEPLETED JUNCTION

N_D = NUMBER DENSITY OF DONOR IMPURITIES

N_A = NUMBER DENSITY OF ACCEPTOR IMP.



BEHAVIOUR OF ELECTRIC FIELD.



VOLTAGE

Fig. 9.4. (a) Geometry of a p-n junction. The static charge number density is n_D . (b) Electric field for a p-n junction.

USE $\vec{\nabla} \cdot \vec{E} = \frac{q n}{\epsilon}$

CHARGE ON ELECTRON
 NUMBER DENSITY
 ACTUALLY $\epsilon_r \epsilon_0$

TO GET THE ELECTRIC FIELD

$$\int_{x_1}^{x_2} \vec{\nabla} \cdot \vec{E} dx = \left[\frac{q n}{\epsilon} \cdot x \right]$$

$$E(x > 0) [0 \rightarrow A] = \left[\frac{q n}{\epsilon} \right]_x^A = \frac{-q n_A [x - A]}{\epsilon}$$

$$E(x < 0) [-D \rightarrow x] = \left[\frac{q n}{\epsilon} \right]_{-D}^x = \frac{q n_D [x + D]}{\epsilon}$$

THE JUNCTION HAS TO REMAIN ELECTRICALLY NEUTRAL

$$n_A \cdot A = n_D \cdot D$$

$$E(x < 0) = q \left\{ \frac{n_A \cdot A}{D} \right\} \left\{ \frac{x + D}{\epsilon} \right\}$$

NOW WE WANT TO GET THE VOLTAGE DISTRIBUTION

$$\vec{E} = -\vec{\nabla} V \rightarrow \int \vec{E} = -V$$

$\int \vec{E}_s$ ON LAST PAGE

$$V(x=A) = -V_D$$

$$V(x=-D) = 0$$

↑ WE CAN
CHOOSE THIS

$$V(x>0) = \int q n_A \cdot \frac{x}{\epsilon} dx - \int \frac{q n_A \cdot A}{\epsilon}$$

$$= q n_A \frac{x^2}{2\epsilon} - q n_A \frac{x \cdot A}{\epsilon} + K \quad \text{①}$$

WHEN $x=A$, $V = -V_D$

$$-V_D = q \frac{n_A}{\epsilon} \left(\frac{A^2}{2} - A^2 \right) + K$$

$$-V_D = -q \frac{n_A}{\epsilon} \left(\frac{A^2}{2} \right) + K$$

$$K = q \frac{n_A}{\epsilon} \frac{A^2}{2} - V_D$$

$$K = q \frac{n_A}{\epsilon} \frac{A^2}{2} - V_D$$

NOTICE THAT $\frac{(x-A)^2}{2} = \frac{x^2}{2} - Ax + \frac{A^2}{2}$

FROM ① ABOVE \rightarrow PUTTING IN VALUE OF K

$$V(x > 0) = \frac{q n_A}{\epsilon} \left\{ x^2 - Ax + \frac{A^2}{2} \right\} - V_D$$

$$V(x > 0) + V_D = \frac{q n_A}{\epsilon} \frac{(x-A)^2}{2} \quad \text{--- ②}$$

NOW DO SAME THING FOR $x < 0$

$$V(x < 0) = - \int q \frac{n_A \cdot A}{D} \left(\frac{x+D}{\epsilon} \right) dx$$

$$= -q \frac{n_A \cdot A}{D} \frac{x^2}{2\epsilon} - q n_A \cdot \frac{AD}{D\epsilon} \cdot x + K$$

$$V(x) = -q \frac{\rho_A \cdot A}{D} \frac{x^2}{2\epsilon} - q \rho_A \cdot \frac{A D}{D\epsilon} x + K$$

AT $x = -D$, $V = 0$ BY DEFINITION

$$0 = -q \frac{\rho_A \cdot A}{D} \cdot \frac{D^2}{2\epsilon} + q \frac{\rho_A \cdot A \cdot D^2}{D\epsilon} + K$$

$$K = q \rho_A \cdot \frac{A D^2}{D 2\epsilon} - \frac{q \rho_A \cdot D \cdot A}{\epsilon}$$

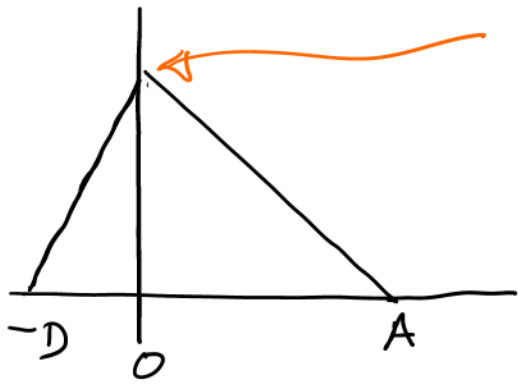
$$= q \rho_A \frac{A \cdot D}{2\epsilon} - \frac{q \rho_A A \cdot D}{\epsilon}$$

$$K = -q \rho_A \frac{DA}{2\epsilon}$$

$$V(x < 0) = -q \frac{\rho_A A}{D\epsilon} \left(-\frac{x^2}{2} - x - \frac{D}{2} \right) = -q \frac{\rho_A}{D\epsilon} \frac{(x+D)^2}{2} \quad (3)$$

VOLTAGE HAS TO BE CONTINUOUS

AT THE JUNCTIONS



$$V(x < 0) = V(x > 0) \text{ AT } x = 0$$

$$-\frac{q \cdot n_A \cdot A (x+D)^2}{2D\epsilon} = \frac{q \cdot n_A}{2\epsilon} (x-A)^2 - V_D$$

$$V_D = \frac{q \cdot n_A \cdot A (x+D)^2}{2D\epsilon} + \frac{q \cdot n_A}{2\epsilon} (x-A)^2$$

$$= q \cdot n_A \left[\left\{ \frac{x^2}{D} + D + \frac{2Dx}{D} \right\} + x^2 - 2Ax + A^2 \right]$$

$x=0$

$$= \frac{q \cdot n_A}{2\epsilon} \left\{ AD^2 + A^2 \right\}$$

$$V_D = \frac{q \cdot n_A}{2\epsilon} A (A+D)$$

WHAT WE
WANTED

$$V_D = \frac{q \rho_A}{2\epsilon} A (A+D)$$

USUALLY DETECTORS HAVE ASYMMETRIC DOPING

FOR EXAMPLE IF $n_D \gg n_A, A \gg D$

$$d = A + D \rightarrow A$$

$$V_D = \frac{q \rho_A d^2}{2\epsilon}$$

DO NOT
CONFUSE
WITH ρ

n LAYER IS VERY THIN, PUT $n_A = p$

$$E(x > 0) = -q \rho_A (x-A) / \epsilon \rightarrow -q p (x-d) / \epsilon$$

$$V(x > 0) = \frac{q \rho_A (x-A)^2}{2\epsilon} - V_D \rightarrow \frac{q p (x-d)^2}{2\epsilon} - V_D$$

PUTTING $V(x=0) \sim 0$

BIAS VOLTAGE $\rightarrow V_D = \frac{[q p] d^2}{2\epsilon}$ \leftarrow DEPTH OF DEPLETION ZONE

$$V_D = \frac{[qP] d^2}{2\epsilon}$$

$$d = \left(\frac{2\epsilon V_D}{qP} \right)^{\frac{1}{2}}$$

RESISTIVITY

$$\rho = \frac{1}{q\mu n_A} = \frac{1}{q\mu P}$$

$$\frac{1}{qP} = \mu\rho$$

$$d = \sqrt{2\epsilon\rho\mu V_D}$$

CAN PUT IN THE CONTACT POTENTIAL $V_D \approx 1V$

$$d = \sqrt{2\epsilon\rho\mu(V_D + V_0)}$$

$V_D =$ BIAS VOLTAGE - 300V IN MODERN DETECTOR

TIME DEVELOPMENT OF SIGNAL PULSE

WE HAVE CHARGES MOVING IN AN ELECTRIC FIELD

$$E(x) = -q/p (x-d)/\epsilon, \text{ BUT } \frac{qP}{\epsilon} = \frac{2V_0}{d^2}$$

$$E(x) = -\frac{2V_0}{d^2} (x-d)$$

TAKE SIMPLE CASE OF POINT IONIZATION @ $x=0$
 $t=0$
FOR THE MOVING CHARGE

$$dx = \mu E dt = -\mu \frac{2V_0}{d^2} (x-d) dt$$

$$\int_{x_i}^{x_f} \frac{dx}{x-d} = -\mu \frac{2V_0}{d^2} \int_0^t dt$$

$$\ln(x_f - d) - \ln(x_i - d) = -2\mu \frac{V_0}{d^2} \cdot t$$

$$\ln \left\{ \frac{x_f - d}{x_i - d} \right\} = - \left(\frac{2\mu V_D}{d^2} \right) \cdot t$$

$\rightarrow \frac{1}{\tau_D}$

τ_D IS TIME FOR A CHARGE TO MOVE THRU DISTANCE d IN FIELD $E(0)$

$$x_f - d = (x_i - d) e^{-t/\tau_D}$$

$x \rightarrow 0$

$$x_f = d(1 - e^{-t/\tau_D})$$

USING $\left\{ \begin{array}{l} \text{POTENTIAL ENERGY} \\ \text{CHANGE} \end{array} \right\} =$ WORK DONE FOR CHARGE MOVING IN $E(x)$

\rightarrow CURRENT $I(t) = \frac{dq}{dt} =$

$$\mu q_s \frac{E^2}{V_D}$$

TOTAL SIGNAL CHARGE

NEED THIS

$$E(x) = -\frac{2V_D}{d^2} (x-d)$$

$$E^2(x) = \frac{4V_D^2}{d^4} \left[d(1 - e^{-t/\tau_D}) - d \right]^2$$

$$E^2(x) = \frac{4V_D^2}{d^4} \cdot d^2 e^{-2t/\tau_D}$$

$$\text{so } I(t) = \frac{\mu q_s}{V_D} \cdot \frac{4V_D^2}{d^2} e^{-2t/\tau_D}$$

$$= \mu q_s \frac{4V_D}{d^2} e^{-2t/\tau_D} \quad \mu = \frac{d^2}{2\tau_D V_D}$$

$$I(t) = 4 q_s \frac{d^2}{2\tau_D} \cdot \frac{1}{d^2} e^{-2t/\tau_D}$$

$$I(t) = \frac{2q_s}{\tau_D} \cdot e^{-2t/\tau_D}$$

Signal from Si Detector

SAME TREATMENT
AS SIGNAL IN GAS TUBE

$$\begin{aligned} I(t) &= \frac{dQ}{dt} = \frac{\mu q_s E^2}{V_B} \\ &= \frac{4\mu q_s V_B}{d^2} \exp\left(-\frac{2t}{\tau_D}\right) \\ &= \frac{2q_s}{\tau_D} \exp\left(-\frac{2t}{\tau_D}\right) \end{aligned}$$

$$I(0) = \frac{2q_s}{\tau_D}$$

$$I(\infty) = 0$$

$$\tau_D = \frac{d^2}{2\mu V_D} = \frac{d}{\mu E(0)}$$

• for a source charge $q_s \sim 5fC$

• peak electron (hole) current 710 nA (240 nA)

• How does this compare to the noise level?

electron mobility $\mu_e \sim 1400 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$

drift velocity $\sim 42 \mu \text{ ns}^{-1}$

for 300μ $\tau_D \sim 7 \text{ ns}$

DEPLETION LAYER PROPERTIES

FOR A PARALLEL PLATE CAPACITOR

$$C = \frac{\epsilon A}{d} \quad \leftarrow \text{AREA}$$

CAPACITANCE PER UNIT AREA

$$\frac{C}{A} = \frac{\epsilon}{d} = \sqrt{\frac{1}{2\mu\rho(V_0+V_D)}}$$

INCREASING $V_D \rightarrow \frac{C}{A} \propto \frac{1}{\sqrt{V_D}}$

$$\text{IN } d = \sqrt{2\epsilon\mu\rho(V_0+V_D)} \quad \text{PUT } \rho = \frac{1}{q\mu n_A}$$

$$d = \sqrt{\frac{2\epsilon(V_0+V_D)}{q n_A}} \quad \leftarrow \text{DOPING CONCENTRATIONS}$$

$$d \propto \left(\frac{1}{n_A}\right)^{1/2}$$

$$d \propto \left(\frac{1}{n_A} \right)^{1/2}$$

- ONLY CHARGES RELEASED IN THE DEPLETION ZONE ARE COLLECTED & GIVE A SIGNAL
- HIGH DOPING \rightarrow SMALL d
- FOR SMALL DOPING \rightarrow NEED INTRINSIC CARRIER CONCENTRATION SMALL.

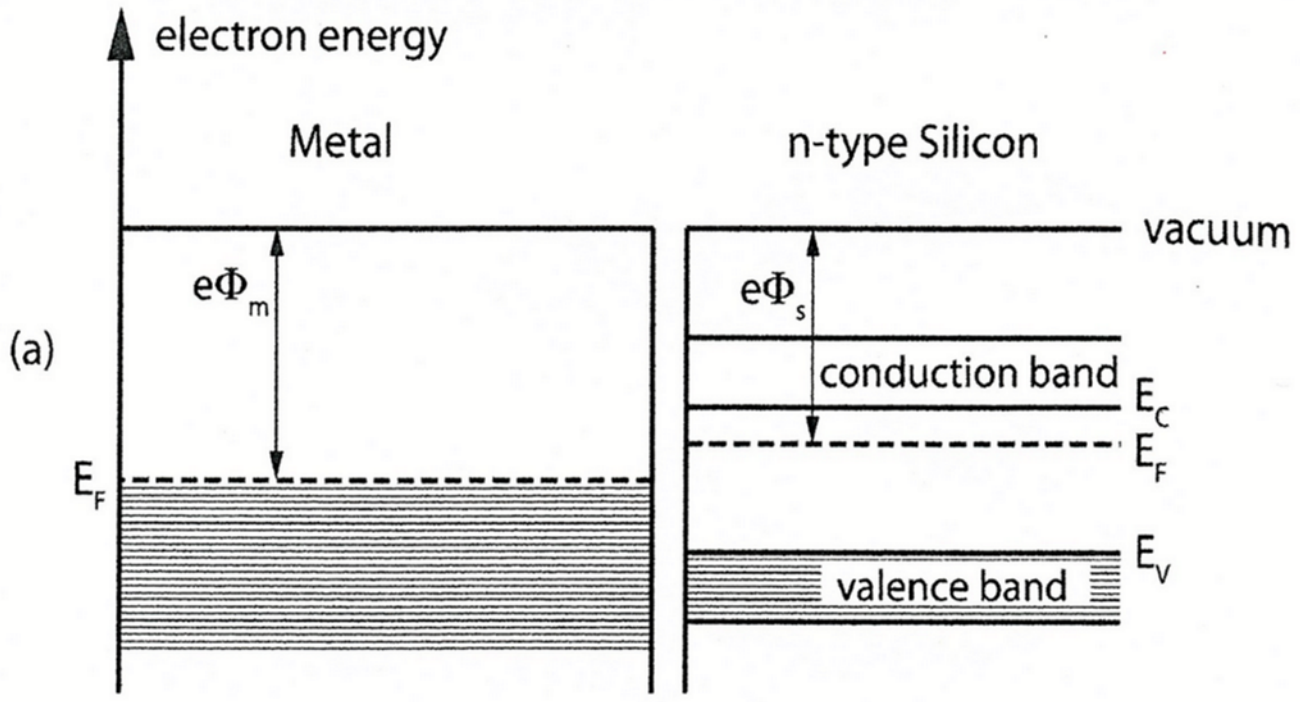
RESISTIVITY $\rightarrow \rho = \frac{1}{q n_i \mu}$ $n_i \rightarrow$ INTRINSIC

NEED HIGH RESISTIVITY (PURITY) SILICON

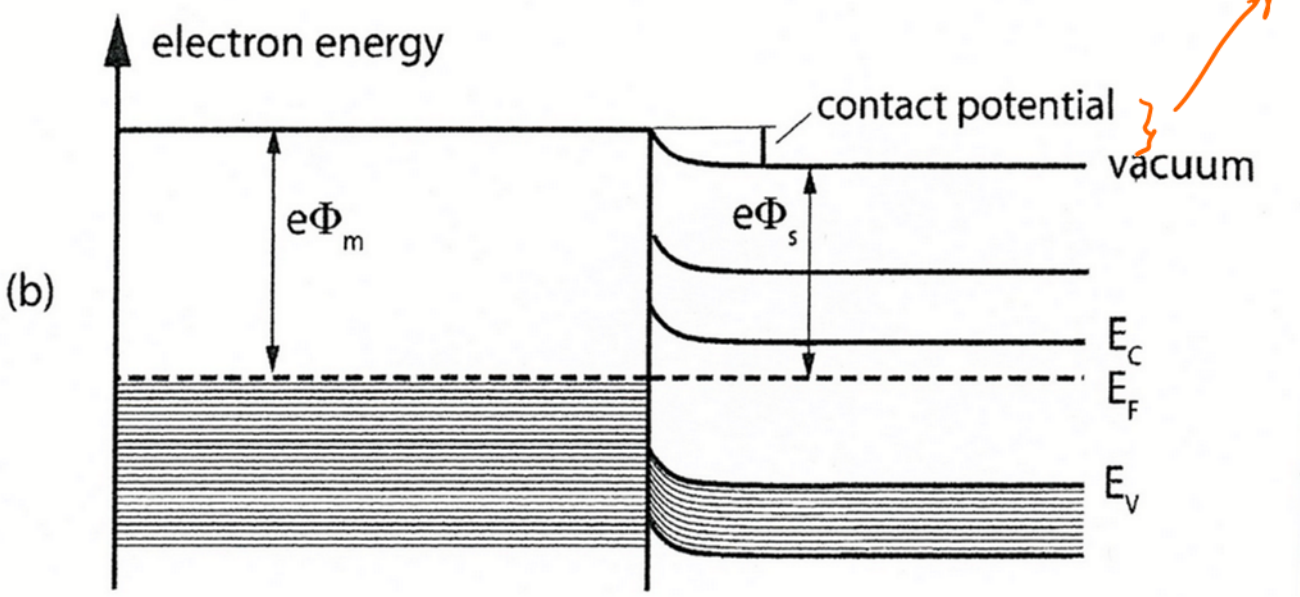
20 000 Ω cm ALLOWS $n_A \sim 2.3 \times 10^{15} / \text{cm}^3$

$$d_{\text{MAX}} = \frac{\epsilon E_{\text{BREAKDOWN}}}{q n_A}$$

20 000 Ω cm \rightarrow 16,000 V/mm \rightarrow 10 mm DEPLETION
10 cm IN G_E



NO CONTACT



TO GET FROM Si INTO METAL ELECTRONS MUST OVERCOME THIS POTENTIAL

CONTACT

ON PREVIOUS PAGE, WORK FUNCTION IS
ENERGY NEEDED TO MOVE ELECTRON FROM
FERMI LEVEL IN SILICON TO POINT OUTSIDE
ON CONTACT

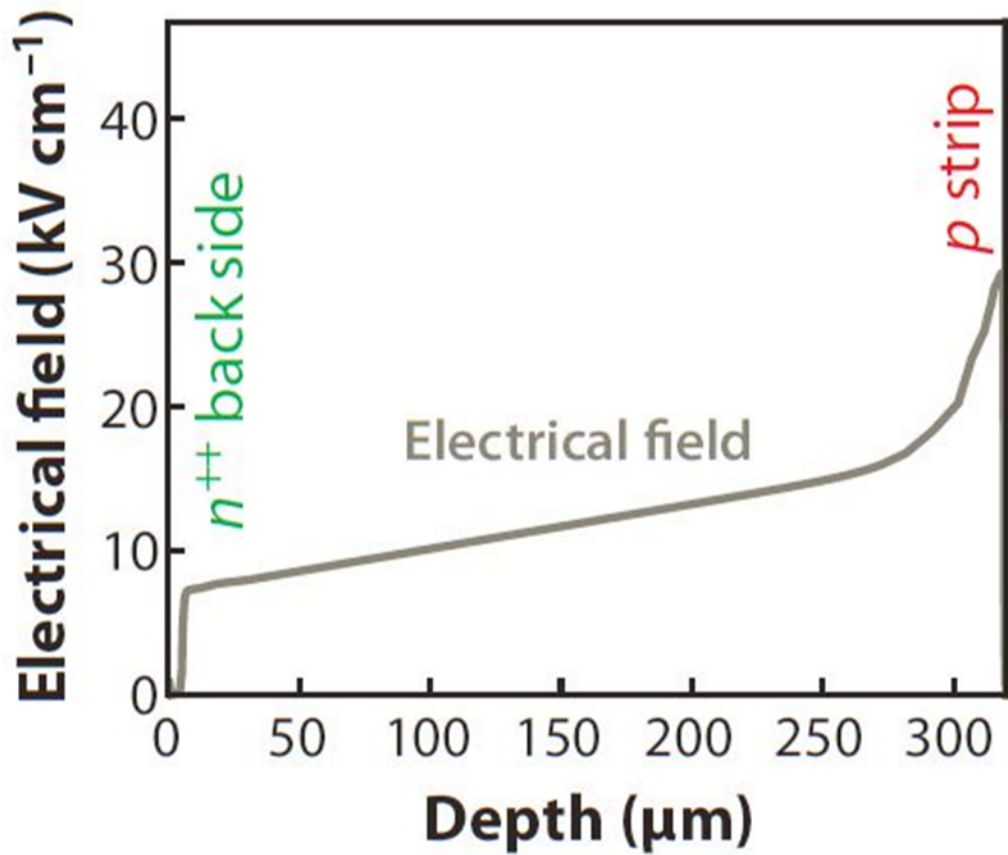
SPACE CHARGE DEPLETION ZONE
IN METAL) IN SILICON

→ HOW TO GET ELECTRON (HOLES) OUT?

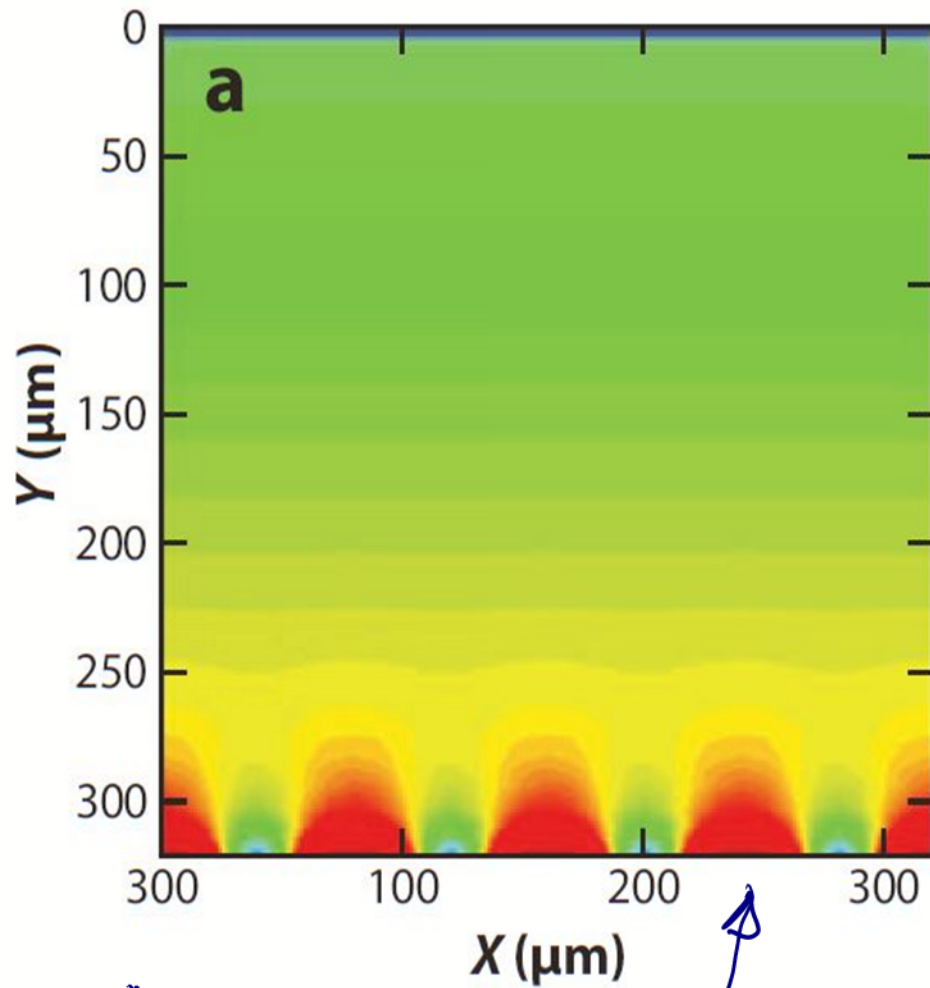
→ VERY HIGH DONOR CONCENTRATION AT INTERFACE

→ d VERY SMALL, CARRIERS TUNNEL THRU

"OHMIC" CONTACT n^+ or p^+ ALLOWS CARRIERS
TO PASS WITH LOW RESISTANCE FROM SILICON
IN TO METAL CONTACT → ELECTRONICS.



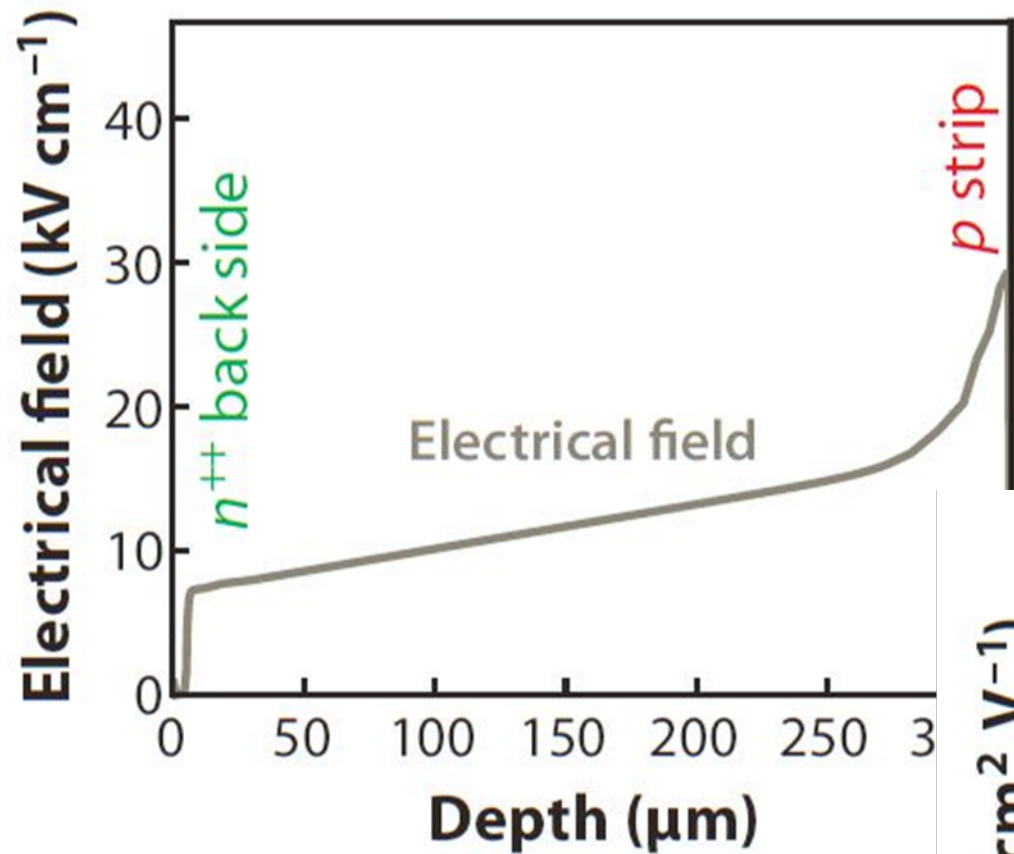
SIMULATION



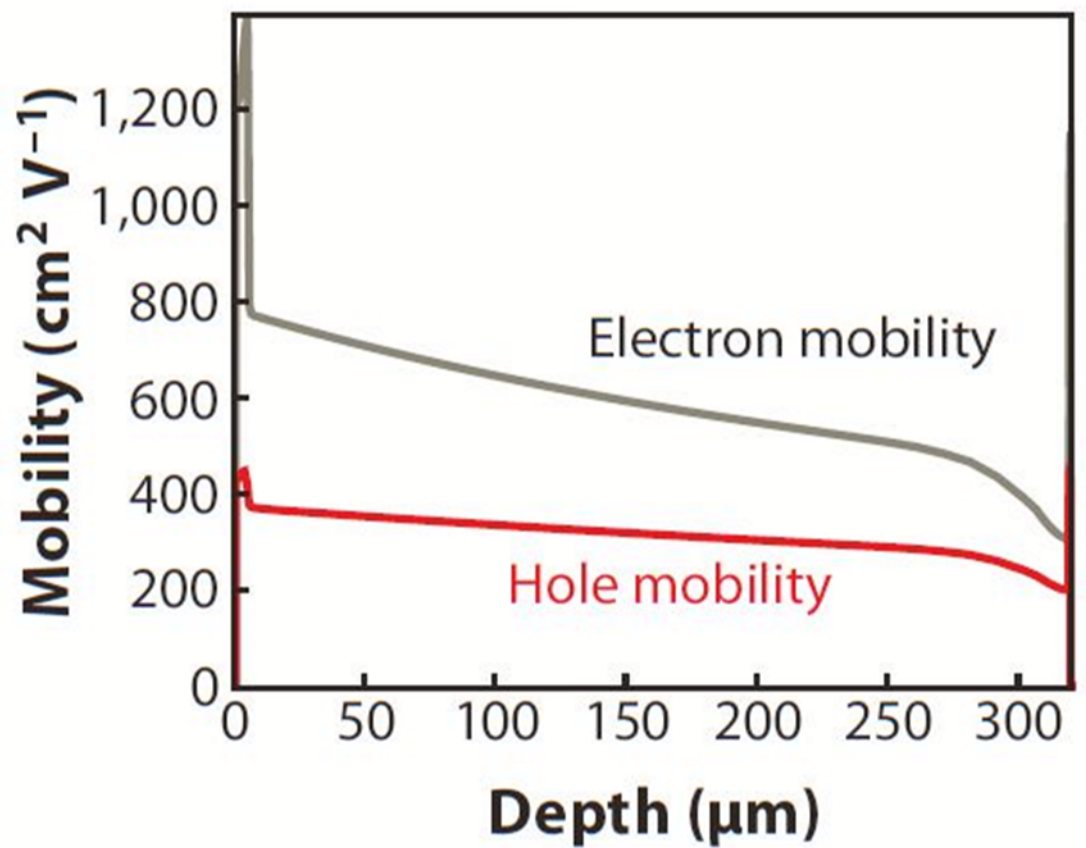
DEPTH

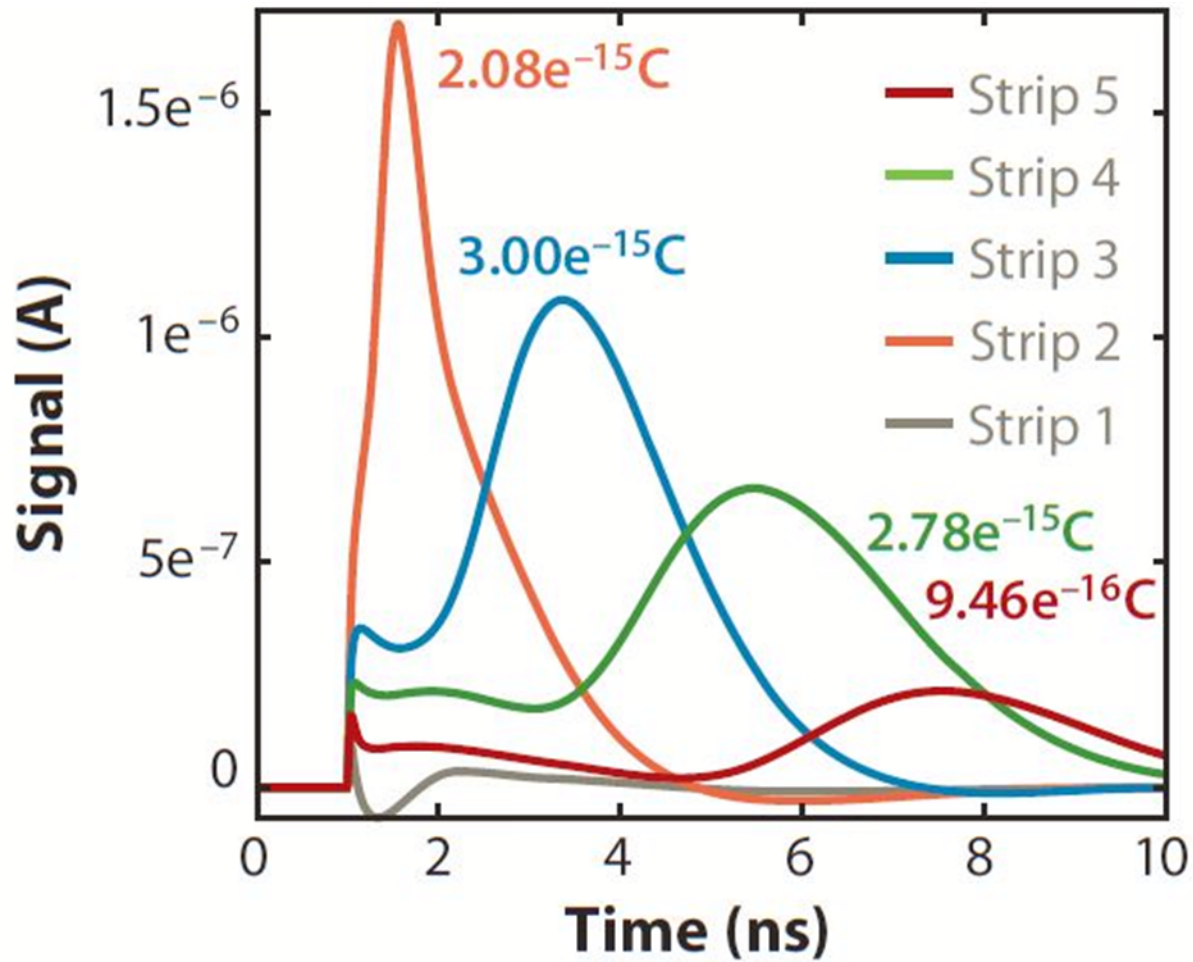


STRIPS



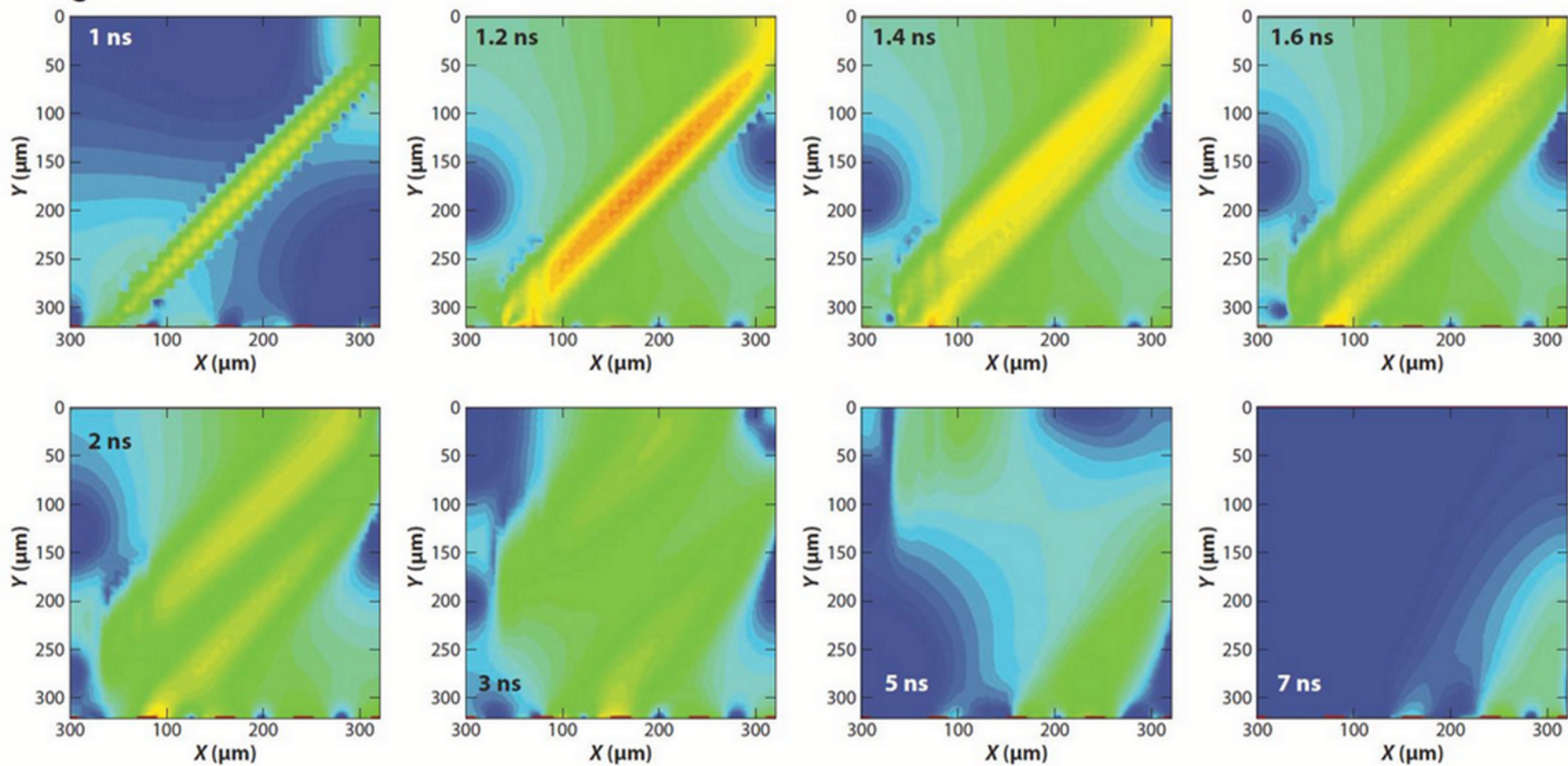
MOBILITY IS FIELD DEPENDENT
→ POSITION DEPENDENT





SIMULATION OF A
TRACK PASSING
THRU SENSOR
AT 45°

e



$$I(t) = \frac{2q\mu}{\tau_D} \cdot e^{-2t/\tau_D} \quad \text{--- } \textcircled{*}$$

Appendix

→ RECAP OF CHARGE MOVING IN ELECTRIC FIELD

energy in field $U = \frac{CV^2}{2} \rightarrow dU = CVdV \quad \textcircled{1}$

But $Q = CV \rightarrow dQ = CdV$

change in energy of field = work done by field on DRIFTING CHARGE

charge-field energy
↓

$$dU = \underbrace{CV}_{Q} \underbrace{dV}_{\frac{dQ}{C}}$$

$$\underline{dU} = Q \frac{dQ}{C} = qF dx = d[q(t)E \langle v_d \rangle dt]$$

charge induced on electrodes →

$$dQ(t) = q(t) \langle v_d \rangle dt \frac{E}{V}$$

use $\frac{EC}{Q} = \frac{E}{V}$

$$\frac{dQ(t)}{dt} = I(t) = q v_d \frac{E}{V}$$

$v = \mu E$

$$= q \mu \frac{E^2}{V}$$

detector is current source
+
capacitor

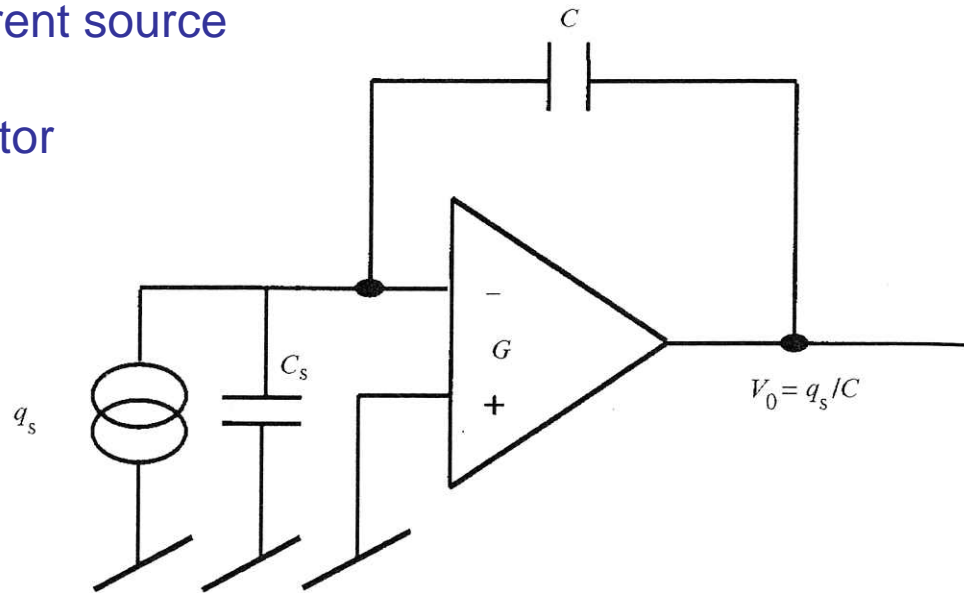


Fig. 9.10. Charge sensitive preamplifier.

$$Q = CV$$

$$I = \frac{dQ}{dt} = C \frac{dV}{dt}$$

$$V_{OUT} \propto q_s$$

Using $Q = CV, I = C \frac{dV}{dt}$

output voltage of OPamp $V_o \propto q/s$

If $G \gg \frac{C_s}{C}$ then ($G \rightarrow \infty$) $V_o = \frac{q/s}{G}$

dissipative elements such as resistors are a source of intrinsic "thermal noise"

the size of the thermal currents is set by the thermal energy kT of the resistor

Noise spectrum is uniform over all frequencies

kT per f

$\frac{\omega}{2\pi} = f$

$f = 2\pi\omega$

1 Hz = 2π rad/s

$f = \frac{\omega}{2\pi}$

$\frac{4kT}{2\pi}$

from Spitzer

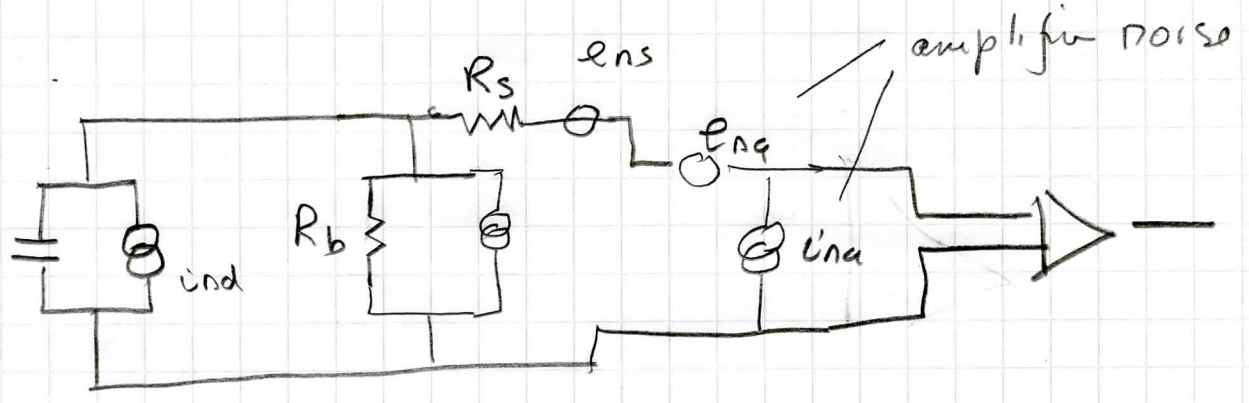
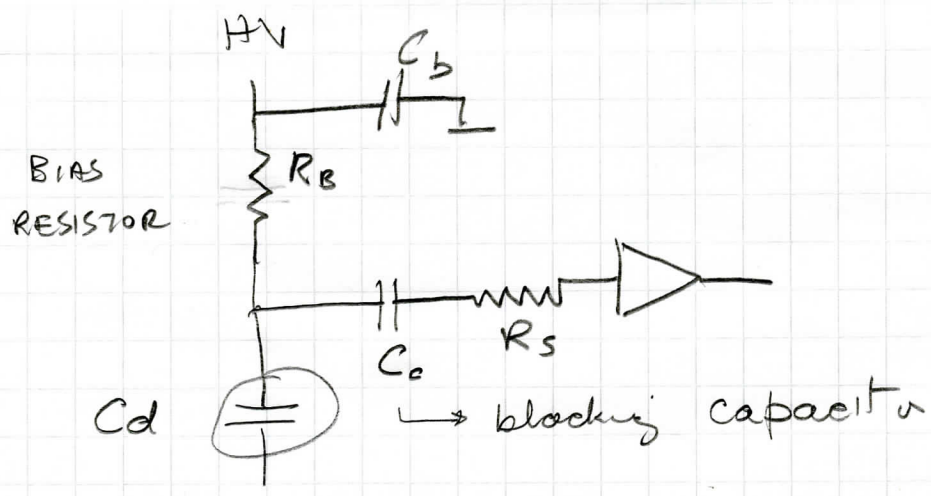
$i_{nd}^2 = 2eI$

$i_{nb}^2 = 4kT/R_B$

$e_{ns}^2 = 4kT R_s$

these are from diagrams over page

cf



- leakage current i_{nd} shot noise

- Resistors SHUNTING INPUT - noise current source.

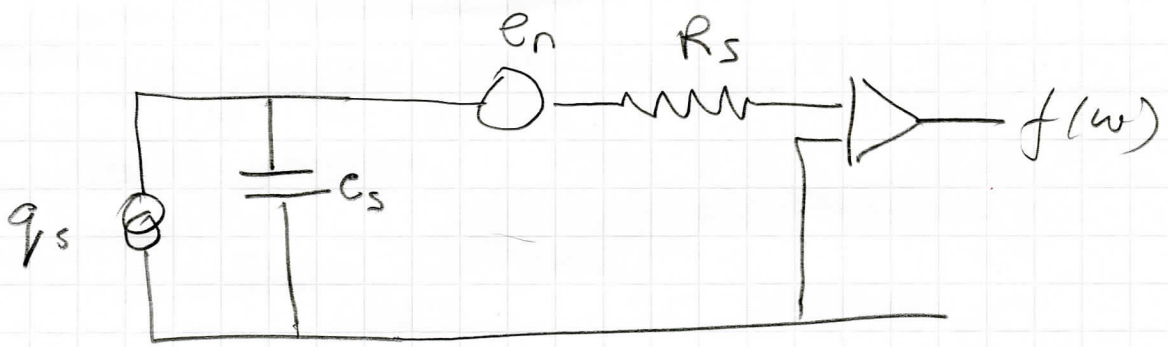
- Resistors in SERIES - noise voltage
 [origin of series / shunt noise

$$i_{nd}^2 = 2e I_d \leftarrow \text{bias current}$$

$$i_{nb}^2 = 4kT/R_B$$

$$e_{ns}^2 = 4kT R_s$$

GREEN



(3)

$$P = I^2 R$$

$$I^2 = \frac{P df}{R} = \frac{4kT}{R} df$$

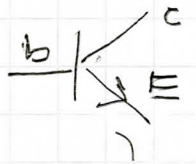
$$= \frac{2kT}{R} \frac{d\omega}{\pi}$$

noise due to standing current is

$$dI_s = q I df = q \frac{d\omega}{\pi}$$

$$dI^2 = q I \frac{d\omega}{\pi}$$

for an input transistor which is
a forward biased



$$R_B = \frac{kT}{q I_E} = \frac{1}{g_m}$$

standing emitter current

3 sources of noise

- 1) thermal noise in source resistor R_S
- 2) shot noise due to standing current in front end emitter I_E
- 3) thermal noise in base resistor R_B

these currents flow into the source capacitance since we assume that $R_S \gg \frac{1}{\omega C_S}$ ← Reactance

Note that $I = C \frac{dv}{dt} = C \omega V$

means that capacitance reactance is

$$V = IR \quad R = \frac{V}{I} = \frac{1}{\omega C}$$

$$X_L = 2\pi f L$$

$$X_C = \frac{1}{2\pi f C}$$

so for the noise voltage we have

$$dV^2 = dI_T^2 Z_C^2 + dI_S^2 Z_C^2 + dI_T^2 R_B^2$$

↑
thermal noise
in source
Resistor

↑
shot noise
in emitter

↑
BASE
RESISTOR
thermal noise

$$g_m = \frac{i_{out}}{v_{in}}$$

$$\frac{1}{R} = \frac{i}{V} \quad V = V_i$$

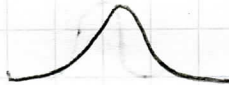
$$\frac{2kT}{R_S(\omega C_S)^2} + \frac{q I_B}{(\omega C_S)^2} + \frac{2kT}{R_B} R_B^2$$

$$= \left[\frac{2kT}{R_S} \frac{1}{(\omega C_S)^2} + \frac{q I_B}{(\omega C_S)^2} + \frac{2kT}{g_m} \right] \frac{d\omega}{\omega}$$

$$\langle V^2 \rangle = \int_0^\infty |f(\omega)|^2 \frac{dV^2}{d\omega} \cdot d\omega$$

now $\int_0^\infty |f(\omega)|^2 \frac{\pi}{4}$

$$\therefore \langle V^2 \rangle = G^2 \left[\underbrace{\left(\frac{kT}{2R_s} + q \frac{I}{4} \right) \frac{\tau}{C_s^2}}_{\text{SHUNT = PARALLEL}} + \underbrace{\frac{kT}{2g_m \tau}}_{\text{SERIES}} \right]$$

noise going into C_s diverges at low frequency
 pure thermal noise diverges at high frequency
 hence shaper 

Optimum filter is when frequency distribution of source = frequency pass of filter = $\frac{1}{\tau}$

$$V = \frac{Q}{C} \quad \text{input } q_s \xrightarrow{\text{amp}} \frac{q_s G}{C_s} \cdot \frac{1}{e} = V$$

frequency distribution of signal

$$V = \frac{q_s}{C_s} e^{-t/\tau} \cdot G$$

at $t = \tau$

$$V = \frac{q_s}{C_s} \frac{G}{e}$$

(6)

$$\langle V^2 \rangle = \left(\frac{q_s}{C_s} \cdot \frac{G}{e} \right)^2$$

write in terms of equivalent noise q
(i.e. ... equivalent to so many electrons)

$$\langle V^2 \rangle = \left(\frac{ENC}{C_s} \frac{G}{e} \right)^2$$

$$ENC = \frac{C_s \cdot e}{G} \sqrt{\langle V^2 \rangle}$$

$$ENC_P = \frac{C_s e}{G} \sqrt{\left(\frac{kT}{2R_s} + \frac{q I_B}{4} \right)} \frac{\sqrt{\tau}}{e_s}$$

$$ENC_P = e \sqrt{\left(\frac{kT}{2R_s} + \frac{q I_B}{4} \right) \tau}$$

$$ENC_S = e C_s \sqrt{\frac{kT}{2g_m}} \frac{1}{G}$$

For low noise

τ small

R_S large

I_B small

} minimize \parallel^l

C_S small

R_B small

} minimize serial

high speed means
goes as $\frac{1}{\sqrt{\tau}}$

τ small, but series noise

plot of noise

\parallel^l part is independent of C_S

series part - increases with C_S

so far have neglected transistor as source of noise

e_n in equivalent circuit

$$ENC_S = \frac{e_n C_S}{\sqrt{\tau}}$$

Equivalent Circuit of Detector + Amplifier

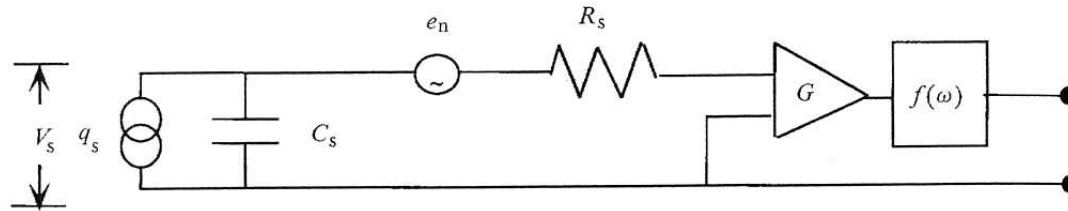


Fig. 9.11. Amplifier and bandwidth limiting filter, $f(\omega)$ with source capacitance, C_s , source resistance, R_s , source charge, q_s , and input noise voltage, e_n .

- resistors – source of thermal noise – thermal energy kT
 - noise is spread uniformly over all frequencies

$$I_T \rightarrow P = VI_T = I_T^2 R$$

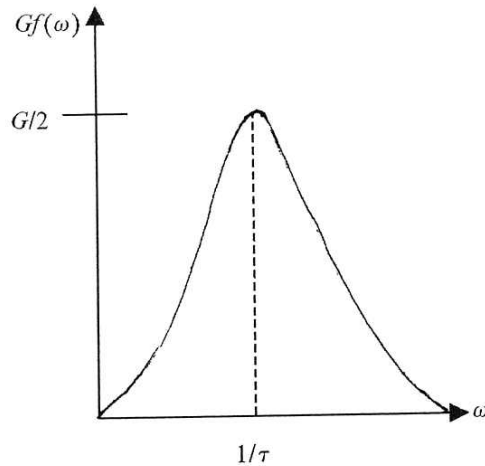
$$dI_T^2 = \frac{2kT}{R} \left(\frac{d\omega}{\pi} \right) \leftarrow \text{thermal noise}$$

- current made of – discrete carriers

$$dI_s^2 = qI \left(\frac{d\omega}{\pi} \right) \leftarrow \text{shot noise}$$

- need to limit bandwidth or infinite noise

• frequency filter



Plot of the transfer function $Gf(\omega)$ which $\rightarrow 0$ as $\omega \rightarrow 0$ and as $\omega \rightarrow \infty$ and $= 1/\tau$.

$$f(\omega) = G \left[\frac{\omega\tau}{1 + (\omega\tau)^2} \right]$$

$$\int_0^{\infty} f^2(\omega) \cdot d\omega = \frac{\pi}{4}$$

$$\sqrt{qI} = 0.4 \text{ nA} \sqrt{I \text{ Hz}}$$

$$\sqrt{\frac{2kT}{R}} = 0.9 \text{ nA} \sqrt{\frac{\text{Hz}}{R}}$$

• for a frequency range of 100 MHz and 1mA

• 126 nA – pretty close to signal

$$dI_s^2 = q I \frac{d\omega}{\pi}$$

Three sources of noise

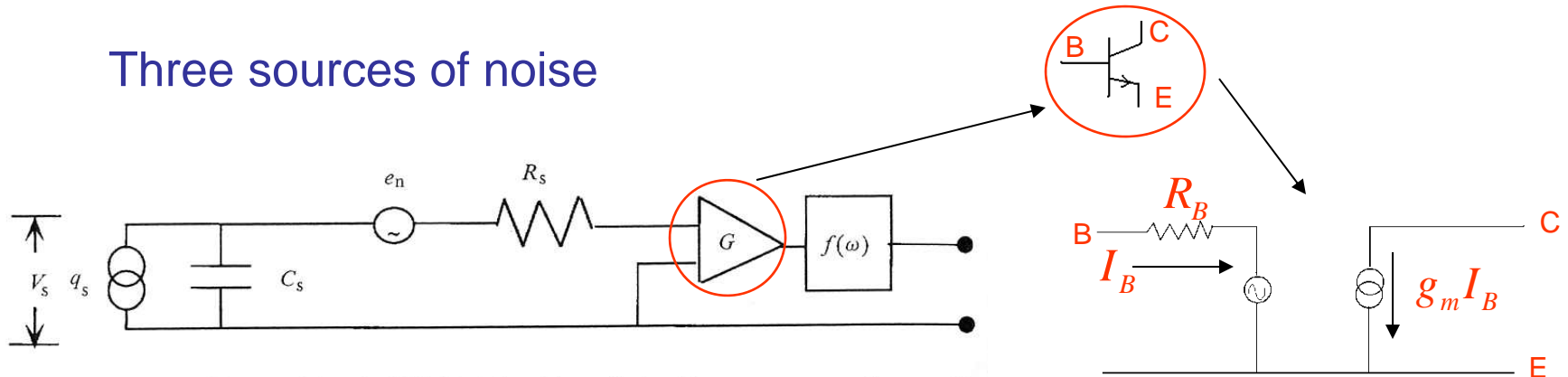


Fig. 9.11. Amplifier and bandwidth limiting filter, $f(\omega)$ with source capacitance, C_s , source resistance, R_s , source charge, q_s , and input noise voltage, e_n .

After shaping (filter) Equivalent Noise Charge

- Thermal - R_s
 - Shot - I_E
 - Thermal - R_B
- SEE NEXT SLIDE*

$$ENC_P = 2.72 \sqrt{\tau \left(\frac{kT}{2R_s} + q \frac{I_B}{4} \right)}$$

$$ENC_S = 2.72 C_s \sqrt{\frac{kT}{2g_m \tau}}$$

$$d\bar{V}^2 = d\bar{I}_T^2 Z_{C_s}^2 + d\bar{I}_S^2 Z_{C_s}^2 + d\bar{I}_T^2 R_B^2$$

$$= \left[\frac{2kT}{R_s (\omega C_s)^2} + \frac{qI_B}{(\omega C_s)^2} + \frac{2kT}{g_m} \right] \left(\frac{d\omega}{\pi} \right)$$

$\frac{1}{\omega^2}$ constant

- Low temp
 - R_s large
 - I_B small
 - C_s small
 - R_B small
- } parallel noise
 } series noise

THREE SOURCES OF NOISE

- THERMAL NOISE IN SOURCE RESISTOR R_S
- SHOT NOISE DUE TO STANDING EMITTER CURRENT IN AMPLIFIER TRANSISTOR
- THERMAL NOISE IN BASE RESISTOR

THE NOISE CURRENTS DEVELOP A VOLTAGE ACROSS THE SOURCE CAPACITANCE.

SO THEY LOOK JUST LIKE THE SIGNAL ACROSS THE SOURCE CAPACITANCE

FOR A CAPACITOR $Z_C = 1/j\omega C$

FOR A RESISTOR $Z_R = R$

SO YOU MIGHT EXPECT VOLTAGE ACROSS R & C TO BE OUT OF PHASE. BUT THEY ARE STATISTICALLY INDEPENDENT \rightarrow ADD IN QUADRATURE

THERMAL NOISE
IN CAP

SHOT NOISE
IN CAP

THERMAL
NOISE IN BASE
RESISTOR

$$d\bar{v}^2 = d\bar{I}_T^2 Z_{C_s}^2 + d\bar{I}_S^2 Z_{C_s}^2 + d\bar{I}_T^2 R_B^2$$

$\frac{2kT}{R_s}$ $\frac{1}{(\omega C_s)^2}$ $q I_B$ $\frac{2kT}{R_B}$ $\frac{1}{g_m}$

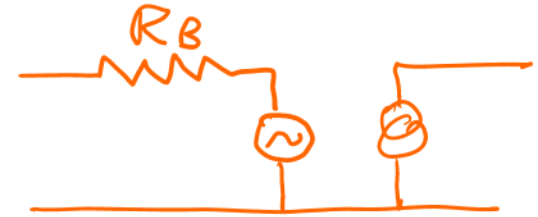
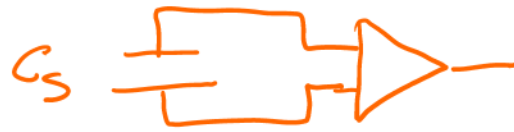
$$d\bar{v}^2 = \left[\frac{2kT}{R_s (\omega C_s)^2} + \frac{q I_B}{(\omega C_s)^2} + \frac{2kT}{g_m} \right] \frac{d\omega}{\omega}$$

RMS VOLTAGE

$$\langle V^2 \rangle = \int_0^\infty |f(\omega)|^2 \frac{d\bar{v}^2}{d\omega} d\omega$$

$$= G^2 \left[\left(\frac{kT}{2R_s} + \frac{q I_B}{4} \right) \frac{\tau}{C_s^2} + \frac{kT}{2g_m \tau} \right]$$

$$\langle V^2 \rangle = G^2 \left[\underbrace{\left(\frac{kT}{2R_s} + g_m \frac{I}{4} \right) \frac{\tau}{C_s^2}}_{\text{"SHUNT = || el"}} + \underbrace{\frac{kT}{2g_m \tau}}_{\text{"SERIES"}} \right]$$



$$\tau \sim \frac{1}{\omega}$$

DIVERGES
AS $\omega \rightarrow 0$

DIVERGES AT
LARGE ω

THIS IS WHY WE NEED FILTER
FREQUENCY RESPONSE = FREQUENCY OF SIGNAL

$$V = q_s / C$$

FREQUENCY DISTRIBUTION OF SIGNAL

$$q_s e^{-t/\tau} \cdot G$$

FILTER
↑
-t/τ

IF PEAK SIGNAL = PEAK FILTER

$$V = \frac{q_s}{C_s} e^{-t/\tau} \cdot G$$

$$\tau \sim t$$

$$V = \frac{q_s}{C_s} \cdot \frac{G}{e}$$

NOT ELECTRIC
CHARGE

$$\langle V^2 \rangle = \left(\frac{q_s}{C_s} \cdot \frac{G}{e} \right)^2$$

WRITE IN TERMS OF EQUIVALENT NOISE CHARGE

$$\langle V^2 \rangle = \left(\frac{ENC}{C_s} \cdot \frac{G}{e} \right)^2 \Rightarrow ENC = \frac{C_s \cdot e}{G} \cdot \sqrt{\langle V^2 \rangle}$$

FOR A SIGNAL CHARGE q_s , IF THE FILTER MATCHES THE FREQUENCY DISTRIBUTION OF THE SOURCE

$$q_s \rightarrow \frac{q_s G}{C_s} / e^{2.72 \dots} = V$$

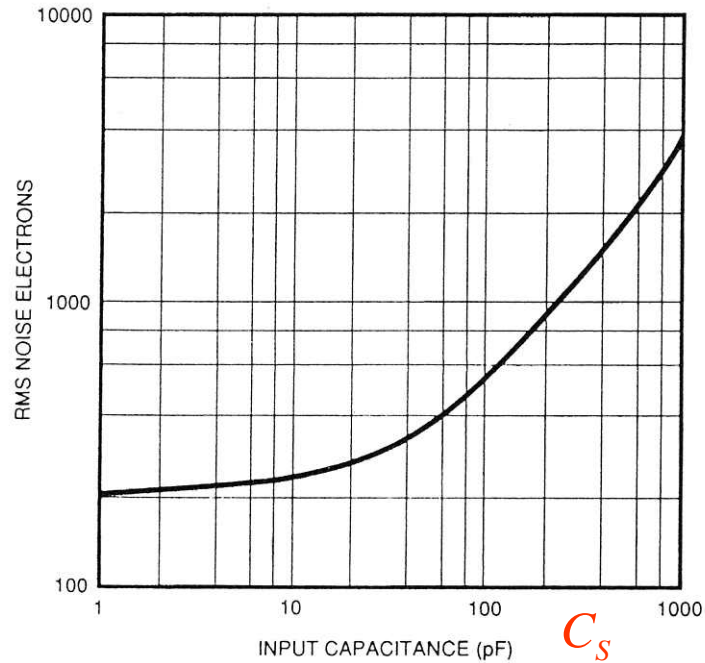
CHARGE ENC $\rightarrow \left(\text{ENC} \cdot \frac{G}{C_s e} \right)^2 \equiv \langle V^2 \rangle$

↑
NOISE CHARGE FROM ALL SOURCES

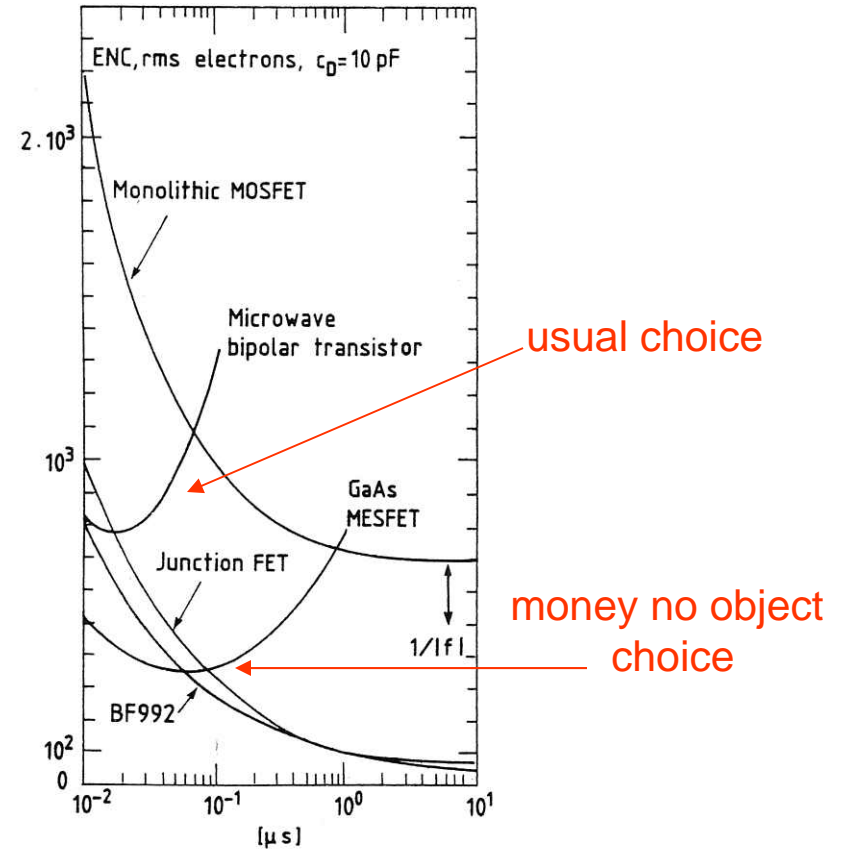
$$\text{ENC}_P = (G_s e / G) \sqrt{\langle V^2 \rangle_P} \equiv e \sqrt{\tau \left(\frac{kT}{2R_s} + \frac{q I_B}{4} \right)}$$

$$\text{ENC}_S = (C_s e / G) \sqrt{\langle V^2 \rangle_S} \equiv e C_s \sqrt{\frac{kT}{2g_m} \frac{1}{\tau}}$$

$P \Rightarrow \parallel^{\text{th}}$ RESISTOR ; $S \Rightarrow$ SERIES RESISTOR



- minimize detector cap – minimize noise
- long strips? – cheap – too noisy

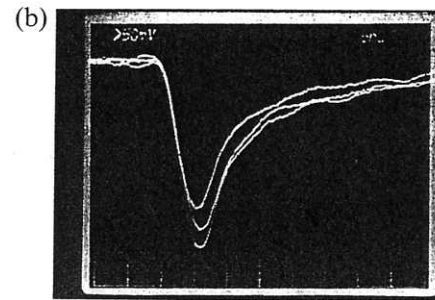
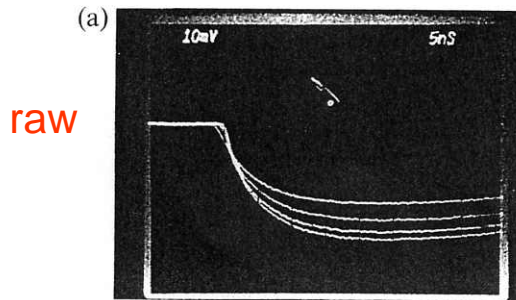


- transistor noise

$$\left. \begin{array}{l} C_s = 25 \text{ pF} \\ \tau = 25 \text{ ns} \end{array} \right\} \sim 1000 \text{ electrons}$$

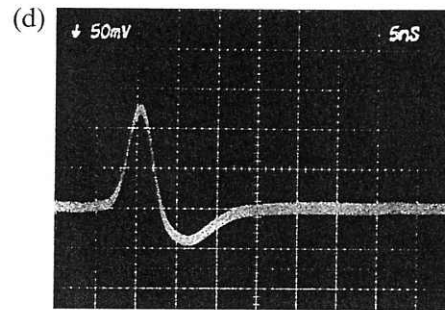
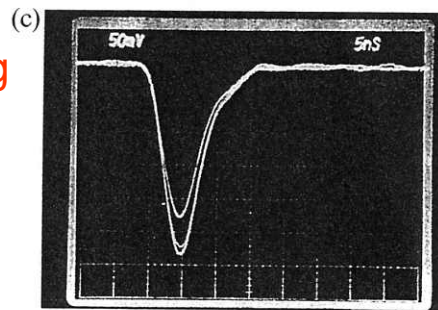
cf signal ~ 31000 electrons

Total Noise



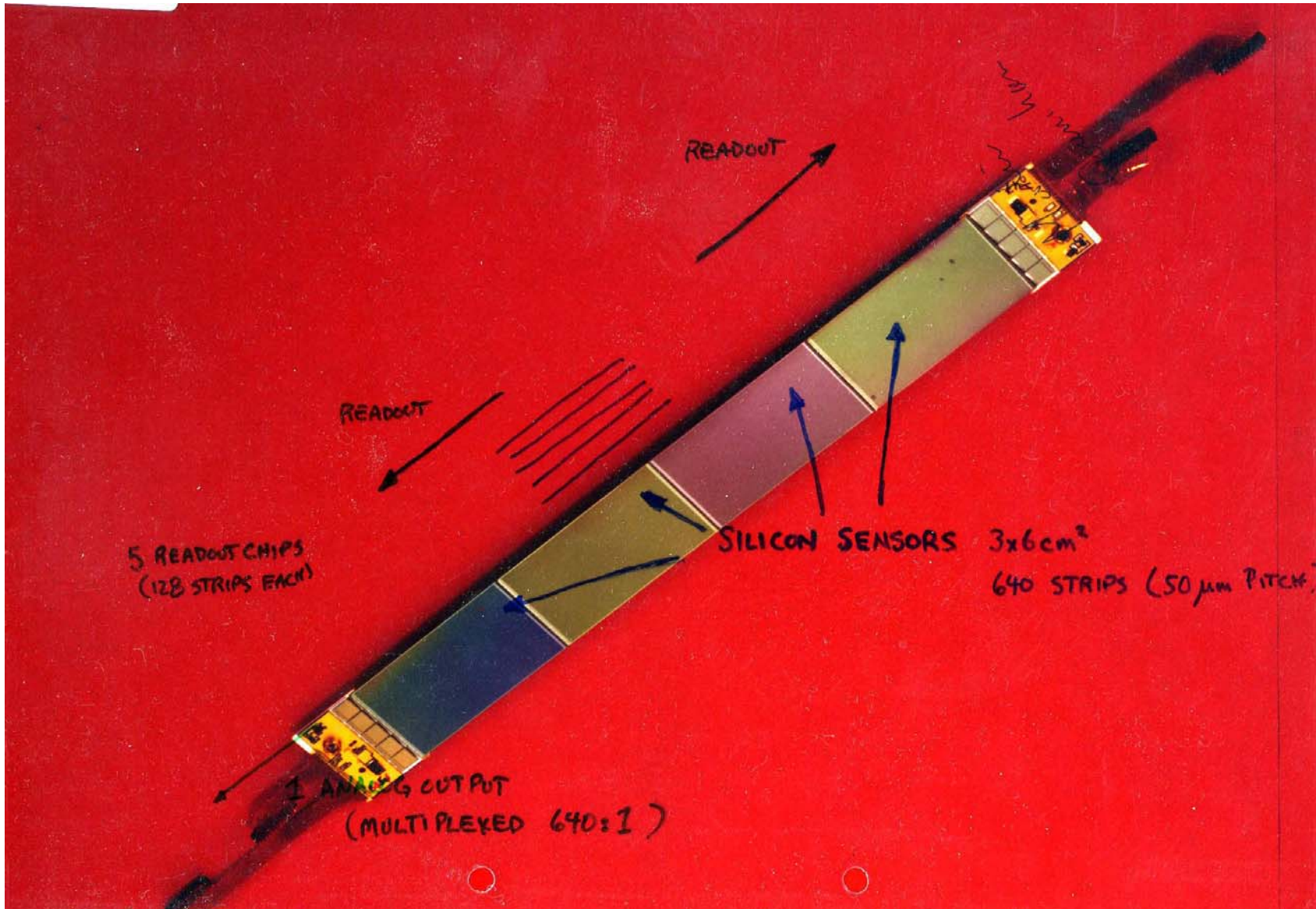
cancel tail

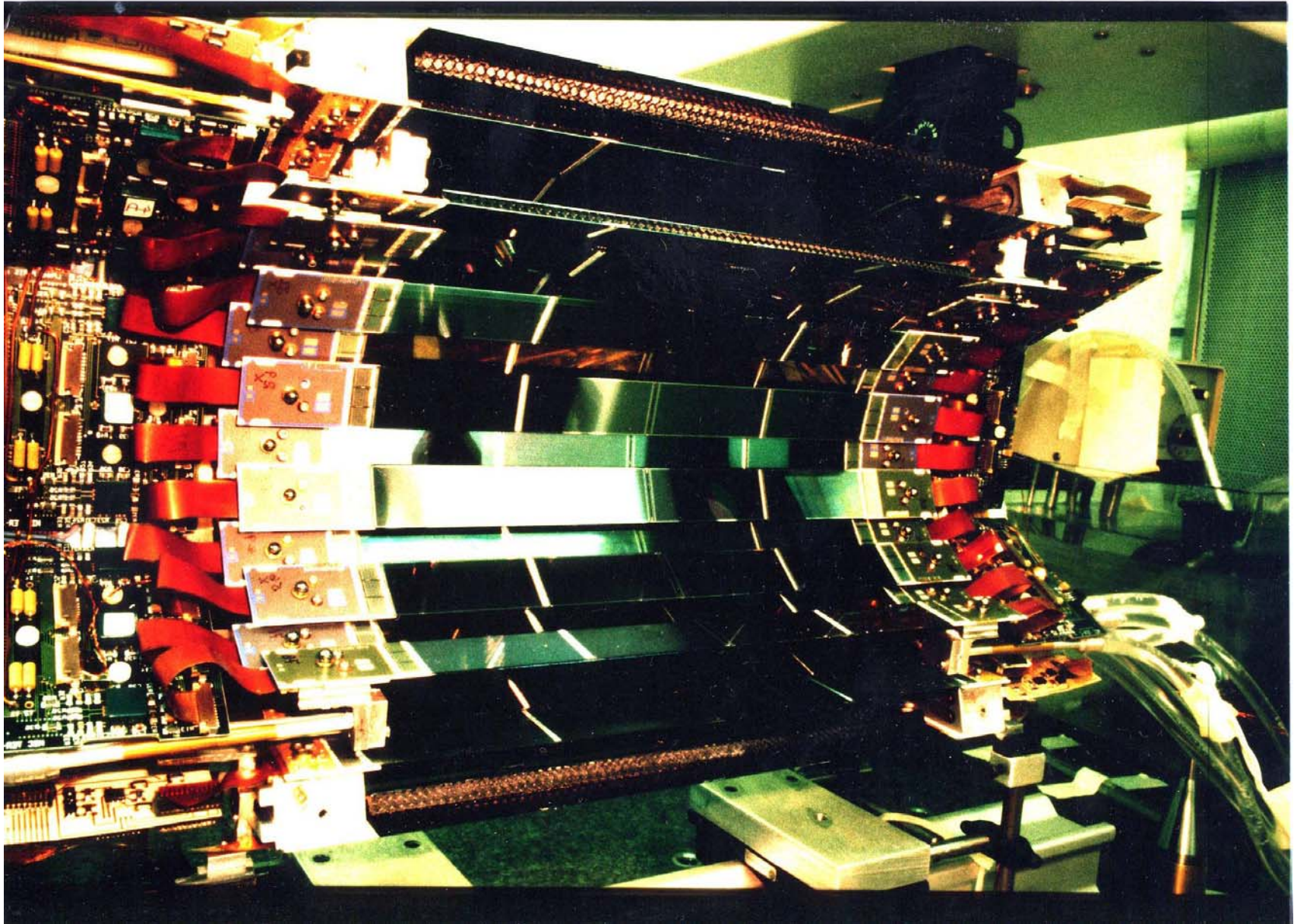
pole-zero shaping



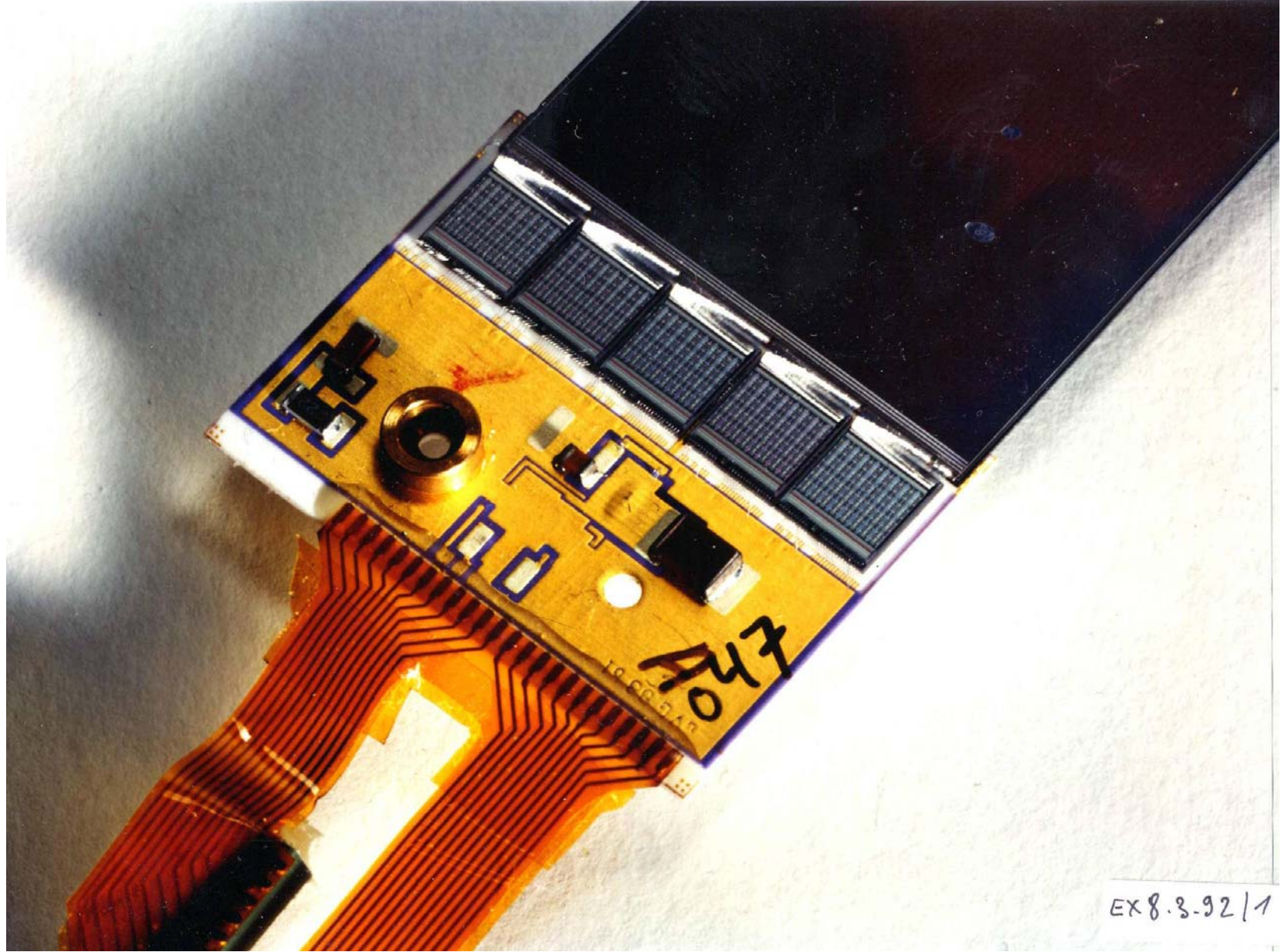
impulse response
- noise

series noise	$q_s \sim 51 \text{ fC}$ $g_m \sim 25 \Omega^{-1}$ $C_s \sim 30 \text{ pF}$ $\tau \sim 10 \text{ ns}$	$\left. \begin{array}{l} \text{---} \\ \text{---} \end{array} \right\} 4 \times 10^{-2}$ $\left. \begin{array}{l} 1125 \text{ electrons} \\ 1152 \end{array} \right\}$	add in quadrature $\frac{\text{Signal}}{\text{Noise}} \sim 23$
parallel noise	$R_s \sim 1 \text{ M}\Omega$ $I_B \sim 1 \text{ mA}$		





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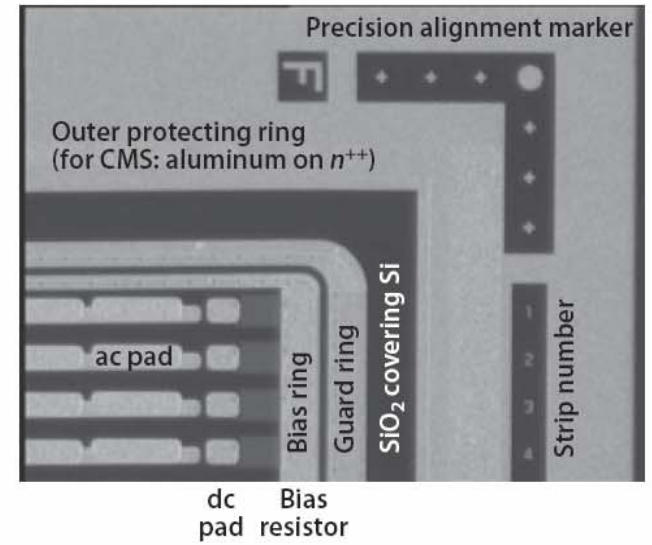
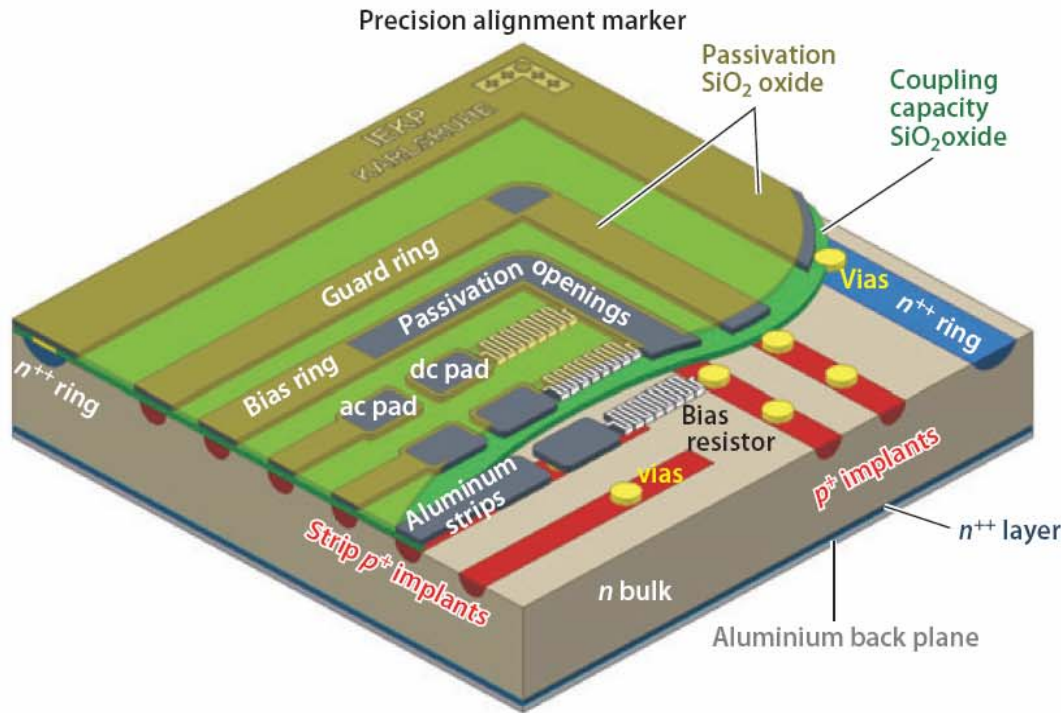
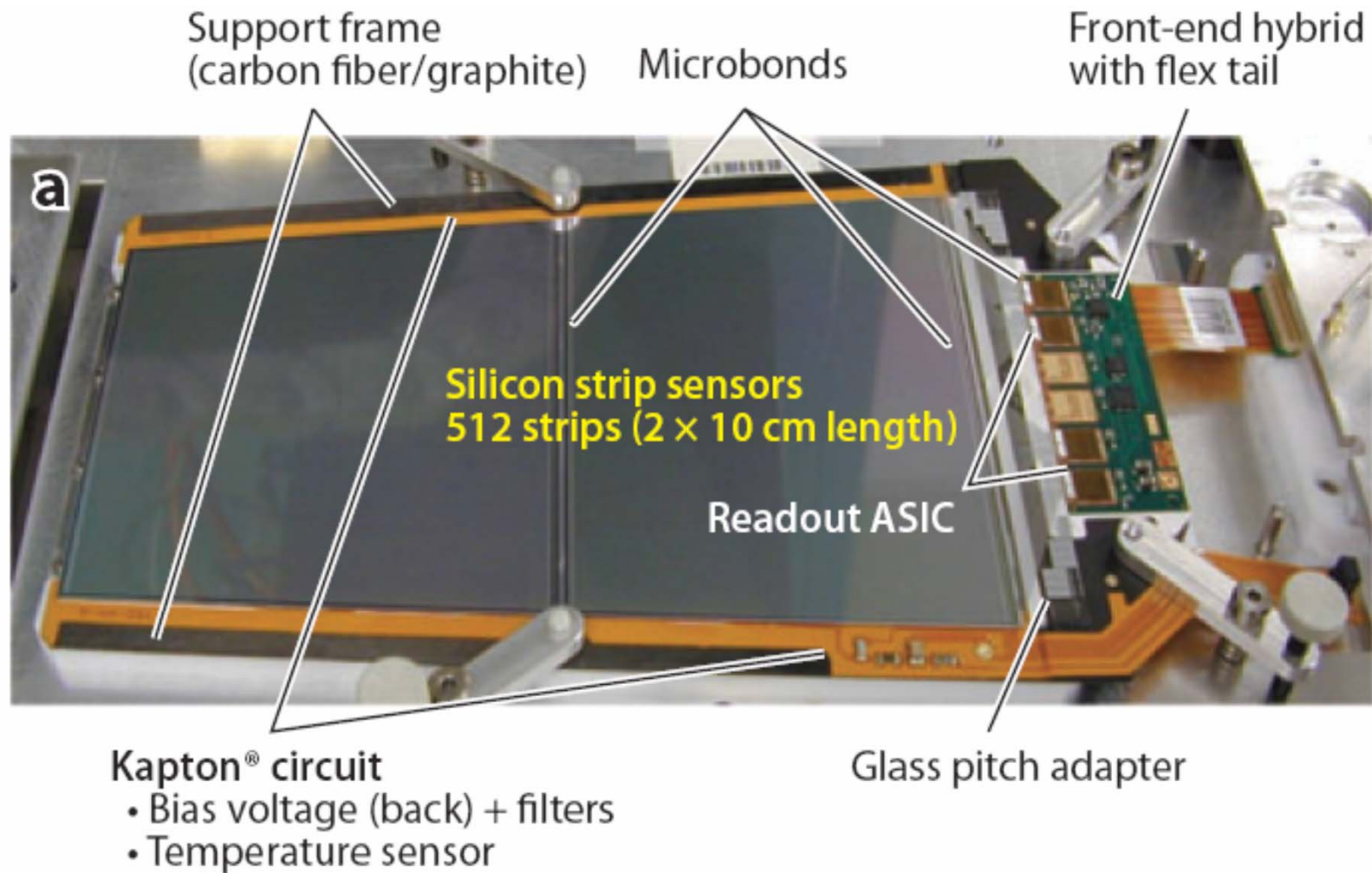
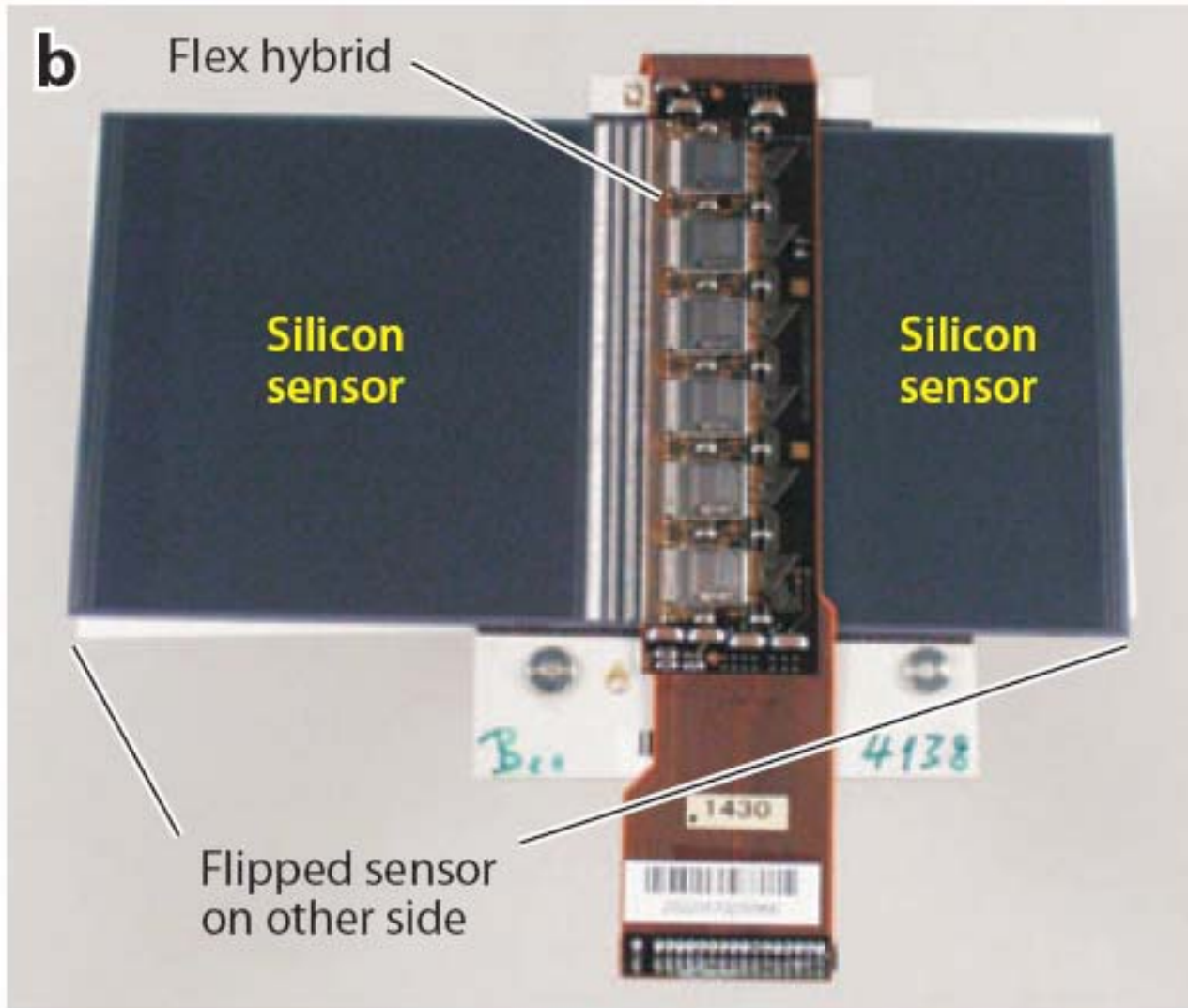
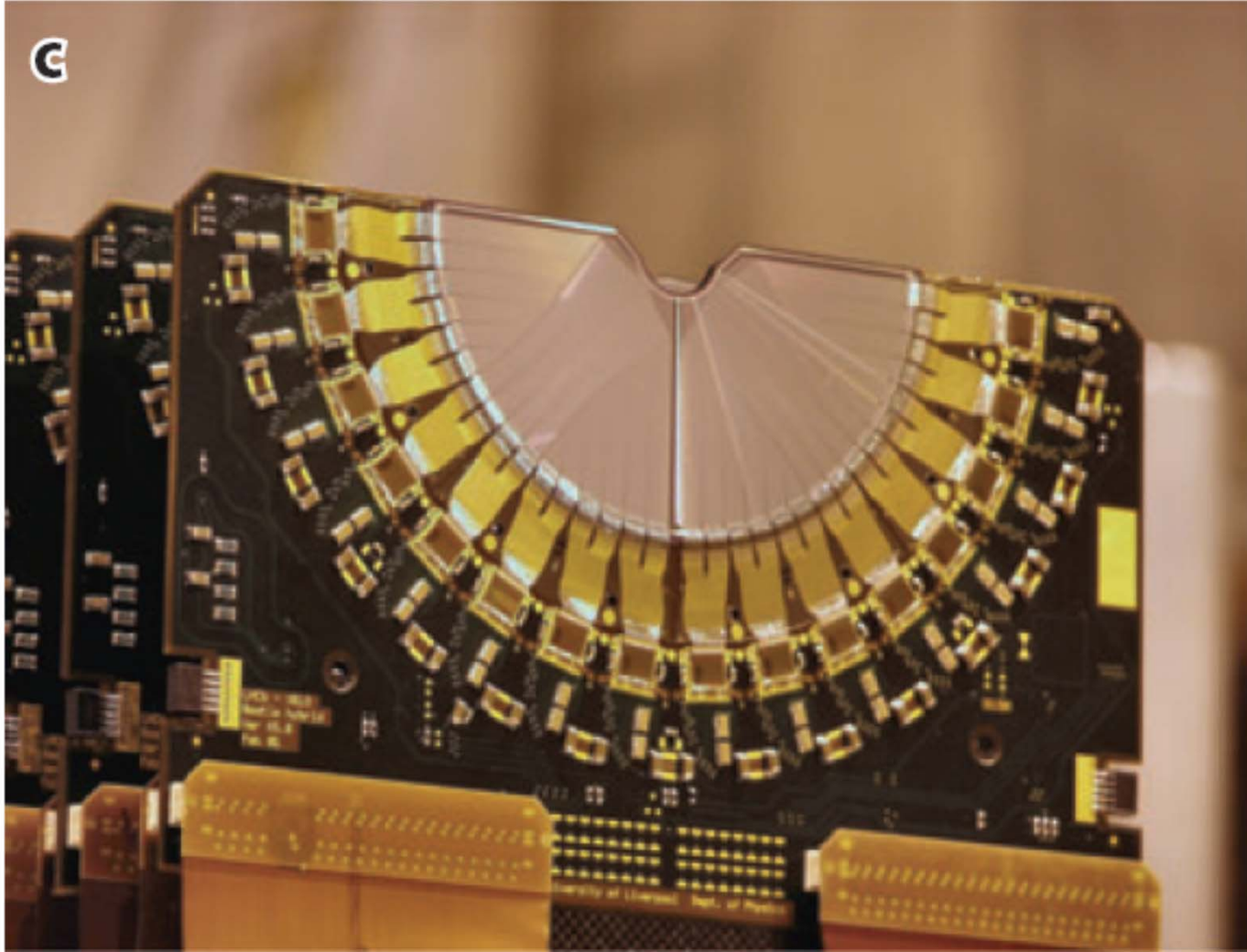


Figure 2

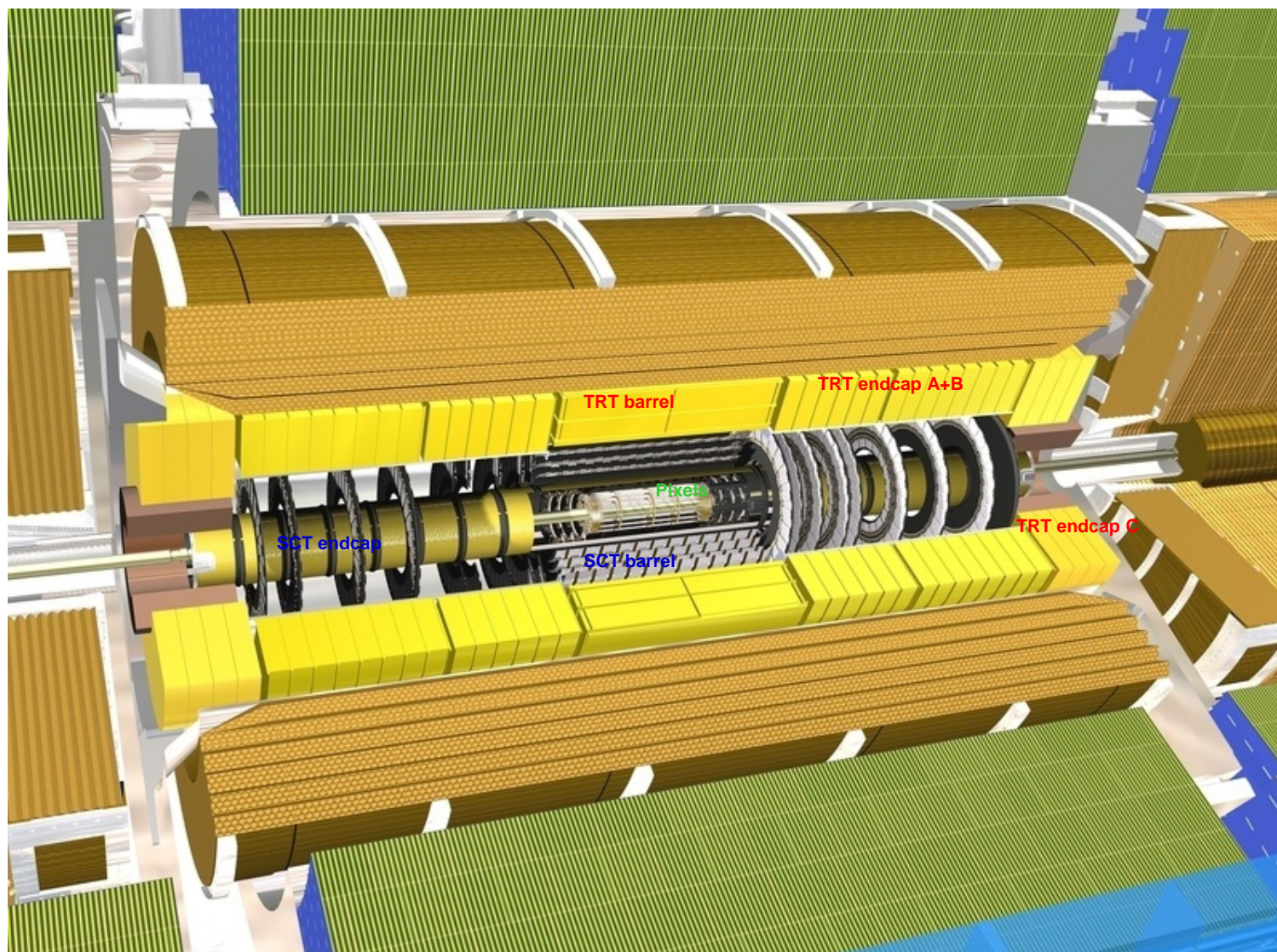
(a) Three-dimensional schematic of a single-sided, ac-coupled, polysilicon resistor-biased sensor showing the baseline of the CMS sensor at the LHC. During operation, the bias ring is connected to the GND (ground) potential, which is then distributed via the polysilicon bias resistors to the p^+ implant strips. The aluminum back plane is set to positive high voltage, depleting the full n -bulk volume of free-charge carriers by forming a pn -junction p^+ strip to n bulk. The long strips and thin decoupling oxide allow high coupling capacitances to be implanted directly into the sensor. The guard ring shapes the field at the borders. The n^{++} ring defines the active volume and prevents high field in the edge regions. (b) View of an actual sensor surface with a strip pitch of $80\ \mu\text{m}$.







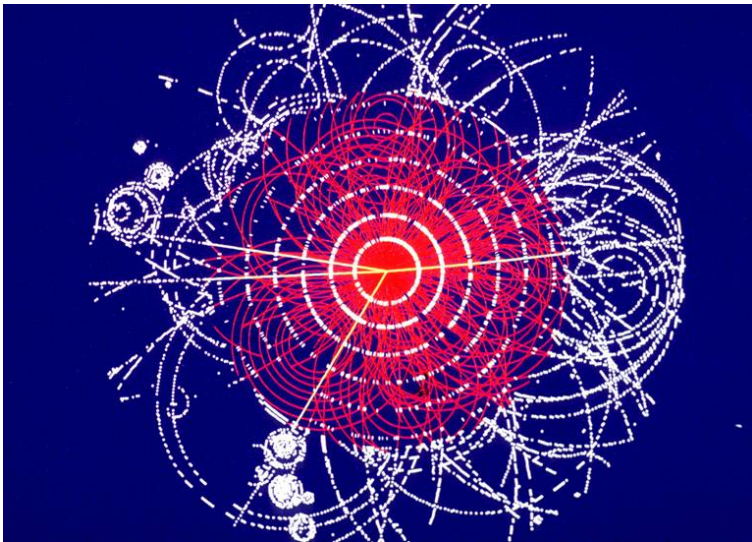
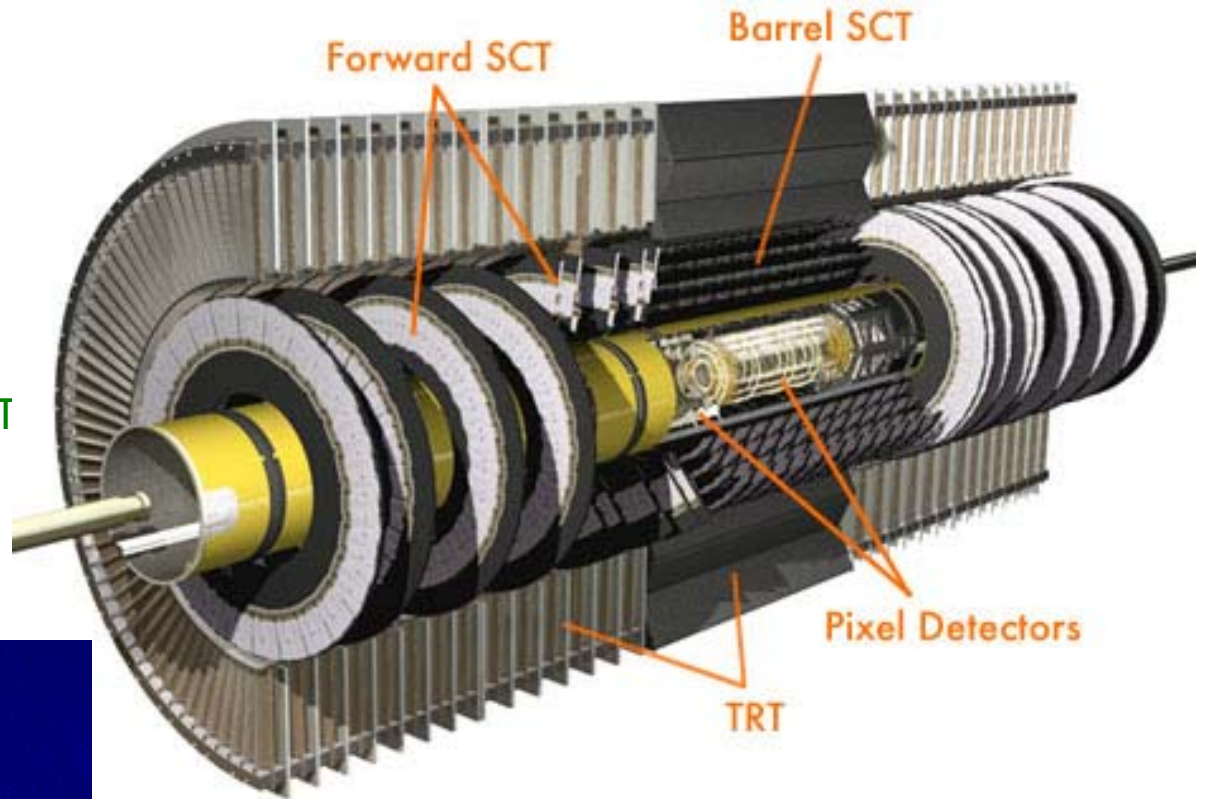
The ATLAS Inner Detector

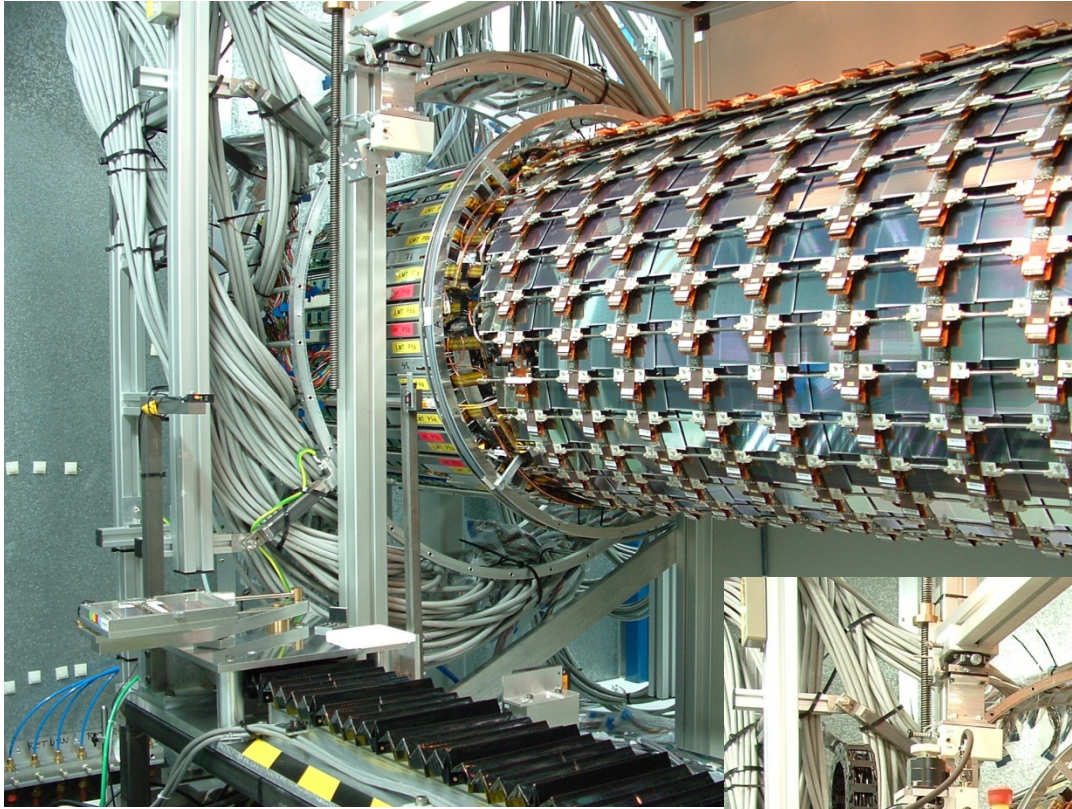


Inner Detector (ID)

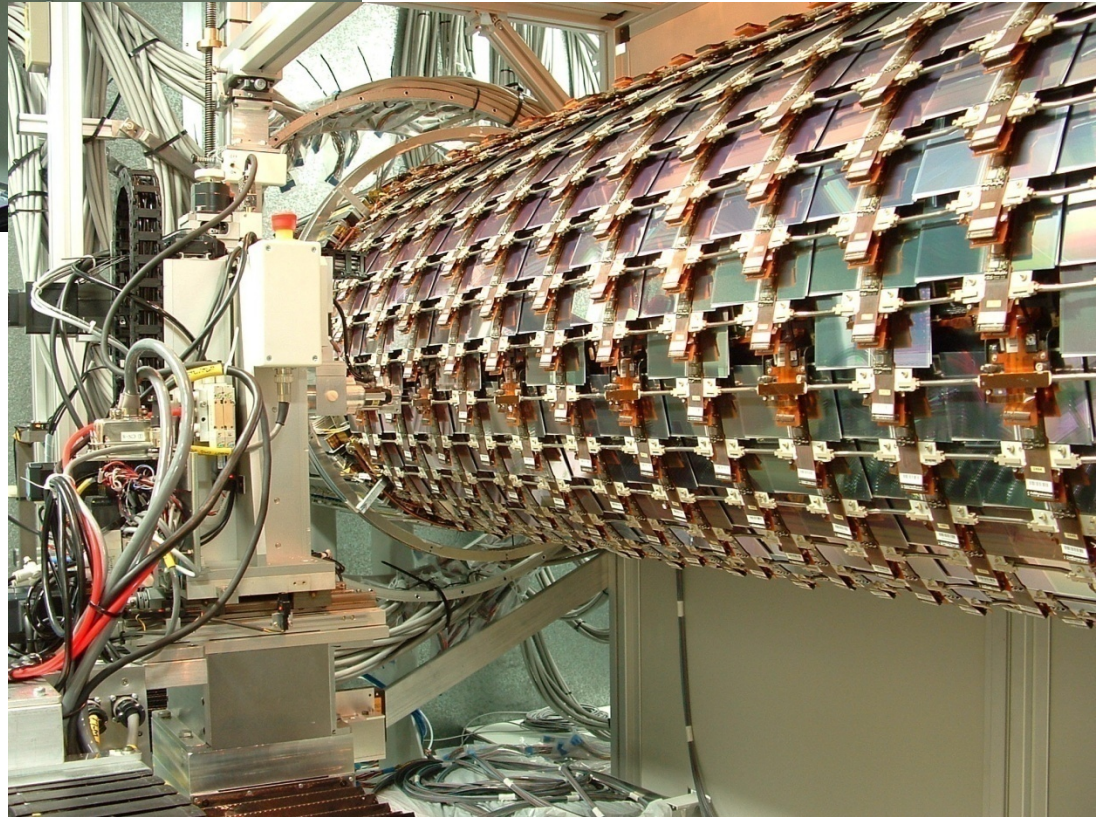
The Inner Detector (ID) comprises four sub-systems:

- Pixels ($0.8 \cdot 10^8$ channels)
- Silicon Tracker (SCT) ($6 \cdot 10^6$ channels)
- Transition Radiation Tracker (TRT) ($4 \cdot 10^5$ channels)

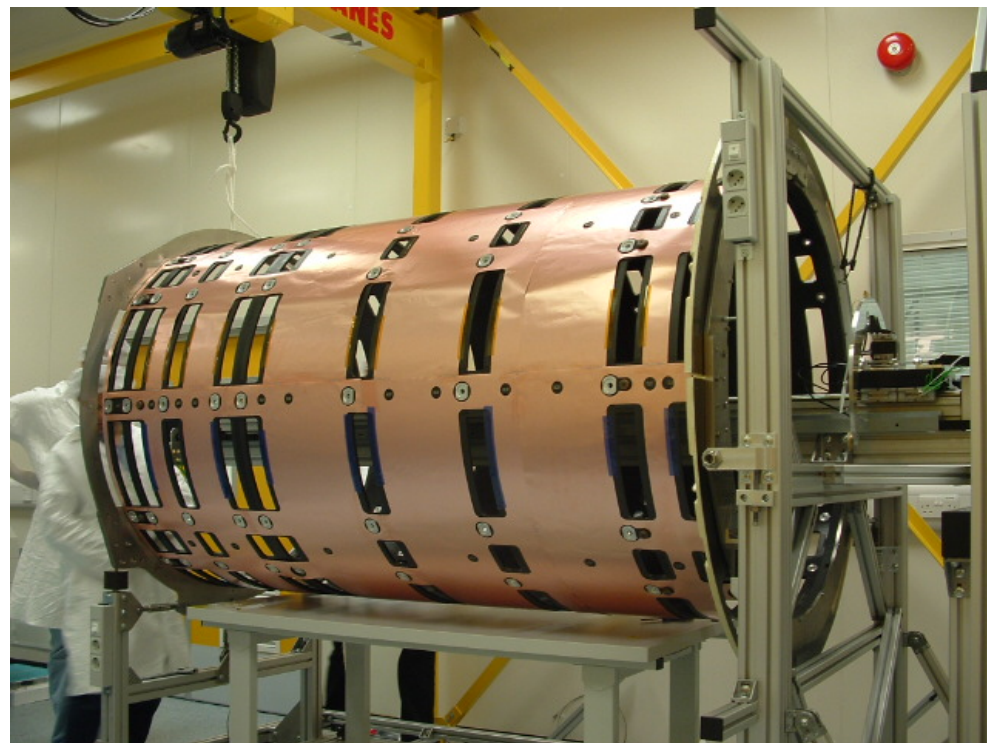
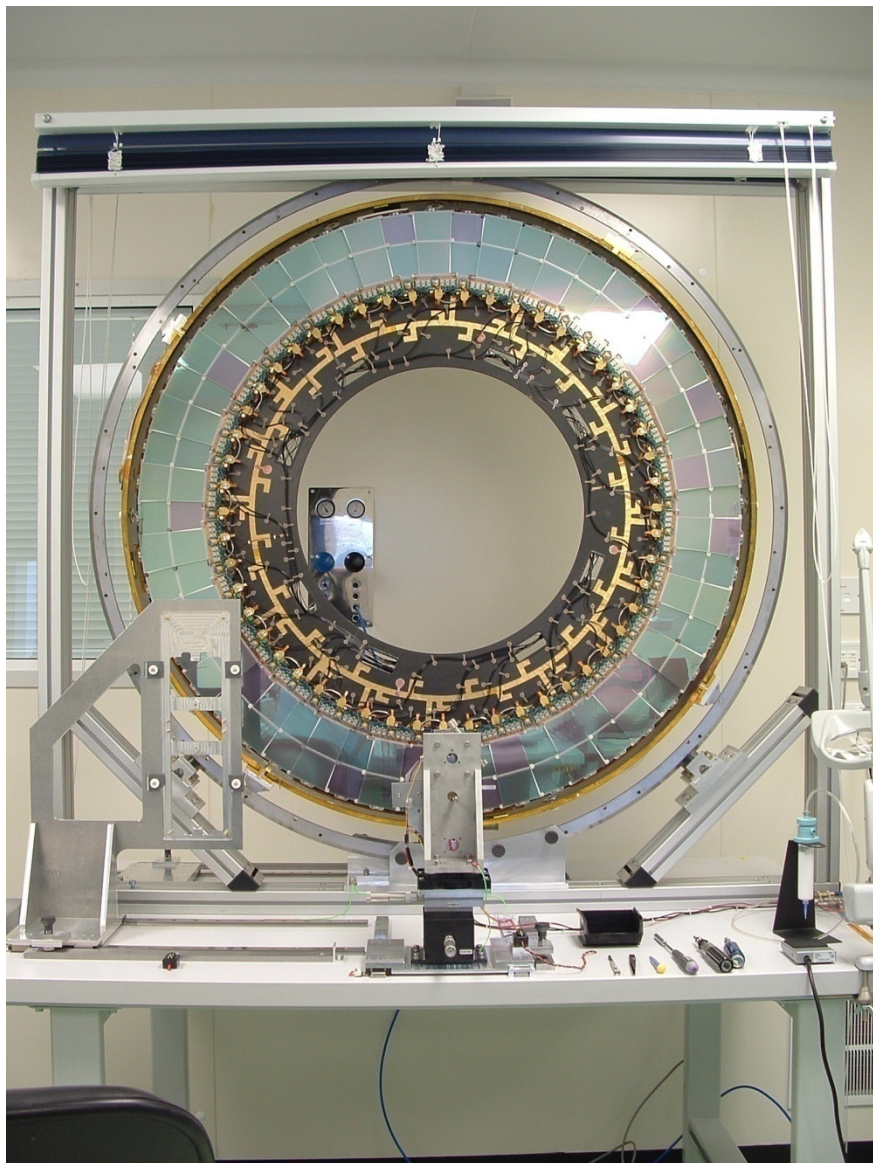


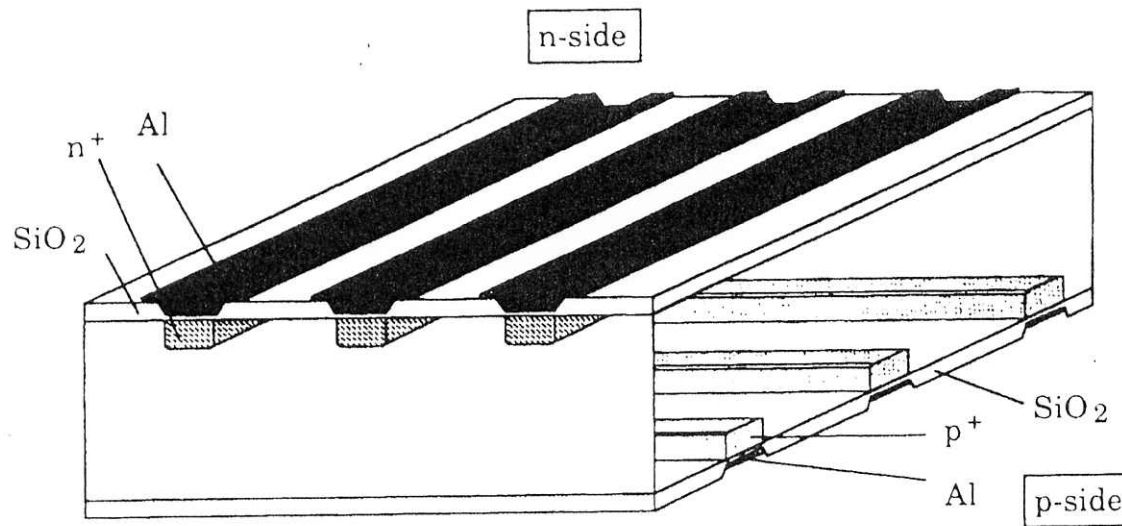


SCT barrel



SCT EndCap



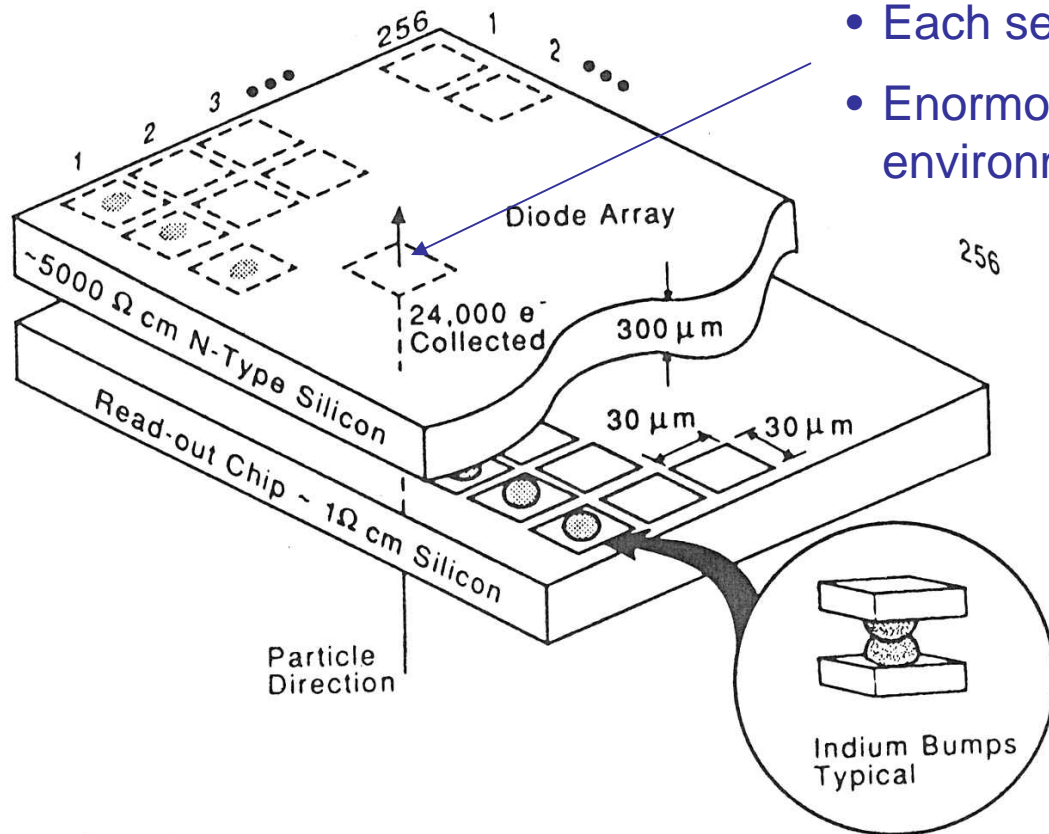


Double-sided silicon strip detector. (From Hubbeling et al.)

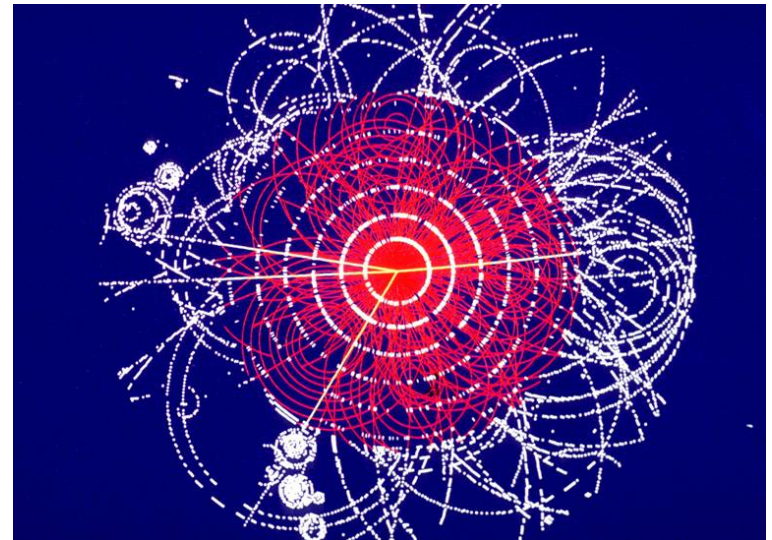
Space Point

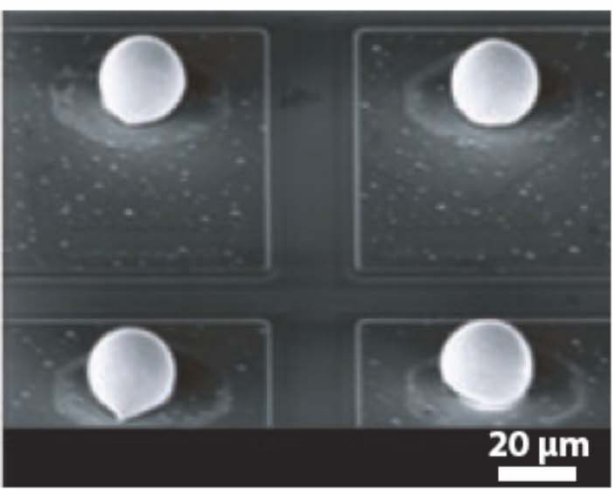
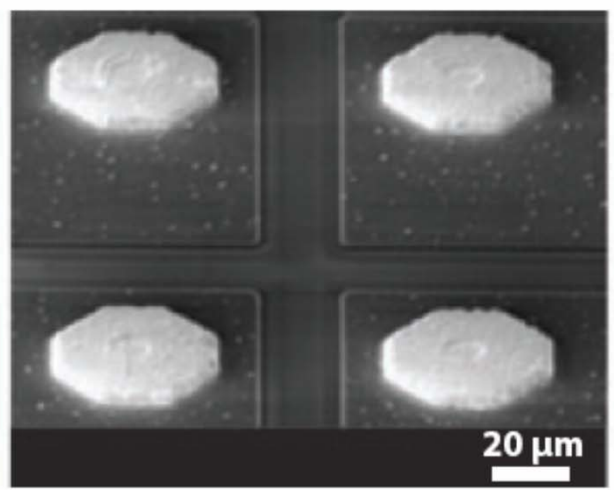
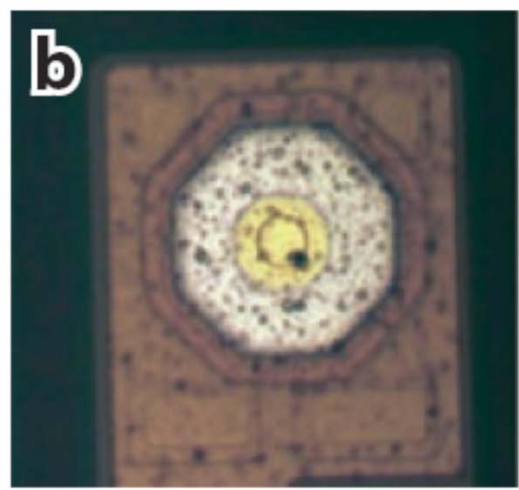
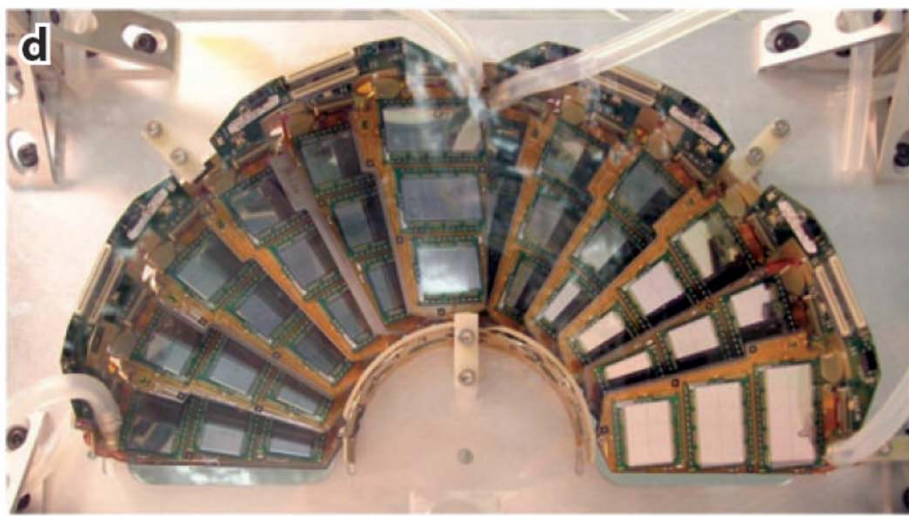
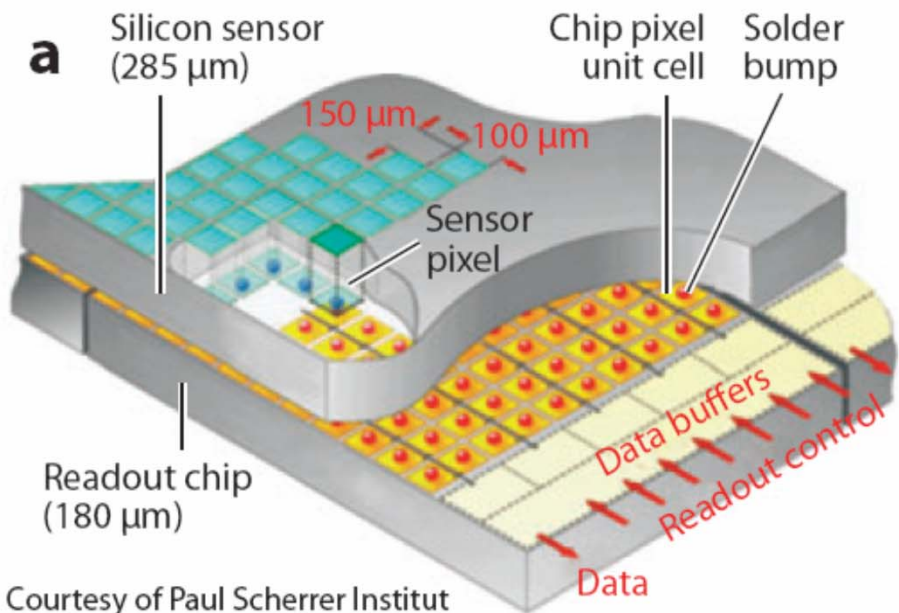
- Harder to fabricate (more expensive)
- Less material – less MCS

Pixel Detector

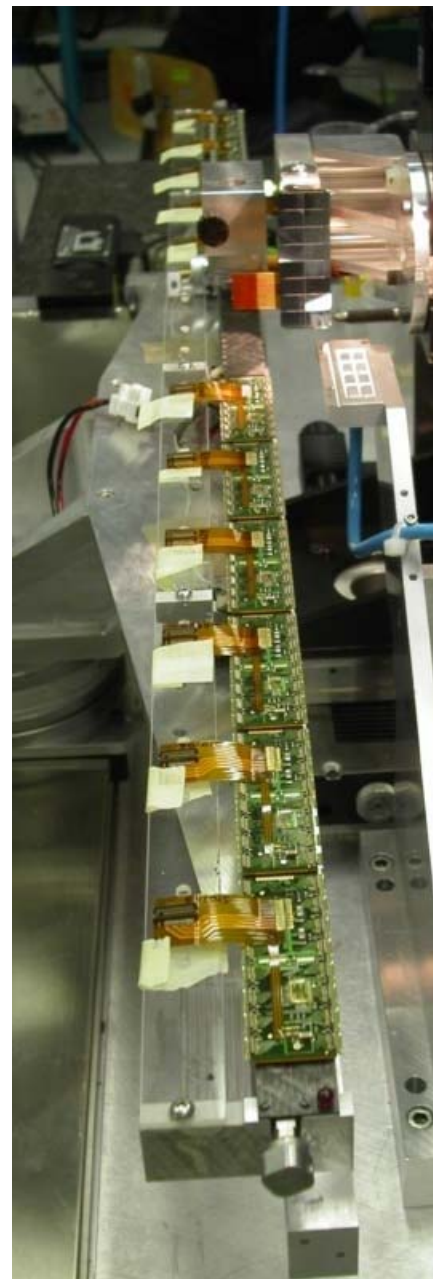
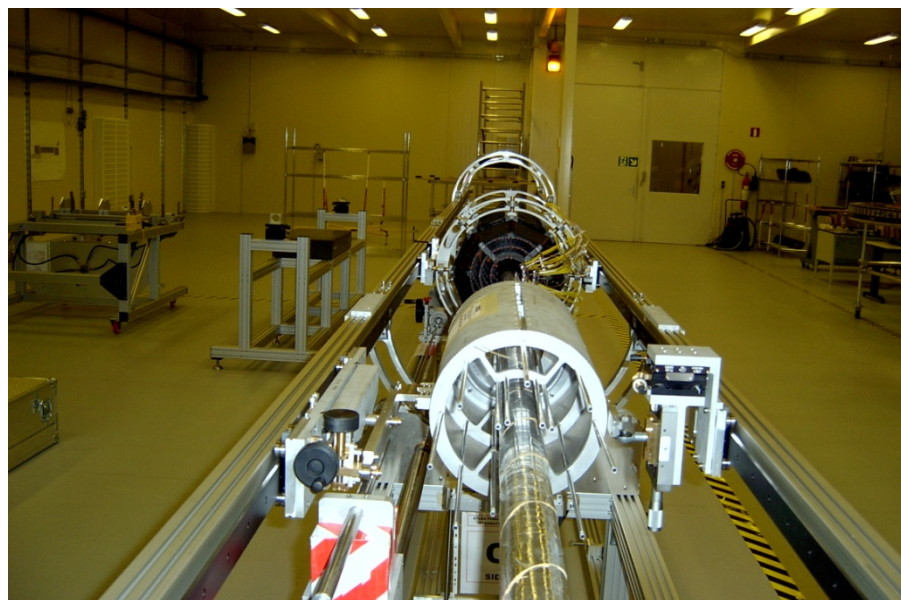
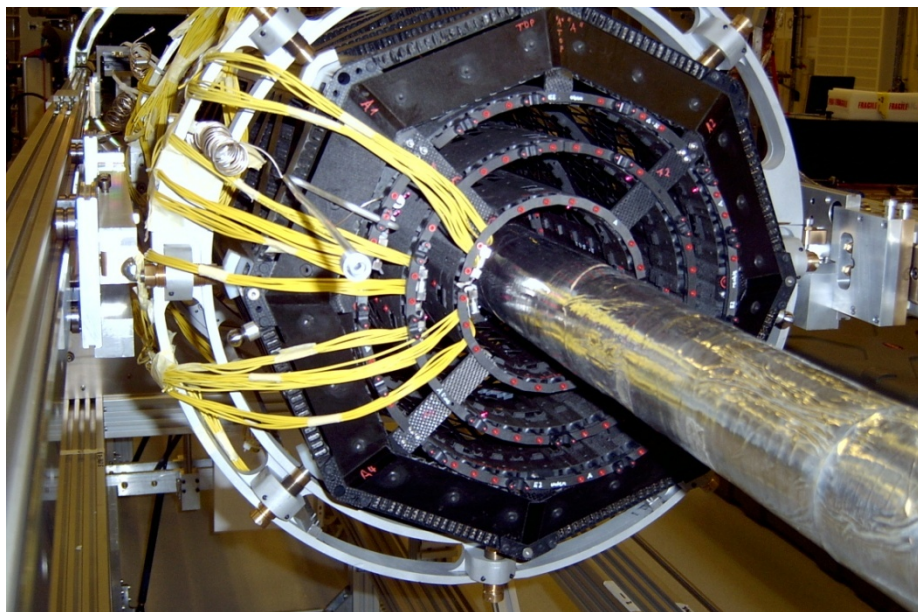


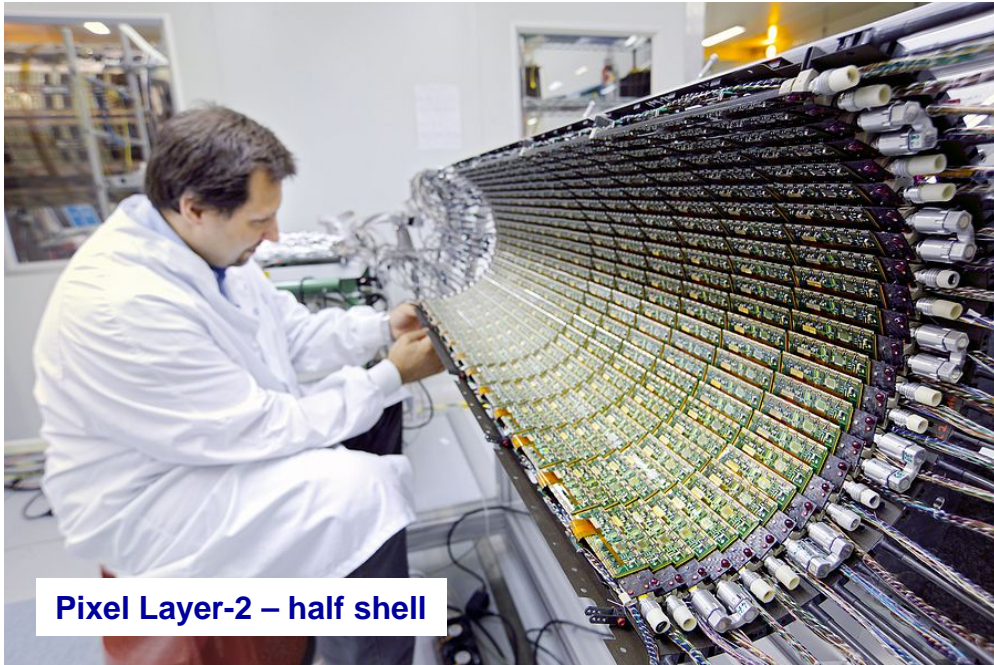
- Each sensor gives a space point
- Enormous advantage in high occupancy environment



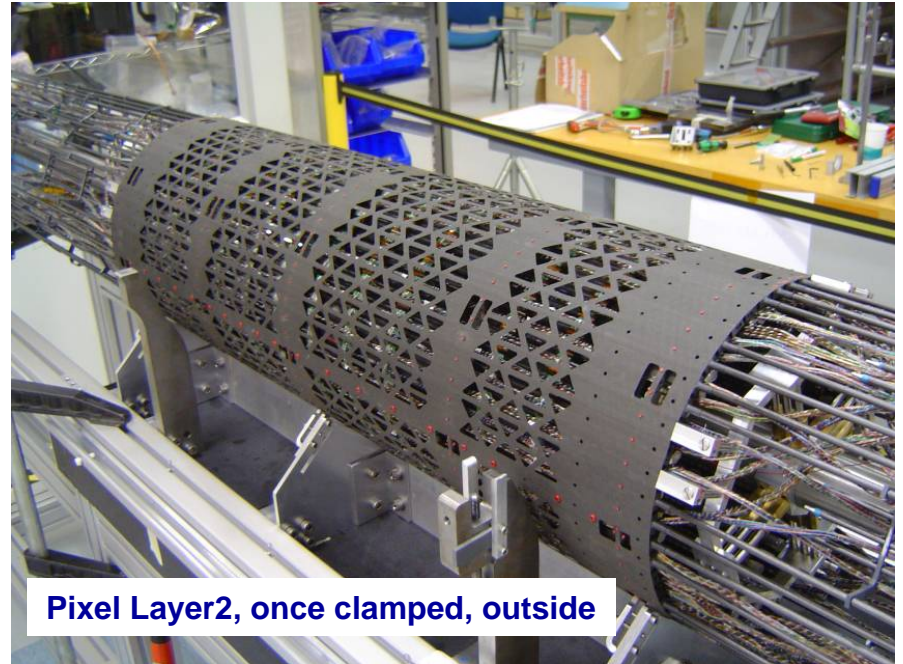


Pixel System

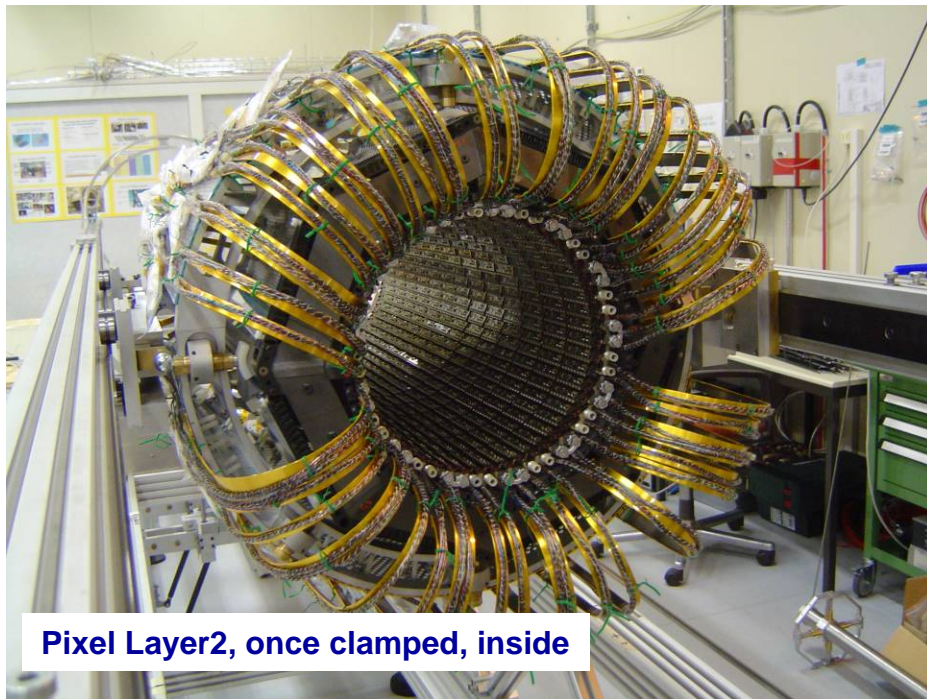




Pixel Layer-2 – half shell



Pixel Layer2, once clamped, outside



Pixel Layer2, once clamped, inside

“Ready for installation” date is 1st April 2007

CCD USE MOS STRUCTURE

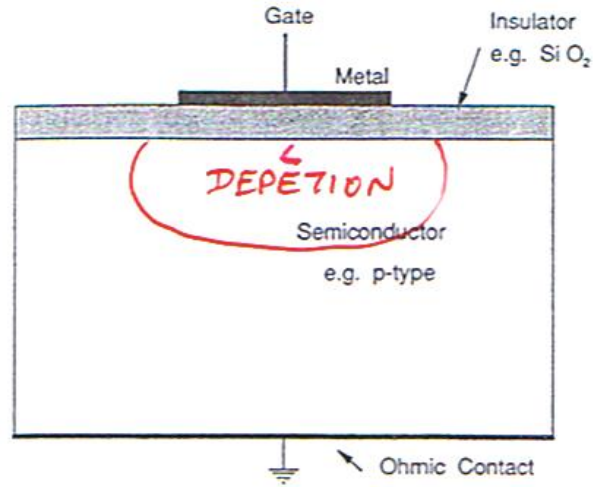
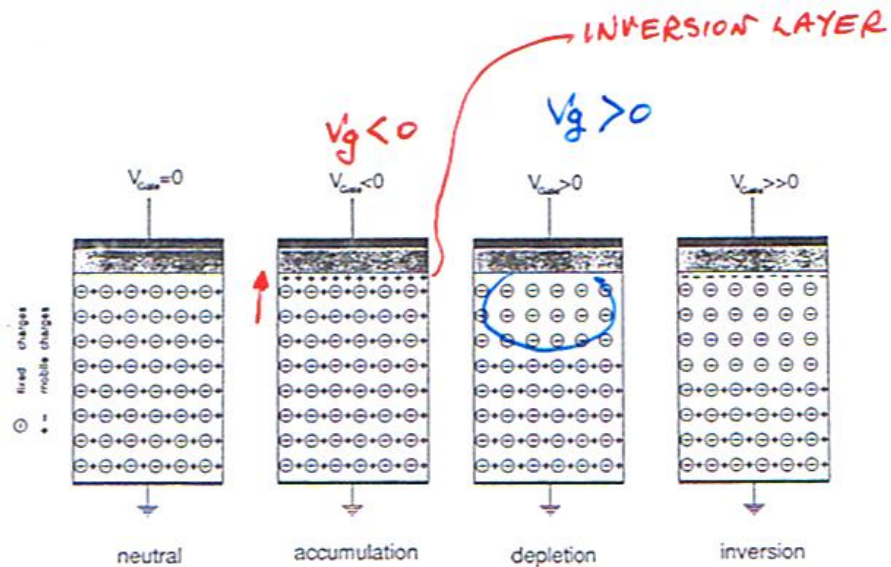


Figure 8: Cross section of a Metal-Oxide-Semiconductor (MOS) structure.



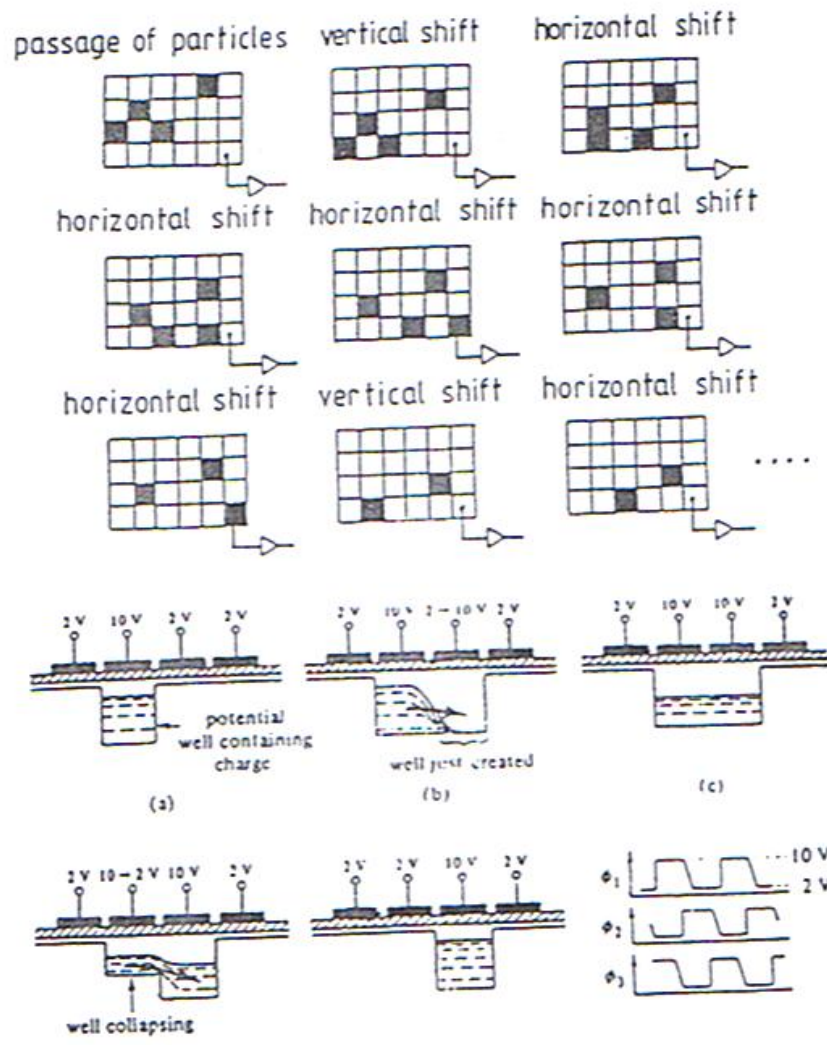
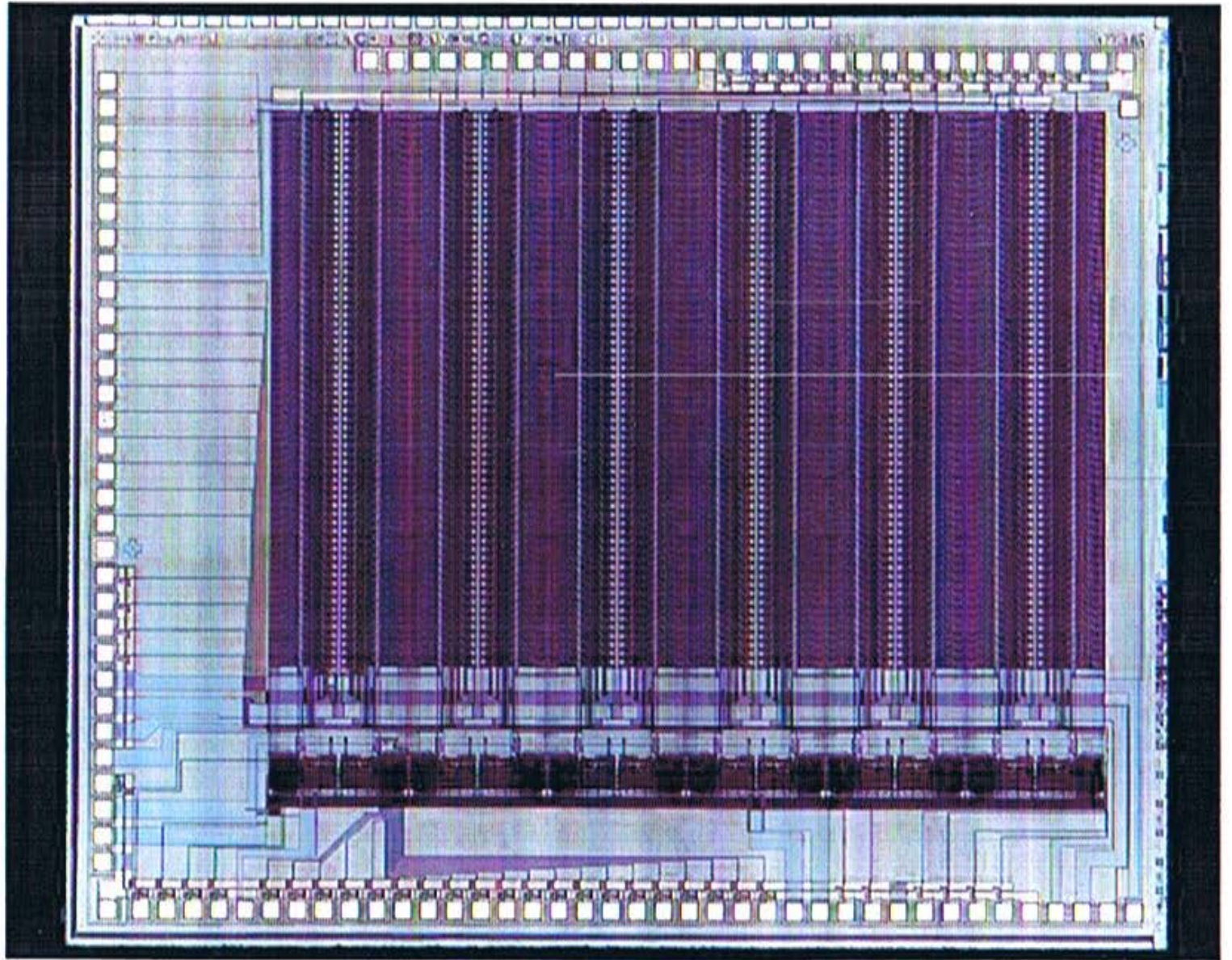


Fig. 3.5 Principle of a CCD.

PIXEL Chip



RADIATION DAMAGE TO SILICON

IMPORTANT ISSUE @ HIGH LUMINOSITY

PARTICLES TRAVERSING SENSOR

— DISPLACE ATOMS

— DEFORM LATTICE

— CREATE COMPLEX STRUCTURES

ALL THESE LATTICE DEFECTS POPULATE

NEW ENERGY LEVELS IN THE BAND GAP

— INCREASE LEAKAGE CURRENT

— CHANGE DEPLETION VOLTAGE

• NEW ACCEPTOR LEVELS

— DECREASE CHARGE COLLECTION
DUE TO TRAPPING

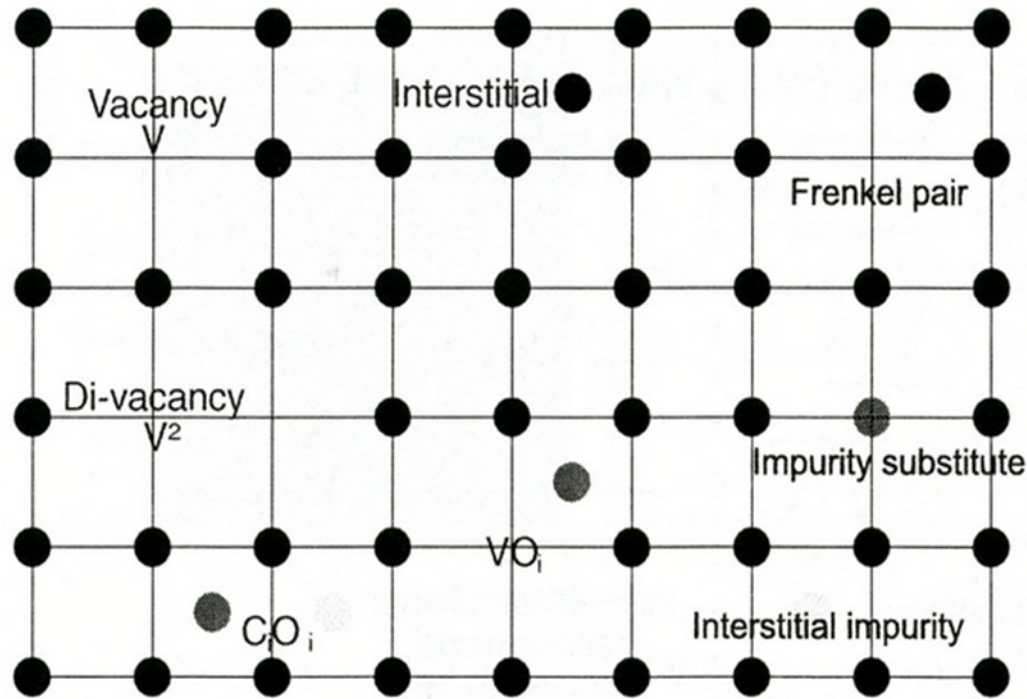


Fig. 1.50 The figure shows an exemplary selection of atomic displacements in the lattice after collision with traversing particles. These vacancies, interstitials and complex clusters are creating new levels in the energy scheme of the semiconductor and therefore change the elementary properties. As abbreviation, vacancies are labeled V , interstitials I , di-vacancies V_2 . Impurities are labeled with their atomic sign, their index defines their position as substitute or interstitial, e.g. C_s or C_i

ANNEALING

INTERSTITIALS AND VACANCIES MOBILE $T > 150K$
AFTER RADIATION DAMAGE PROPERTIES
CHANGE WITH TIME

- FAST
- FRENKEL PAIR RECOMBINATION
 - VACANCY + INTERSTITIAL RECOMBINATION
- SLOW - RECOMBINATION OF COMPLEX STRUCTURES

INITIAL BENEFICAL ANNEALING FOLLOWED
BY LONG TERM DEGRADATION

ANNEAL AT $60^{\circ}C$ FOR 80 MIN

↳ THEN FREEZE ANNEALING AT $< 20^{\circ}C$

with $\alpha_I \sim 1.25 \cdot 10^{-17}$ A/cm, $\beta \sim 3 \cdot 10^{-18}$ A/cm and $t_0 = 1$ min. τ_I takes the annealing temperature T_α dependence into account, where

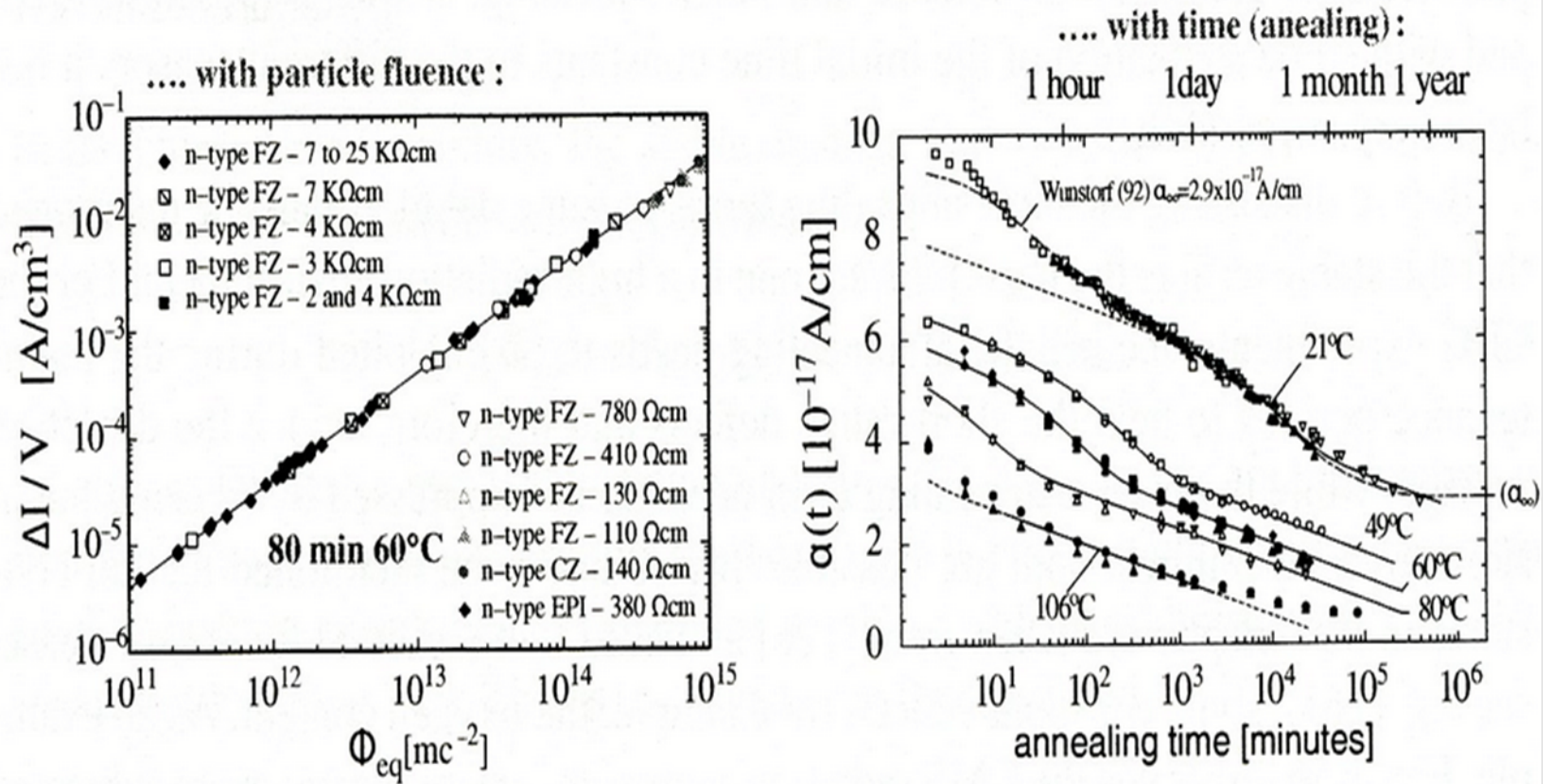


Fig. 1.54 Leakage current vs. fluence and annealing time [126, 166]

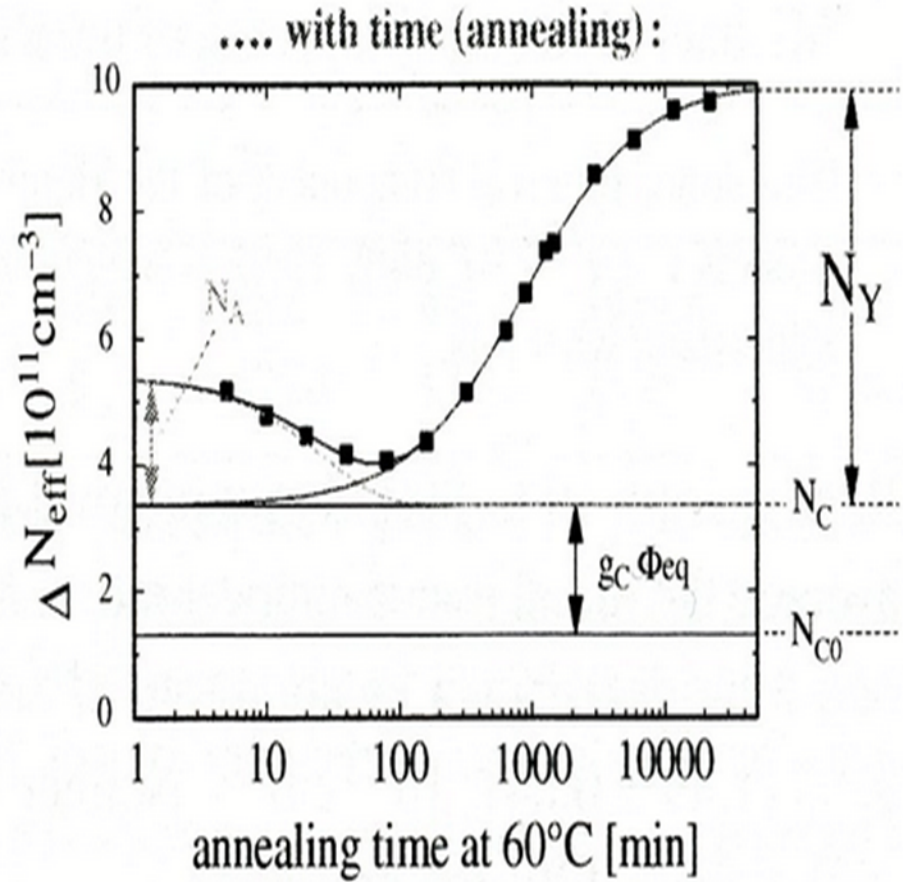
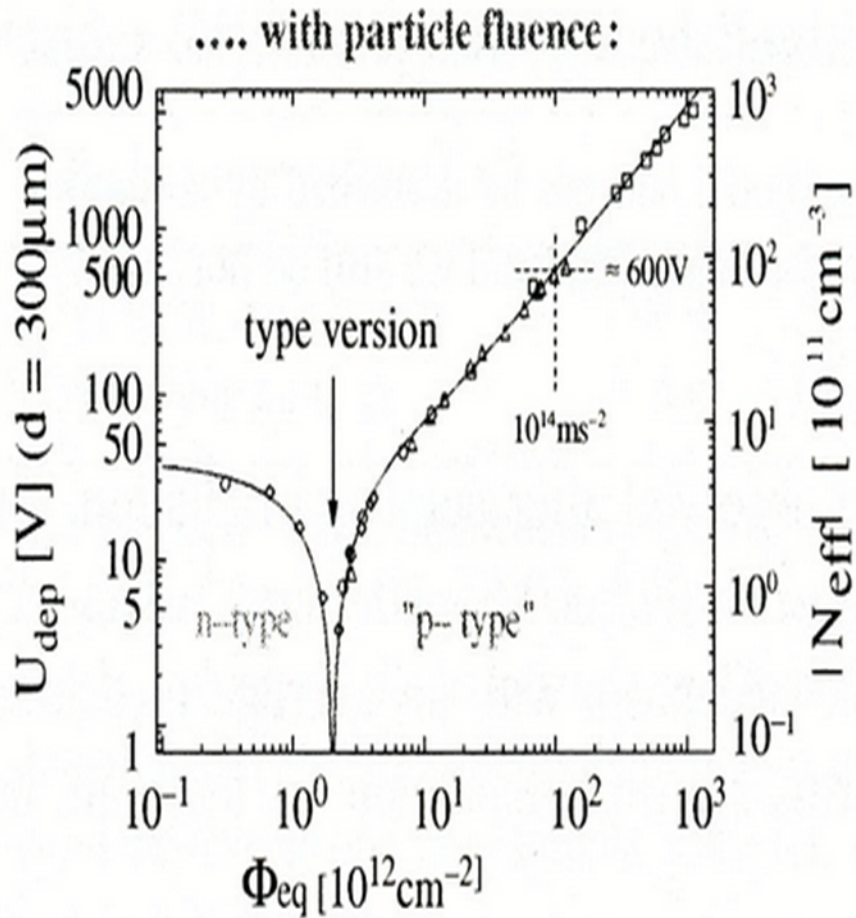


Fig. 1.55 Depletion voltage current vs. fluence and annealing time [126]

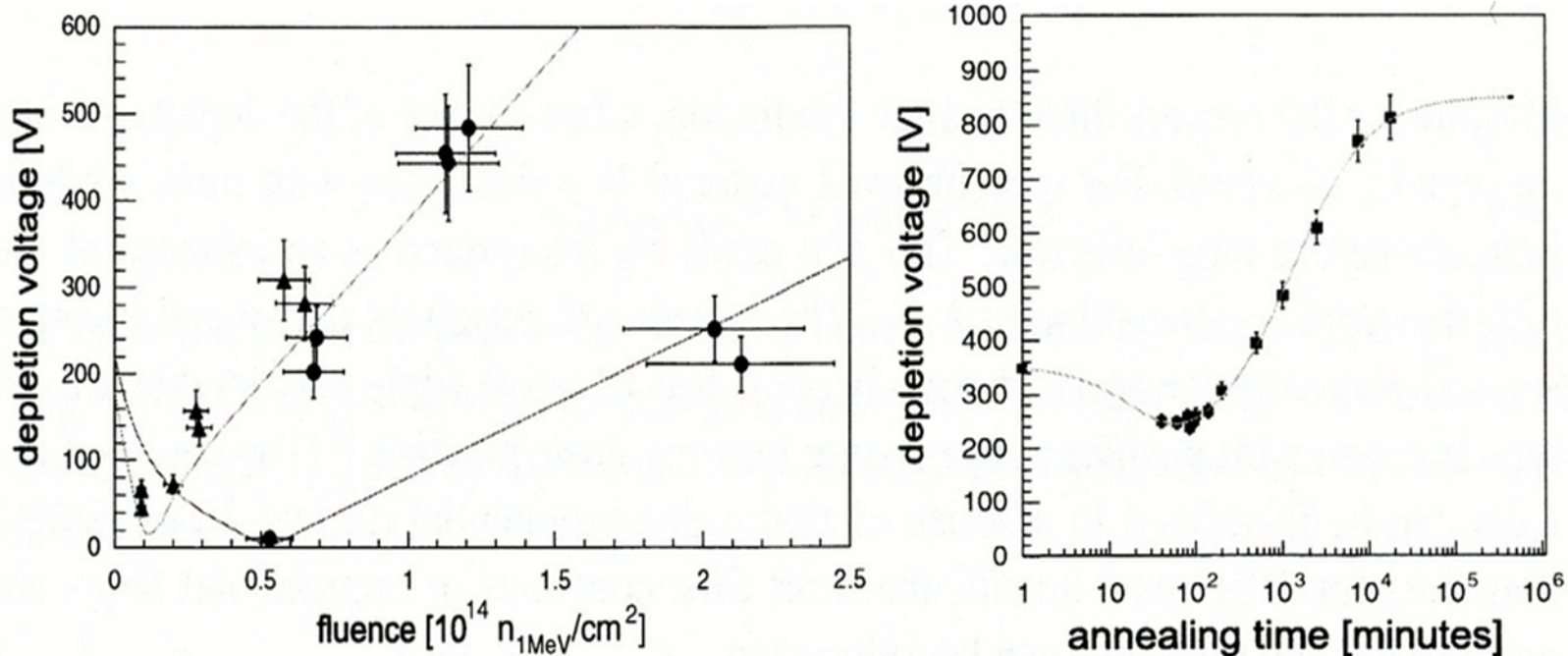


Fig. 1.56 Evolution of V_{FD} for different fluences and annealing durations. To have a basis for radiation evaluation, CMS irradiated several sensors and modules to get actual adapted fit parameters to the Hamburg model for the specific procured sensors. In this case, the beneficial constants g_a were found to be $1.11 \pm 0.16 \cdot 10^{-2} cm^{-1}$ and $t_a(60^\circ C) = 21 \pm 8$ min; the reverse constants are $G_y = 4.91 \pm 0.27 \cdot 10^{-2} cm^{-1}$ and $t_y(60^\circ C) = 1290 \pm 262$ min.

The different V_{FD} curve behaviours in the *left plot* can be explained by the different sensor thicknesses of 500 μm (upper curve) and 320 μm (lower curve) – mind $V_{FD} \sim N_{eff} \cdot D^2$. At fluences of 10^{14} , V_{FD} of the thick sensor would have increased above 1000 V. The initial compatible V_{FD} values are due to the different sensor resistivities. Data are compared to calculations for an annealing time of 80 min and an annealing temperature of $60^\circ C$ at each fluence step. More about this study is described in Sect. 5.1.2 and [162]

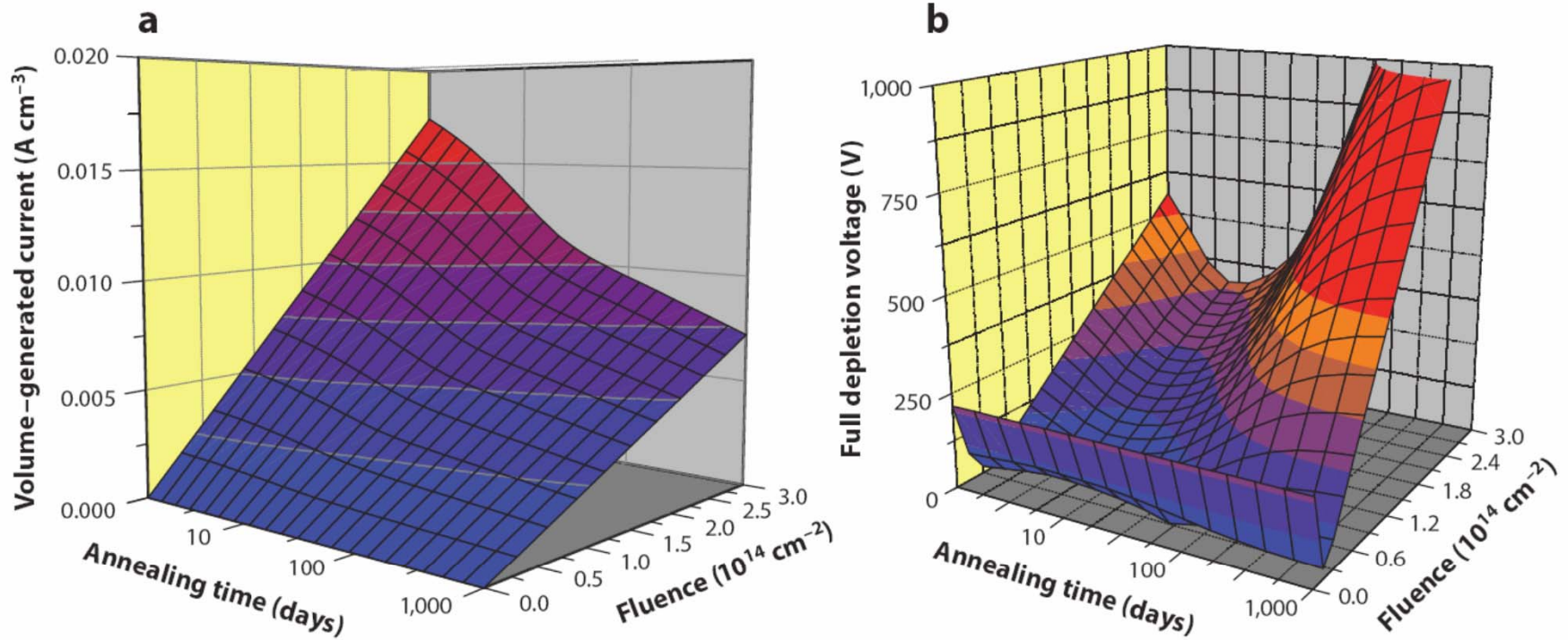
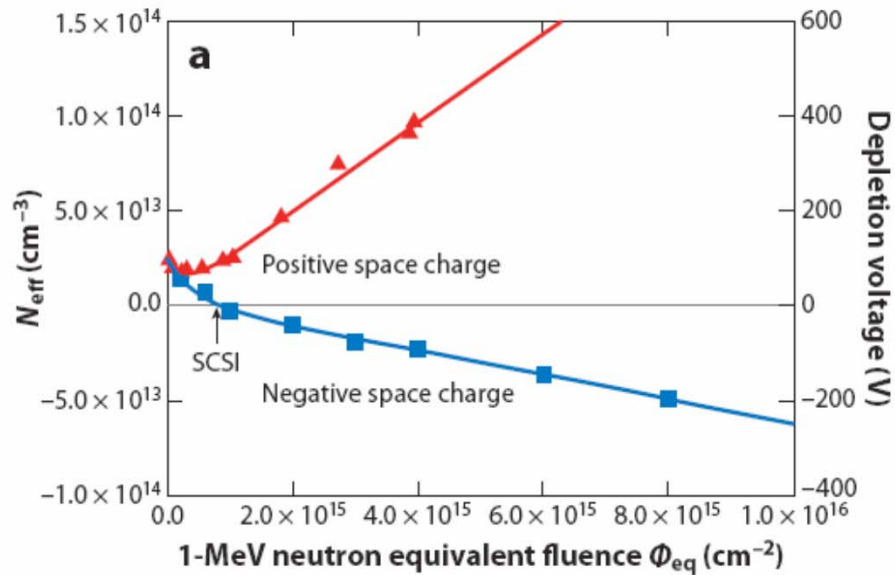


Figure 6

The evolution of current and full depletion voltage ($\sim |N_{\text{eff}}|$) versus fluence and further annealing at room temperature (22). In panel *b*, the dip around 0.5×10^{14} in the fluence axis reveals the space charge sign inversion point; the minimum in the time axis illustrates when the reverse annealing becomes relevant.

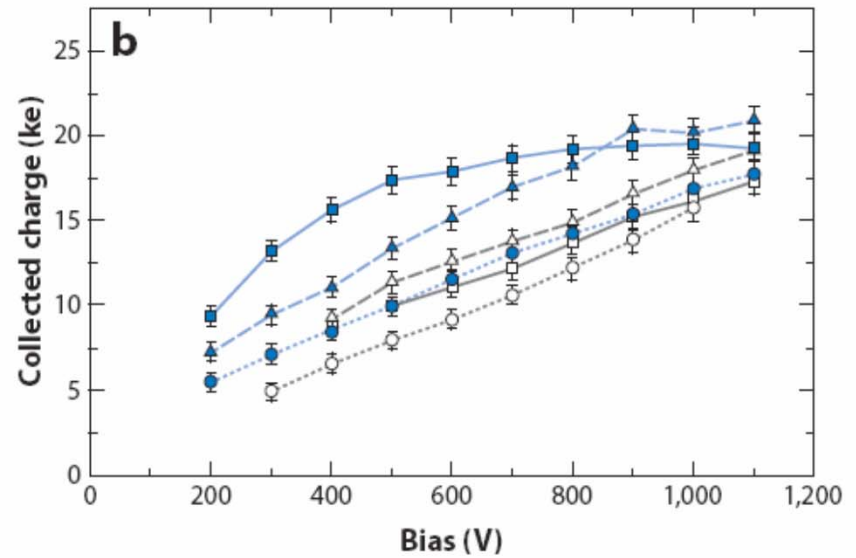
TYPE INVERSION ONLY HAPPENS FOR n-BULK



Reactor neutrons: 23-GeV protons:

■ Experimental data ▲ Experimental data

— Fit (Hamburg model) — Fit (Hamburg model)



■ *n-in-n* MCz ($5 \times 10^{14} \text{ cm}^{-2}$ neutrons + $5 \times 10^{14} \text{ cm}^{-2}$ protons)

□ *n-in-n* FZ (5×10^{14} neutrons + 5×10^{14} protons)

● *n-in-n* MCz ($1.1 \times 10^{15} \text{ cm}^{-2}$ protons)

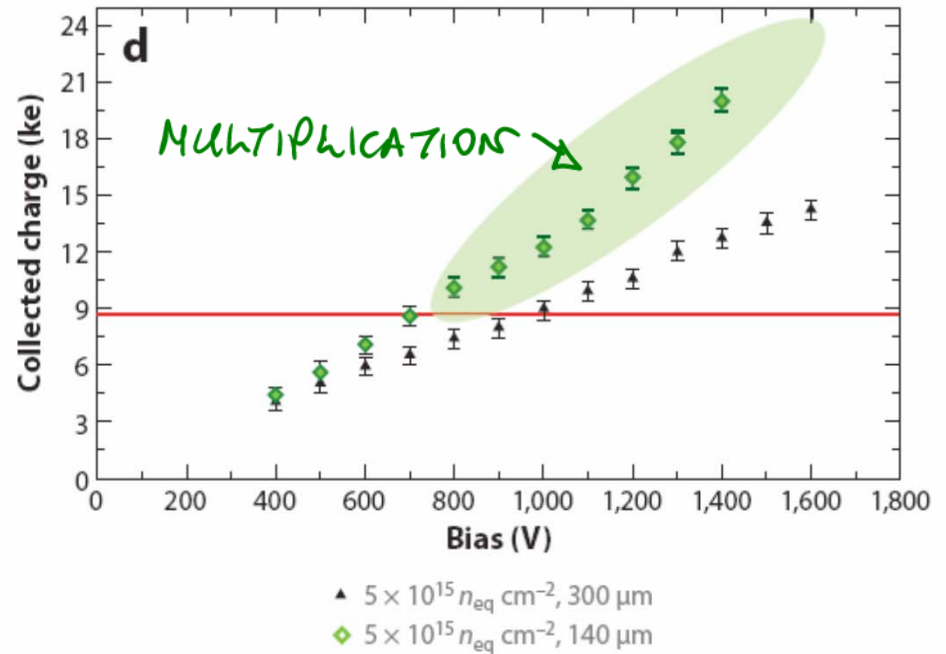
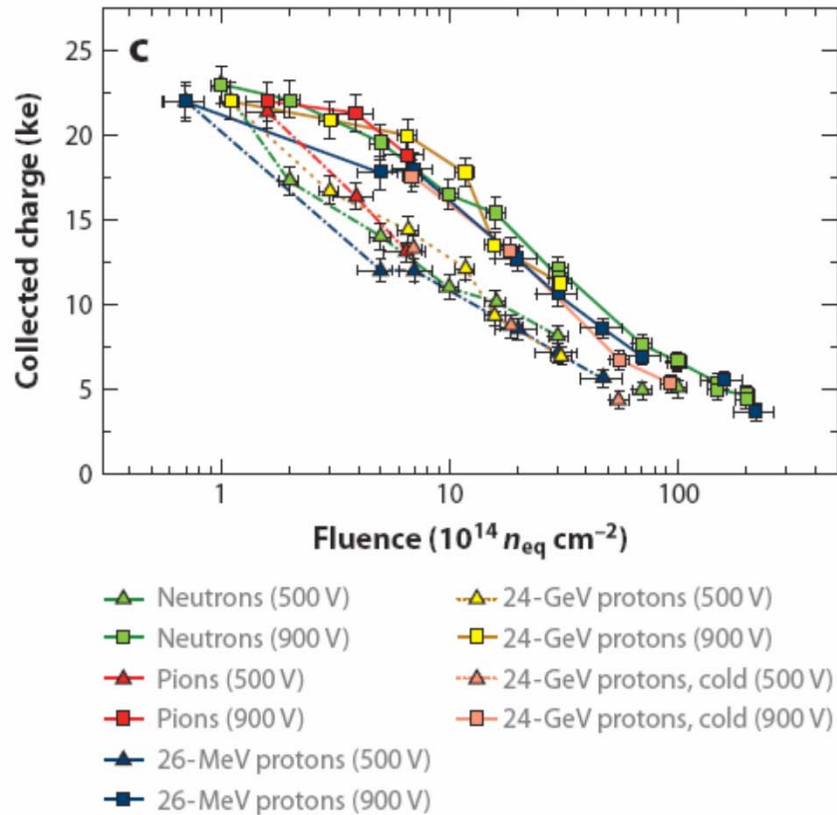
○ *n-in-n* FZ ($1.1 \times 10^{15} \text{ cm}^{-2}$ protons)

▲ *n-in-n* MCz ($1 \times 10^{15} \text{ cm}^{-2}$ neutrons)

△ *n-in-n* FZ ($1 \times 10^{15} \text{ cm}^{-2}$ neutrons)

PROTON + NEUTRON ADD
UP FOR FLOAT ZONE

CANCEL FOR CZOCHARALSKI



AT HIGH FLUENCES
 CHARGE COLLECTION
 EFFICIENCY BECOMES
 PARTICLE INDEPENDENT
 $\eta - I - P$

AT HIGH FLUENCES
 SEE ELECTRON MULTIPLICATION

Experimental Study and Empirical Modeling of Long Term Annealing of the ATLAS18 Sensors

Robert S. Orr

On behalf of the ATLAS ITk Collaboration

Motivation

- The ATLAS ITk – or for that matter any silicon detector - will suffer radiation damage and temperature dependent annealing
 - Increase of leakage current - operational consideration
 - Increase of Full Depletion Voltage – operational consideration
 - Reduction of Charge Collection Efficiency
 - At some level of degradation this will adversely affect the efficiency for track finding
 - Annealing is reduced at low temperature
 - Not possible to just keep detector at very low temperature permanently
 - For the ITK this period would be 14 years
 - Detector maintenance
 - Cooling system maintenance
 - Other possible warm ups
 - While the phenomenon of annealing after radiation damage is interesting in its own right, we have taken a more empirical approach

Parametrisation of Long Term Annealing

- Rather than trying to develop a deep theoretical understanding, I wanted to come up with some “physically motivated” parametrisation.
- The Hamburg Model seems to be the standard way of understanding annealing effects – so this is a starting point
- Initially looked at some ATLAS12 data
 - ATLASyy are a series of strip sensor prototypes produced by Hamamatsu Photonics from designs by ATLAS ITk – ATLAS18 is the production series
 - The ATLAS12 data has been published in NIM A 924 (2019) 128-132 L. Wiik-Fuchs et al
 - That publication is a subset of data from Leena Diehl – Freiburg Ph.D. Thesis 2018
 - Leena Diehl kindly provided me with the numerical data, and also some additional measurements from her thesis

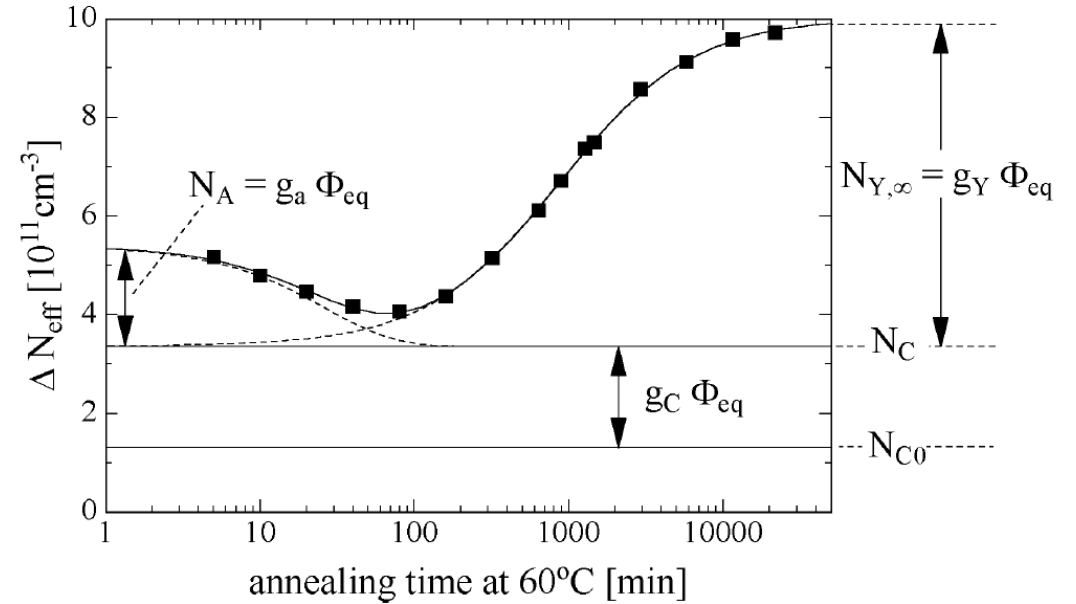
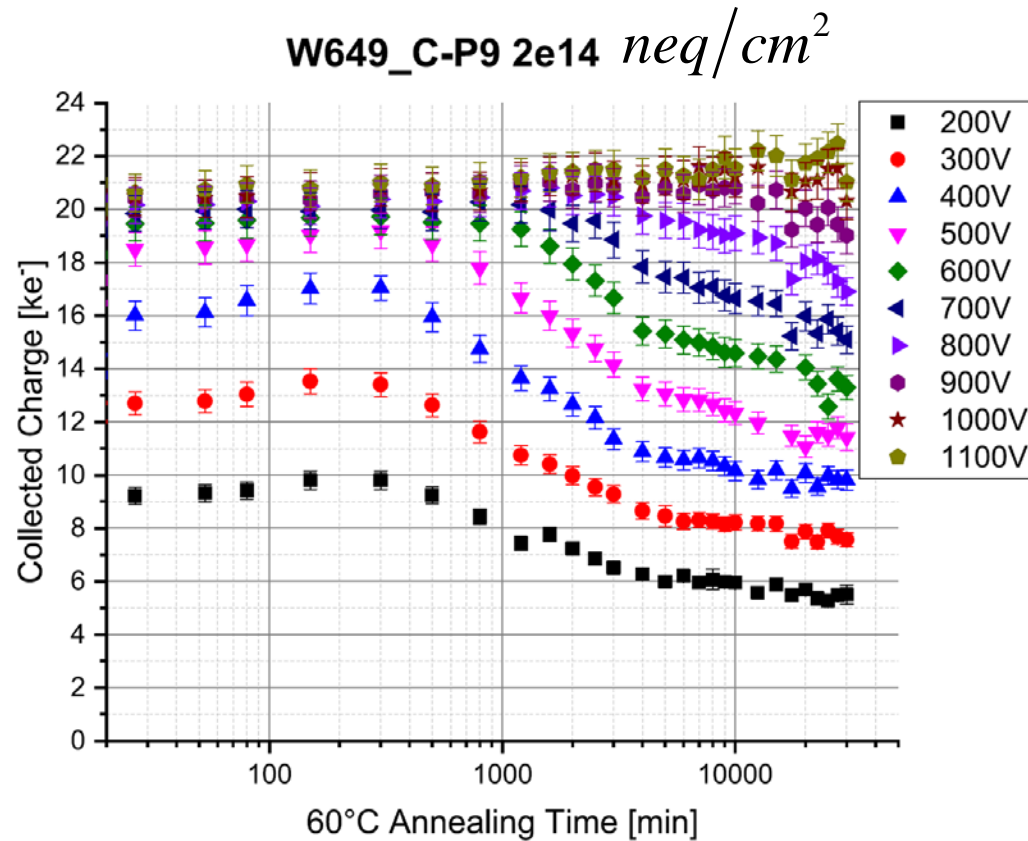


Figure 5.9: Annealing behavior of the radiation induced change in the effective doping concentration ΔN_{eff} at 60°C. The shown example is a sample of type WE-25kΩcm irradiated with a fluence of $1.4 \times 10^{13} \text{ cm}^{-2}$.

- Effective doping concentration N_{eff} depends on Φ_{eq} - fluence of irradiation and time.
- The model hypothesises that there are three phases of annealing in time.

- **Short Term beneficial annealing**

$$N_A(\Phi_{eq}, t) = \Phi_{eq} g_a \exp(-t/\tau_a)$$

- **Constant**

$$N_C(\Phi_{eq}) = N_{C,0} \Phi_{eq} g_a (1 - \exp(-C\Phi_{eq})) + g_C \Phi_{eq}$$

- **Long term degradation**

$$N_Y(\Phi_{eq}, t) = \Phi_{eq} g_Y (1 - \exp(-t/\tau_Y))$$

- **Ansatz = Guess** $CCE \propto (1/N_{eff})$

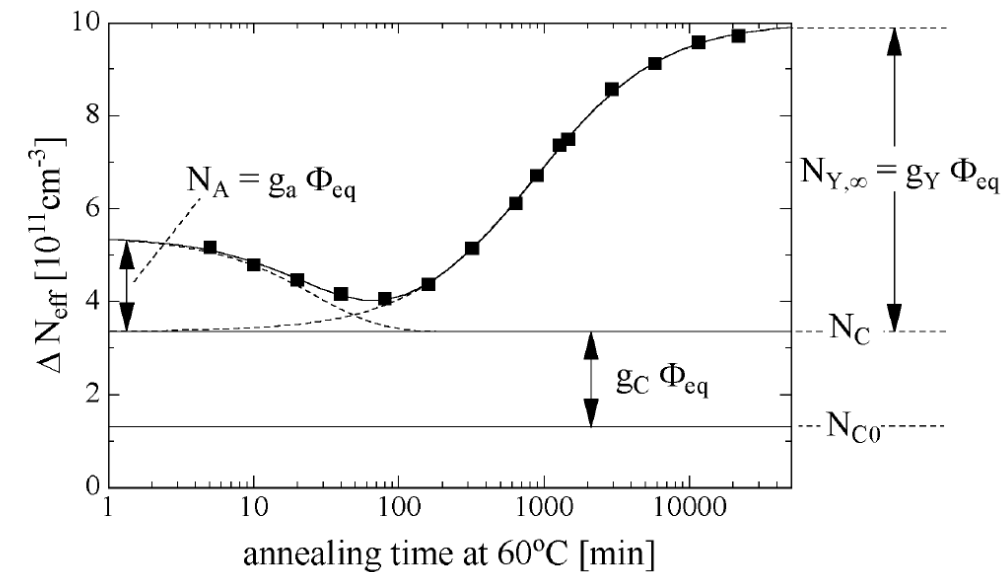


Figure 5.9: Annealing behavior of the radiation induced change in the effective doping concentration ΔN_{eff} at 60°C. The shown example is a sample of type WE-25kΩcm irradiated with a fluence of $1.4 \times 10^{13} \text{ cm}^{-2}$.

We parametrize the collected charge as a function of irradiation fluence as :

$$1 / \left(g_a \exp(-t/\tau_a) + g_C + g_Y (1 - \exp(-t/\tau_Y)) \right)$$

g_a - Coefficient for short term annealing

τ_a - Diffusion time for short term annealing

g_C - Constant term

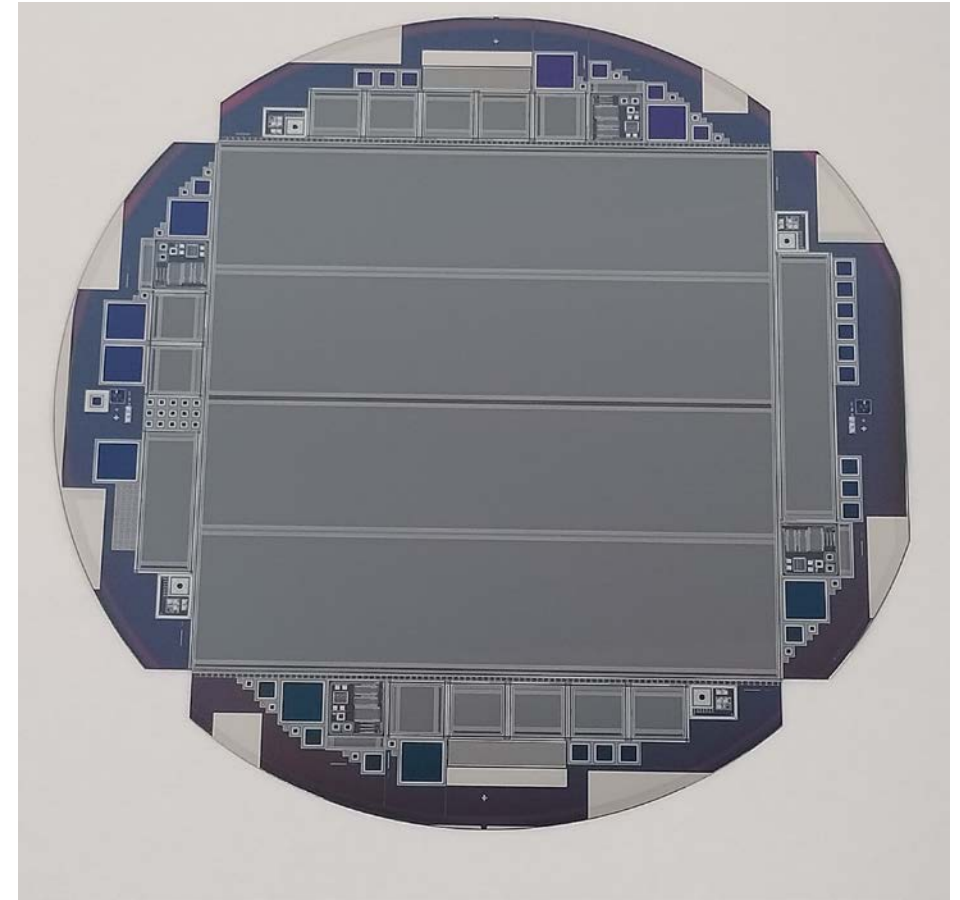
g_Y - Coefficient for long term annealing

τ_Y - Diffusion time for long term annealing

The **dependence** of the collected charge on fluence is incorporated in the g-coefficients

Miniature Sensors

- Each wafer produced by Hamamatsu contains full size sensors which are rectangular or trapezoidal in shape.
- This leaves space for other structures around the periphery of the wafer.
- ATLAS populates this area with test structures and miniature sensors.
- The miniature sensors are “identical” to full size sensors – same strip and bias/guard ring structures, and several sizes. The miniature sensors in this study are 1cm x 1cm with 104 strips of 8 mm length.
- In this study the miniature sensors were irradiated with 24 MeV protons ([ATLAS12 at Karlsruhe](#)) and reactor neutrons ([ATLAS12 and ATLAS18 at Ljubljana](#))

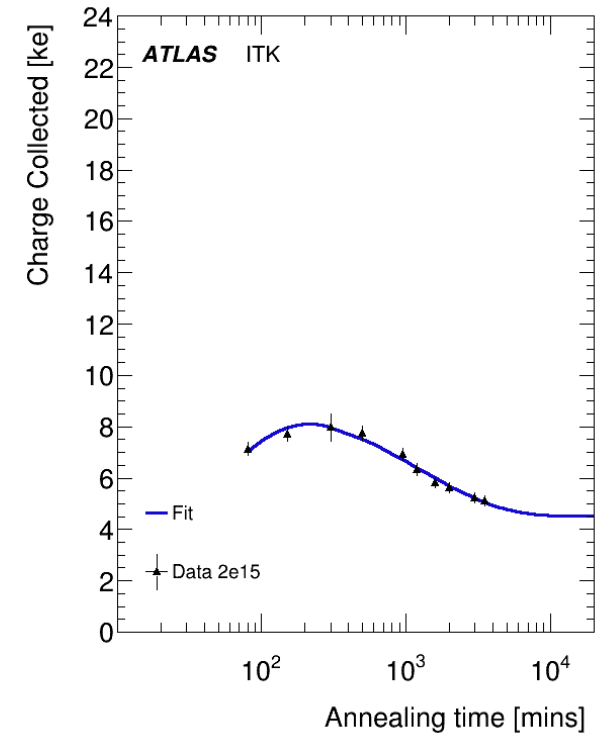
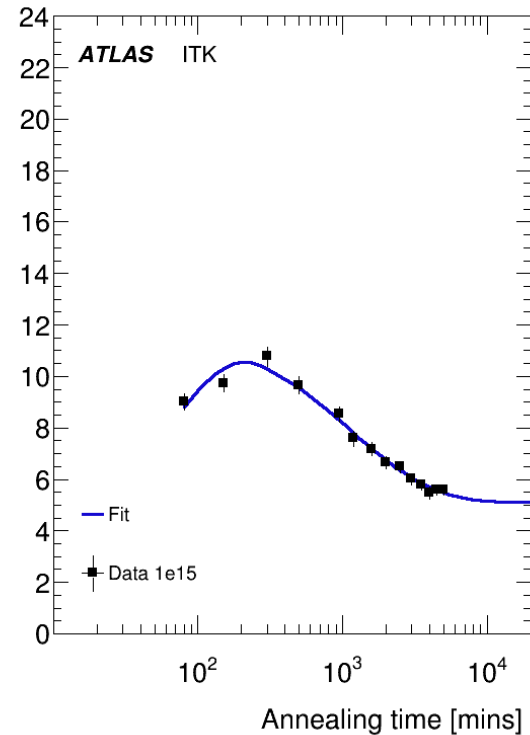
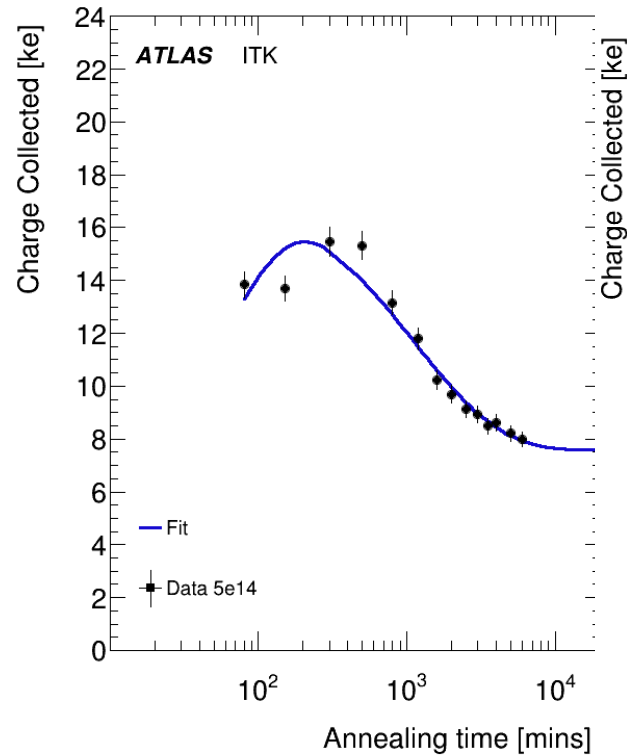
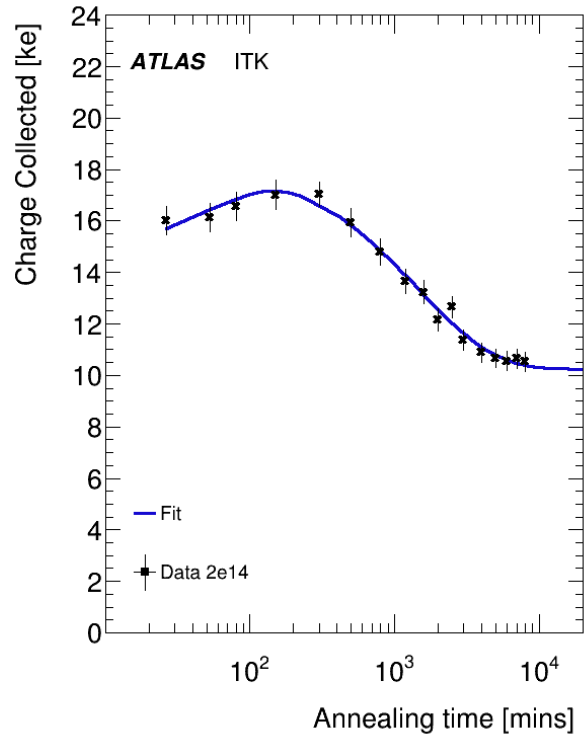


ATLAS18 Wafer

Fitting Procedure

- Initially fit distribution at each fluence with all parameters free
- To have some predictive power need to reduce number of parameters
- While the g-coefficients are functions of the irradiated fluence, it seems reasonable that the diffusion times are not.
- Refit the distributions at each fluence, with the diffusion times fixed.
 - We used the diffusion times from the fit at $2e14 \text{ neq/cm}^2$
- This extracts a set of g-parameters at each fluence
- We then fit an empirical function to the g-parameters as a function of fluence
- Then use fixed diffusion times and fitted function of g-parameters to give a “prediction” or closure test.
- We have data at many bias voltages
- Unirradiated full depletion voltage is 300V, and the ITk is limited to 500V – so we have only studied 400V and 500V in detail

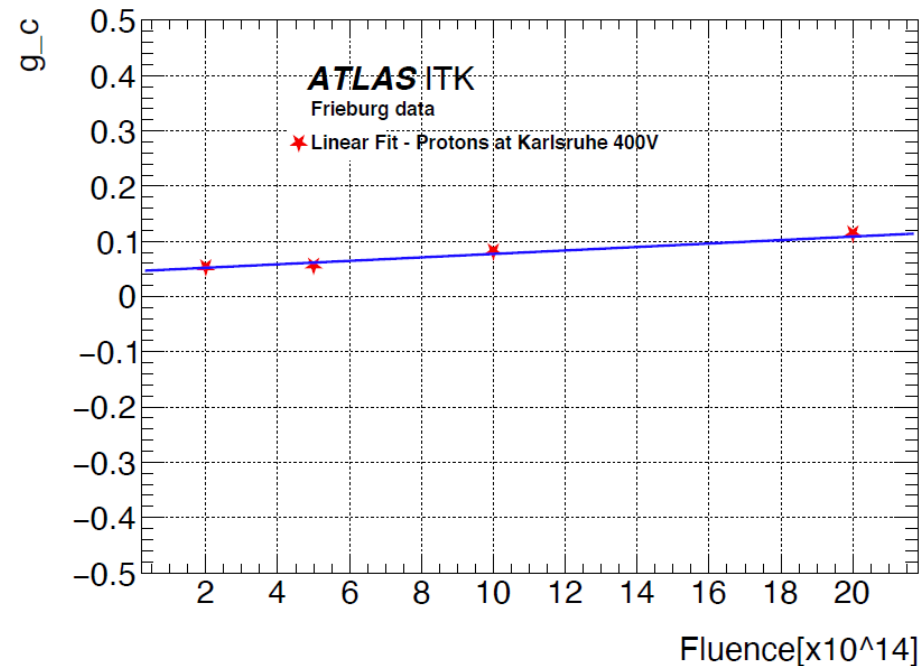
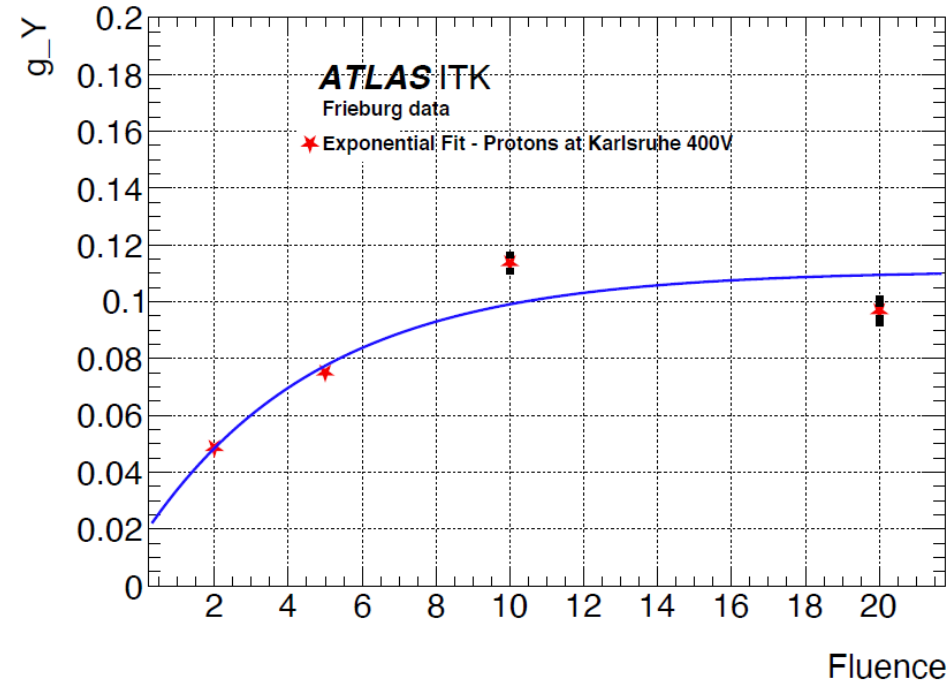
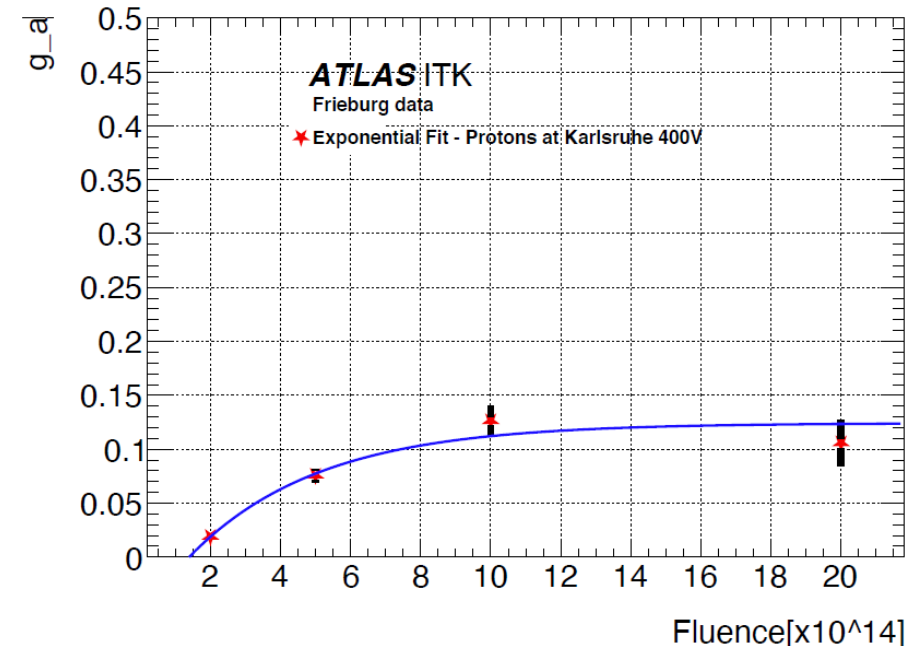
Fit model to 24 MeV Proton Data



- Measured at Freiburg
- Annealing at 60 C
- ATLAS12
- 400 V Bias

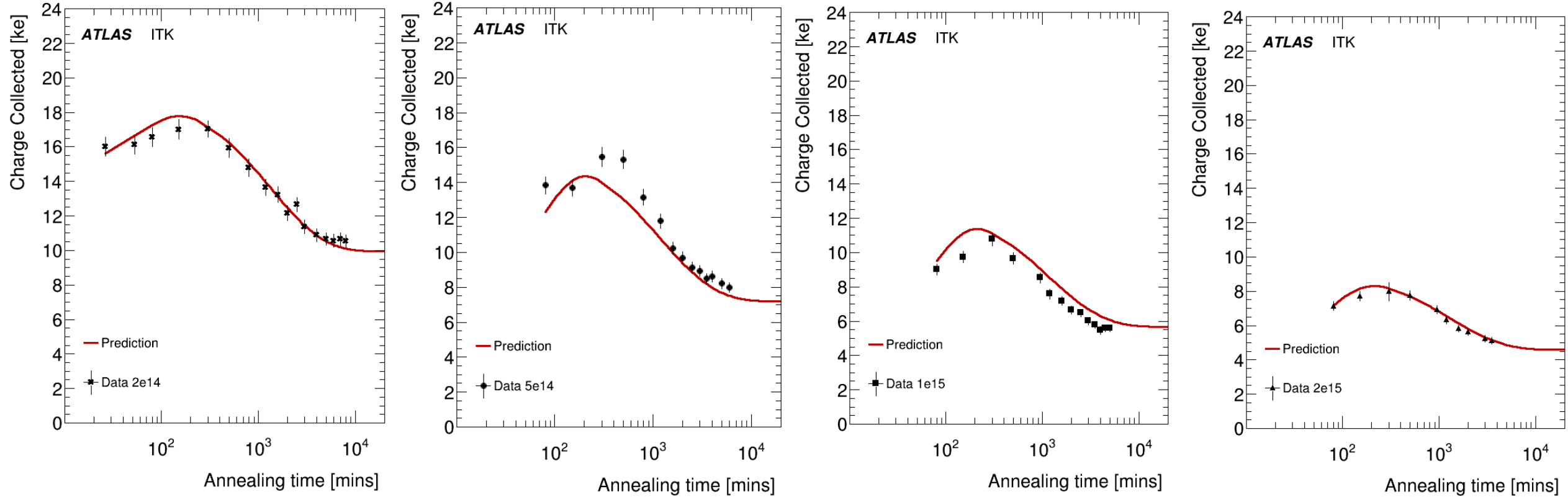
- g- coefficients free at each fluence
- Diffusion times fixed to same value at each fluence $\tau_a = 53s, \tau_Y = 2296s$

Functional Model for Dependence of Coefficients on Fluence



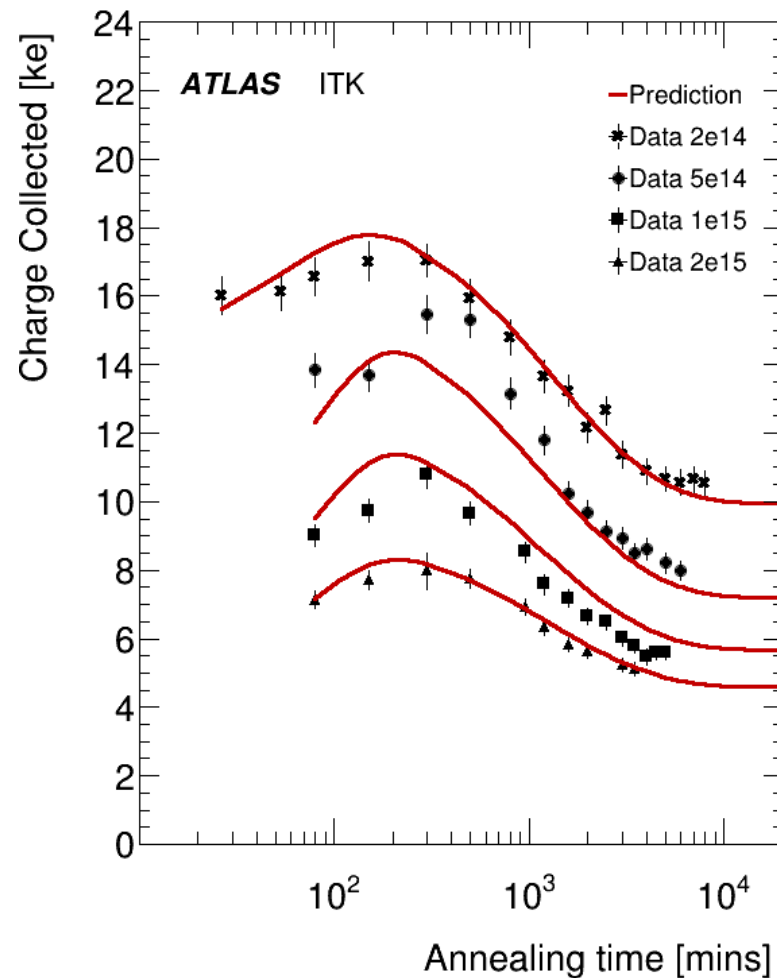
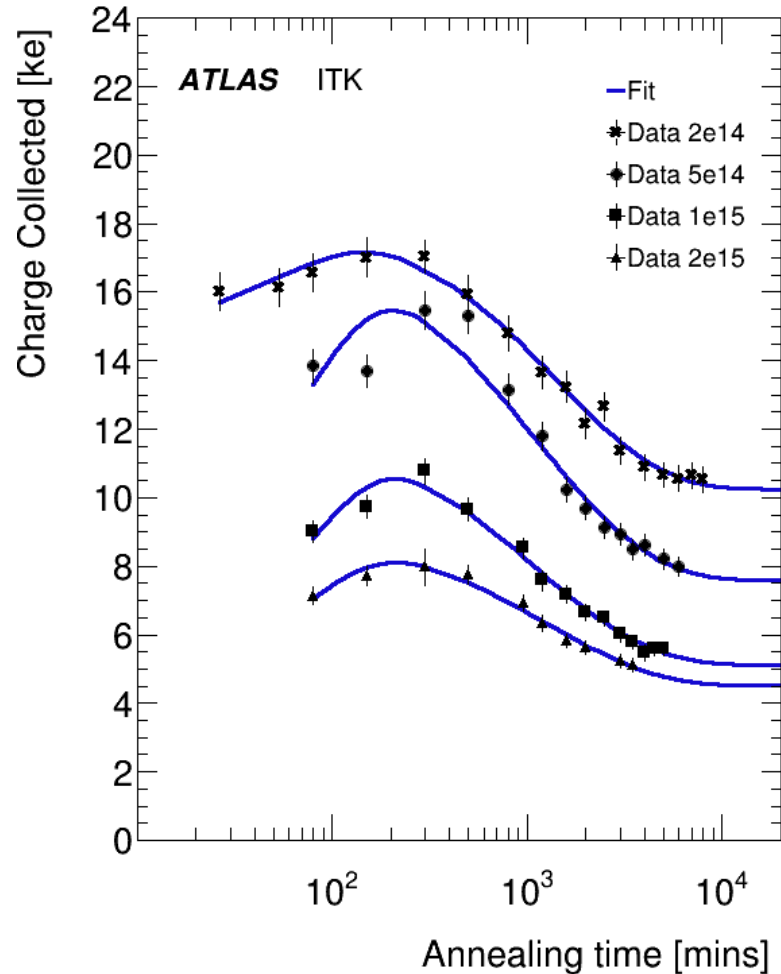
fitted g_a and g_Y to the form $a + b(1 - \exp(-c \times fluence))$ and g_c was taken as linear.

24 MeV protons at Karlsruhe – Closure Test



The fitted functional form of the g-parameters is used to predict the Collected Charge

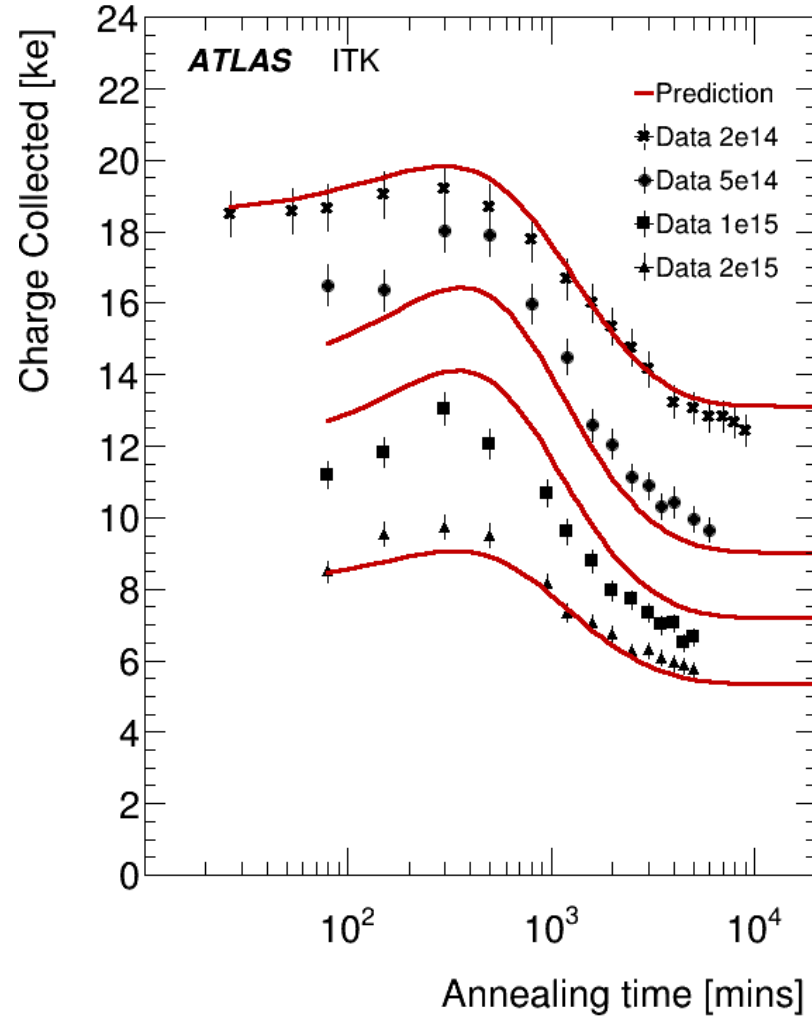
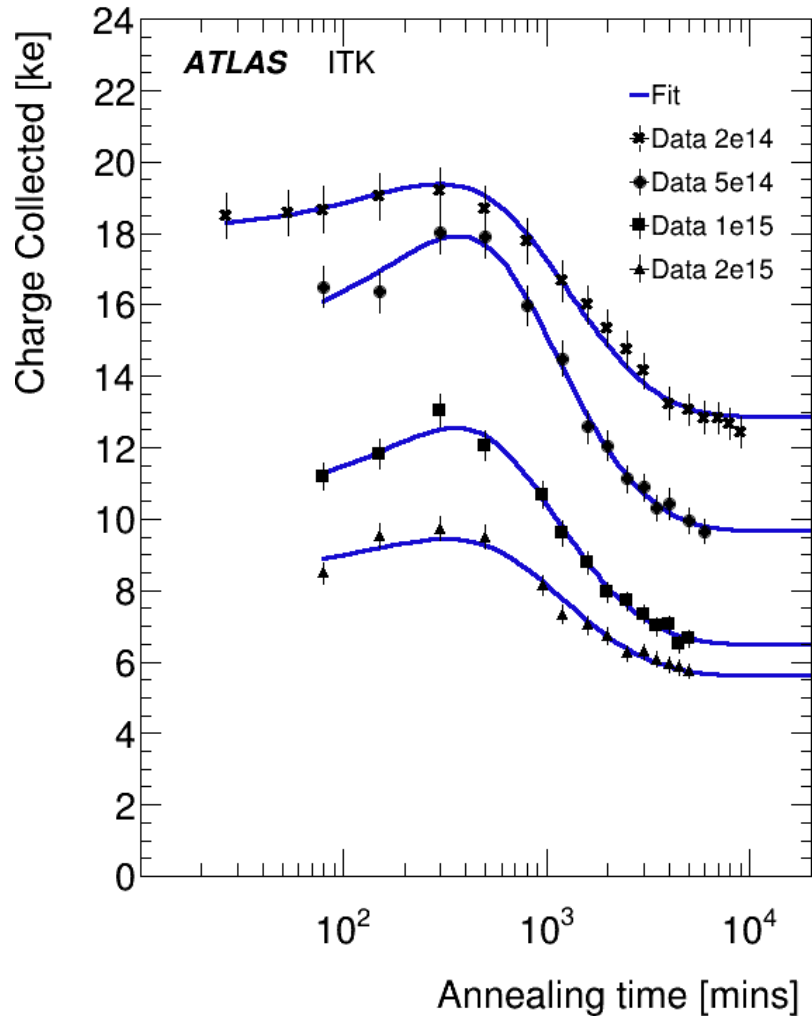
24 MeV protons at Karlsruhe – Closure Test



- ATLAS12
- 400 V Bias Voltage
- Measured at Freiburg
- Annealing at 60 C
- “Fit” is the independent fit to each fluence
- “Prediction” is the prediction of the model using the fitted coefficients as a function of fluence

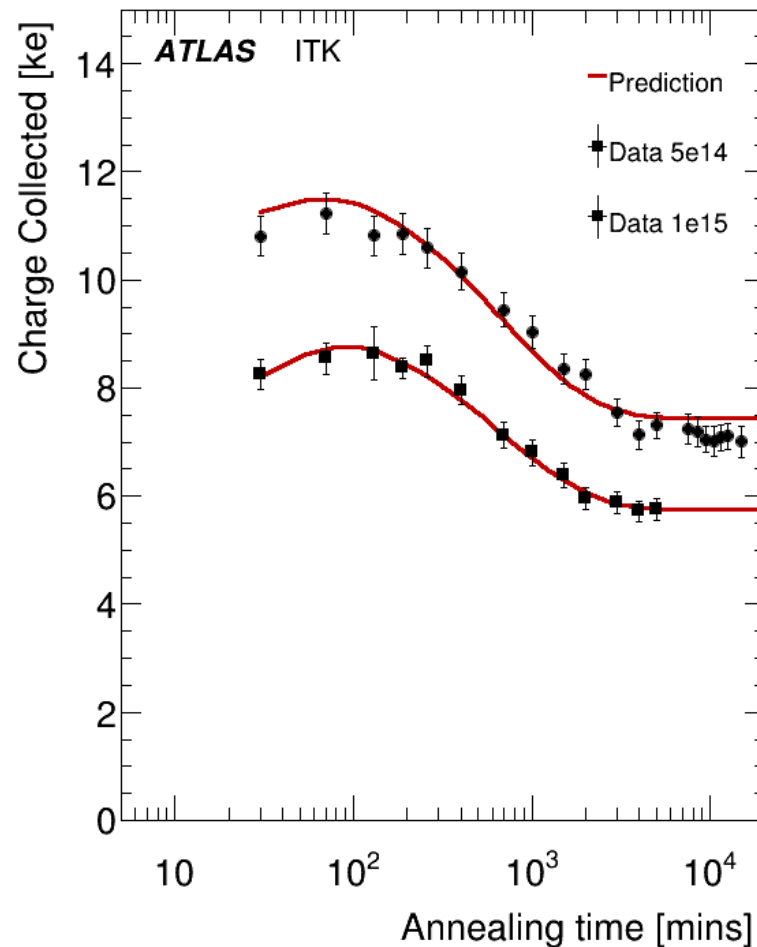
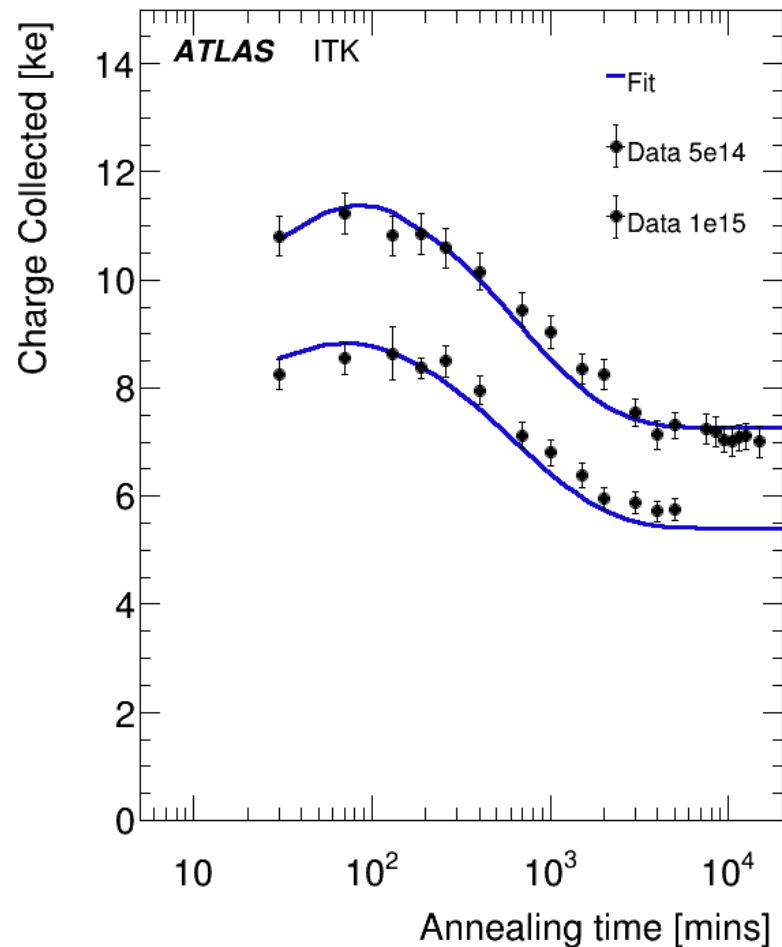
This is a condensation of last three slides

24 MeV protons at Karlsruhe – Closure Test



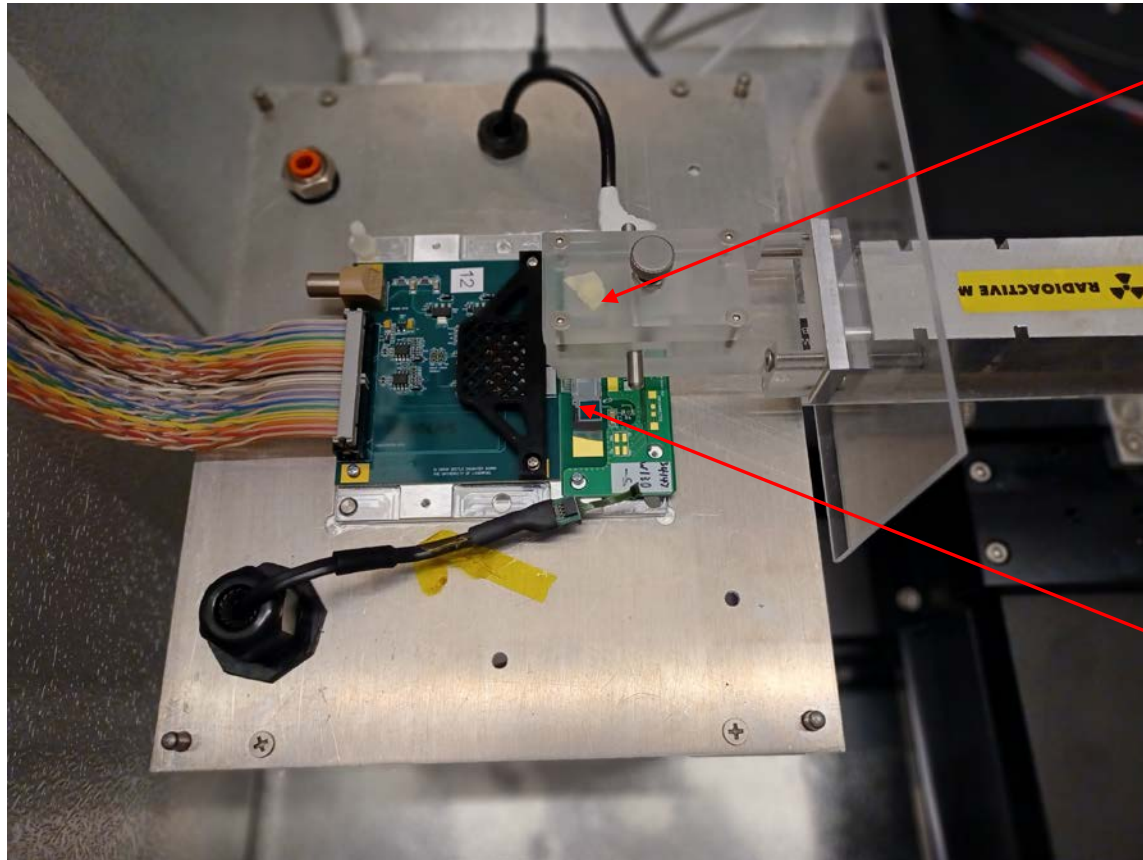
- ATLAS12
- 500 V Bias Voltage
- Measured at Freiburg
- Annealing at 60 C
- Fits to the coefficients are done independently at 400V and 500V

Reactor Neutrons – Closure Test



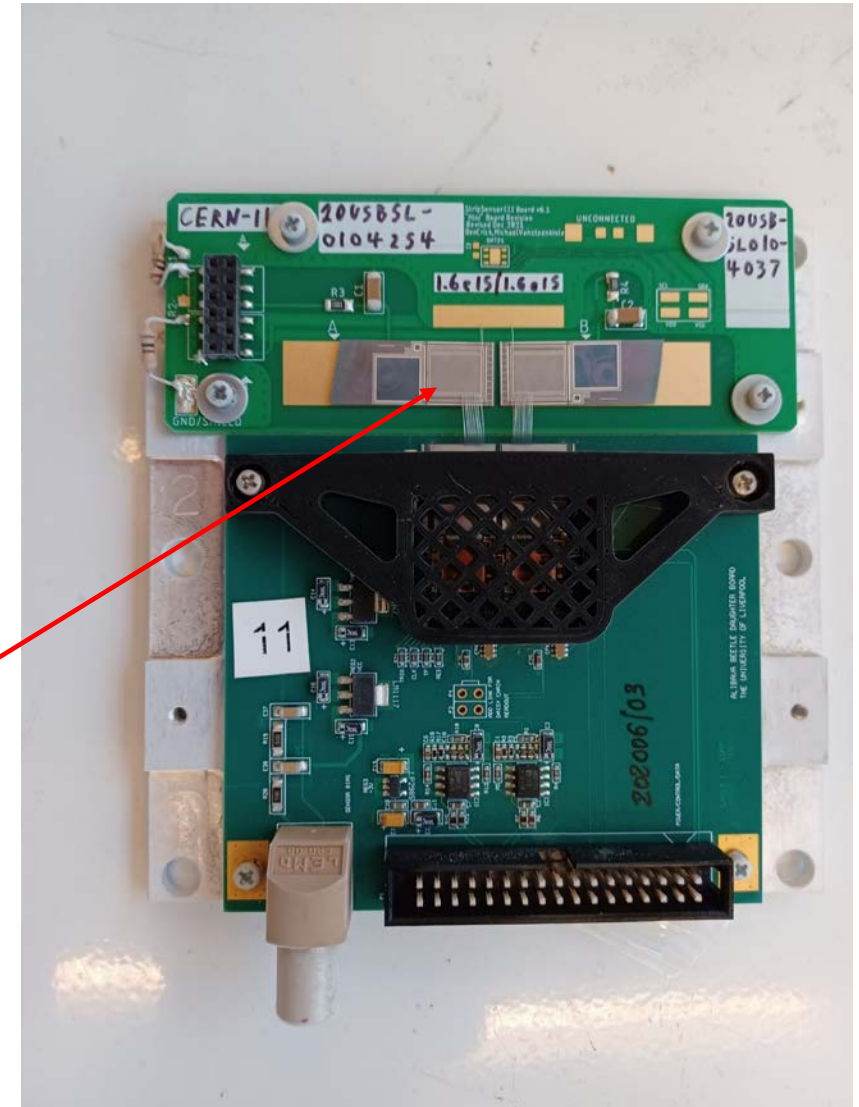
- ATLAS12
- 500 V Bias Voltage
- Annealing at 60 C
- Measured at Freiburg
- All neutron data irradiated at Ljubljana

Toronto Measurement of CCE of Miniature Sensors



^{90}Sr

Mini-sensor

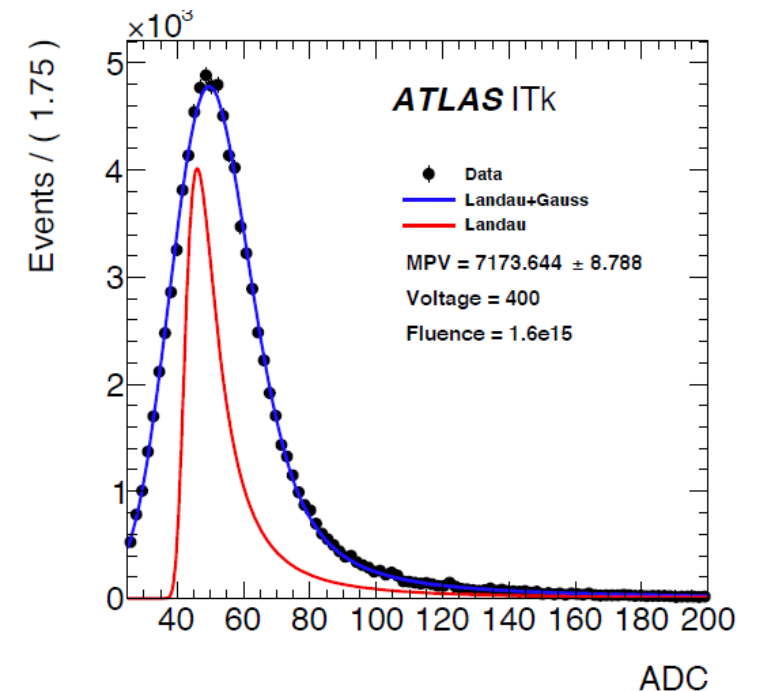
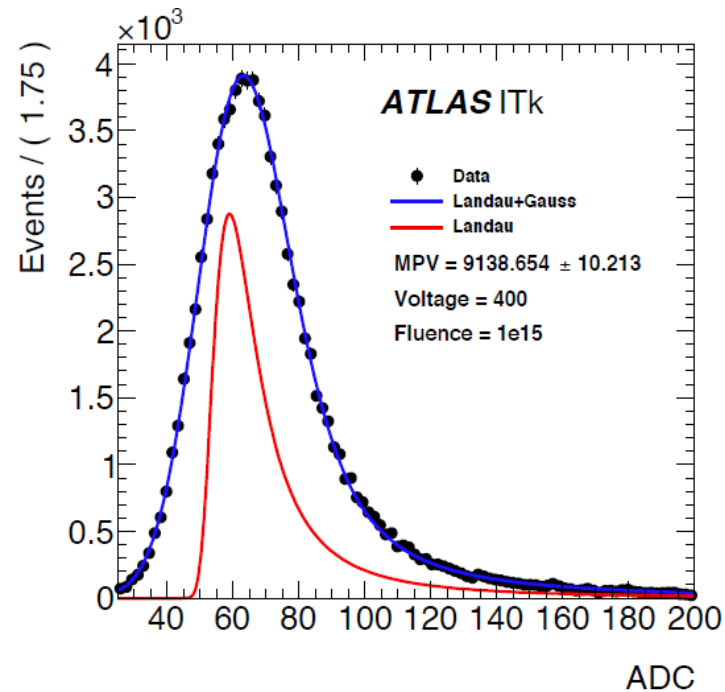
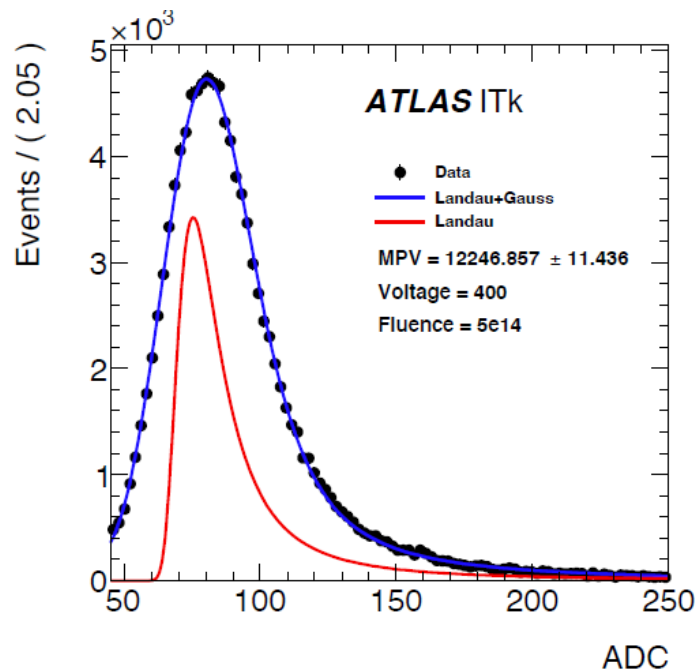


Uses Alibaba readout system to measure pulse height spectrum
Measurements done in freezer at -27 C

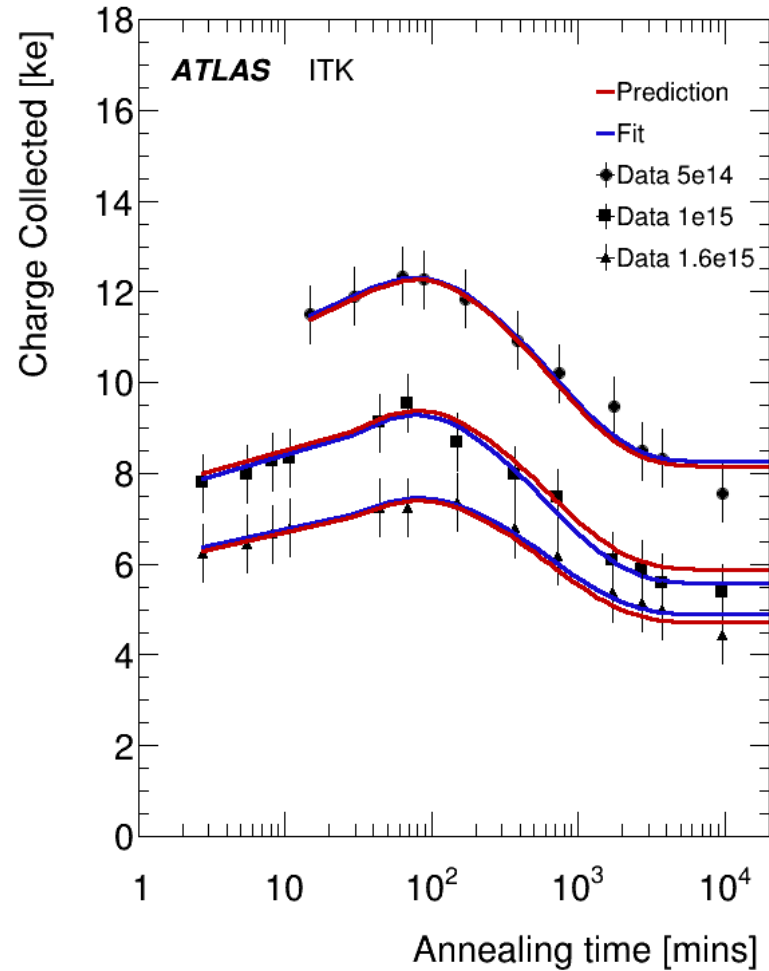
Measurement Procedure at Toronto

- Gain of all Alibava daughter boards calibrated as a function of temperature
- Used sensor mounting board with improved HV filtering
- Took data for Bias Voltage 50V to 1100V
- Pulse height spectra fitted to Landau + Gaussian
- Most probable value of Landau plotted

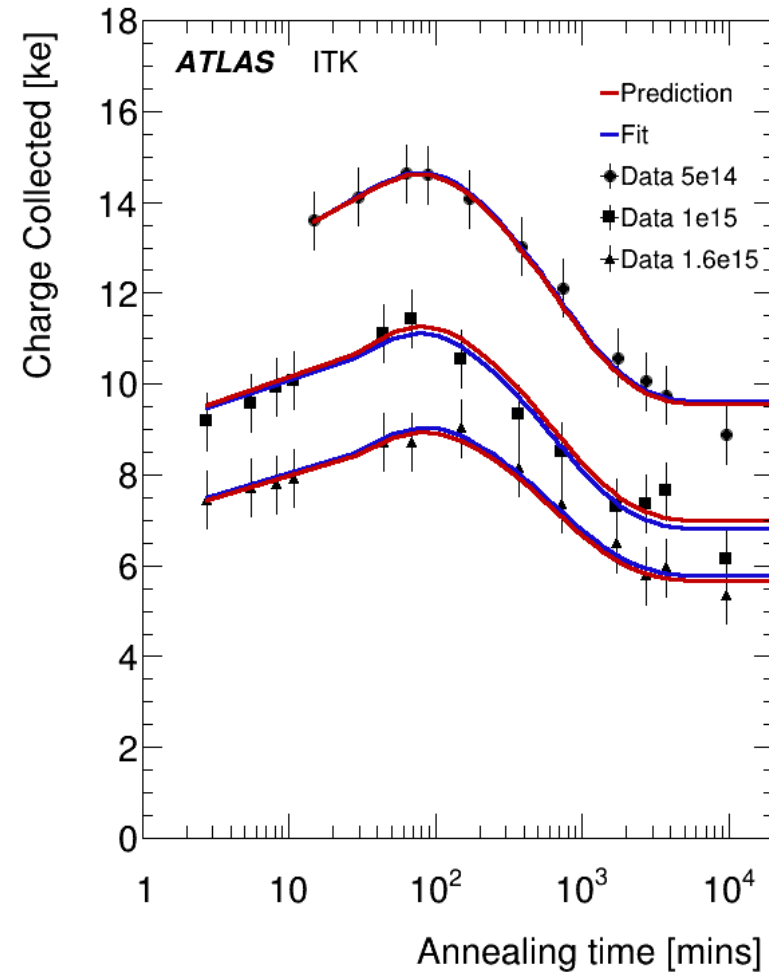
150 Mins Annealing at 60 deg



Fits and Closure of ATLAS18 - Neutrons

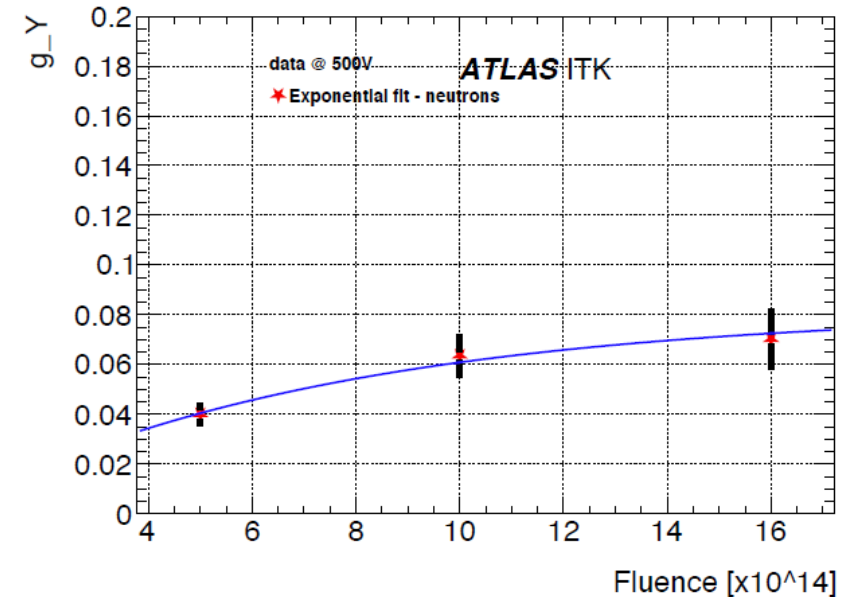
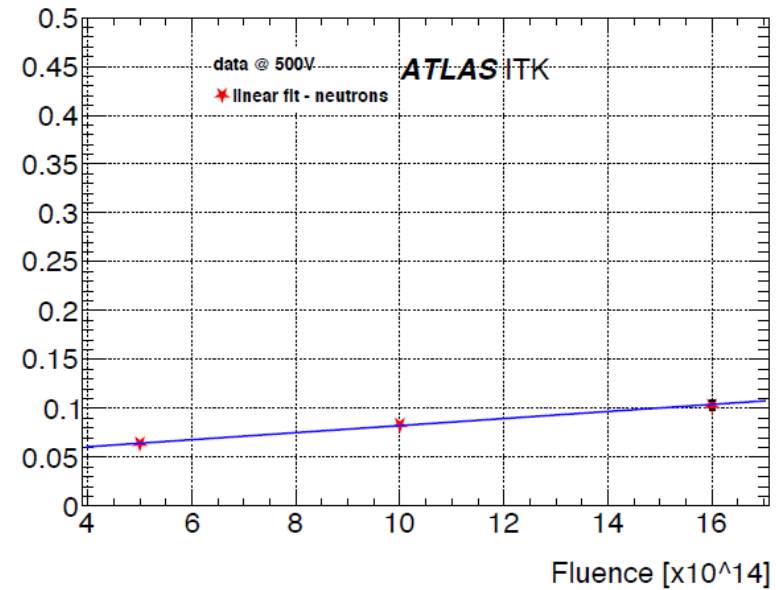
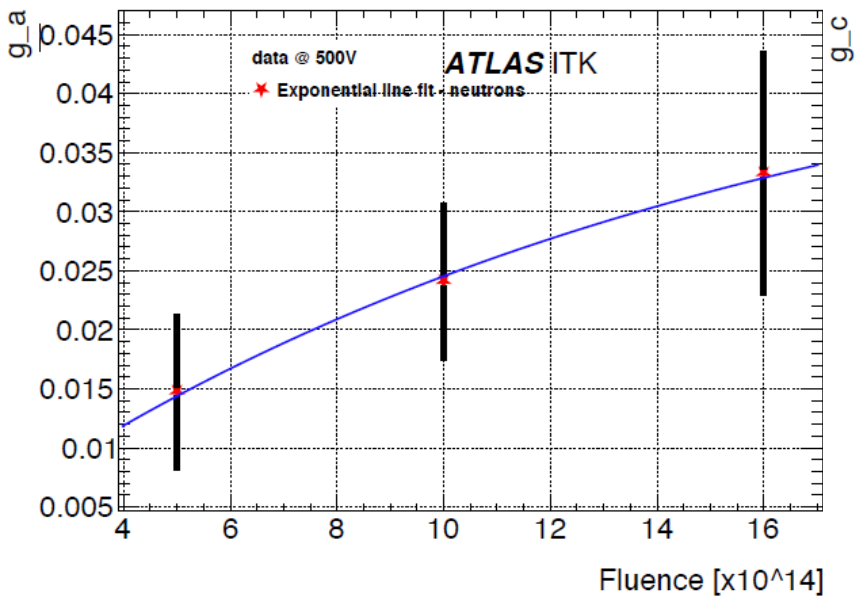


- Measured in Toronto
- **400V** Bias Voltage
- Annealing at 60 C



- Measured in Toronto
- **500V** Bias Voltage
- Annealing at 60 C

g-coefficients for ATLAS18 Neutrons



- Measured in Toronto
- 500V Bias Voltage

Use of Model in Assessing Long Term Running Scenarios

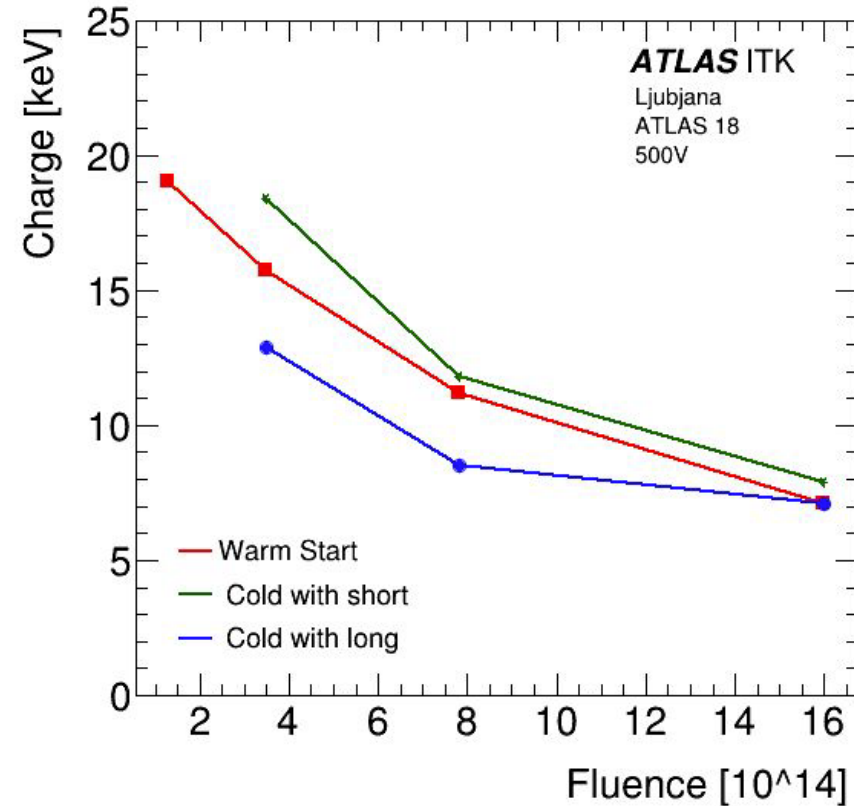
We have used model to investigate the end of life CCE in several possible situations

- 1) Alternative temperature Profiles during running
 - Starting cold -25C, and running cold except for
 - Long warmups
 - Short warmups
 - Starting at room temp and progressively reducing temperature
 - Allows data/model comparison

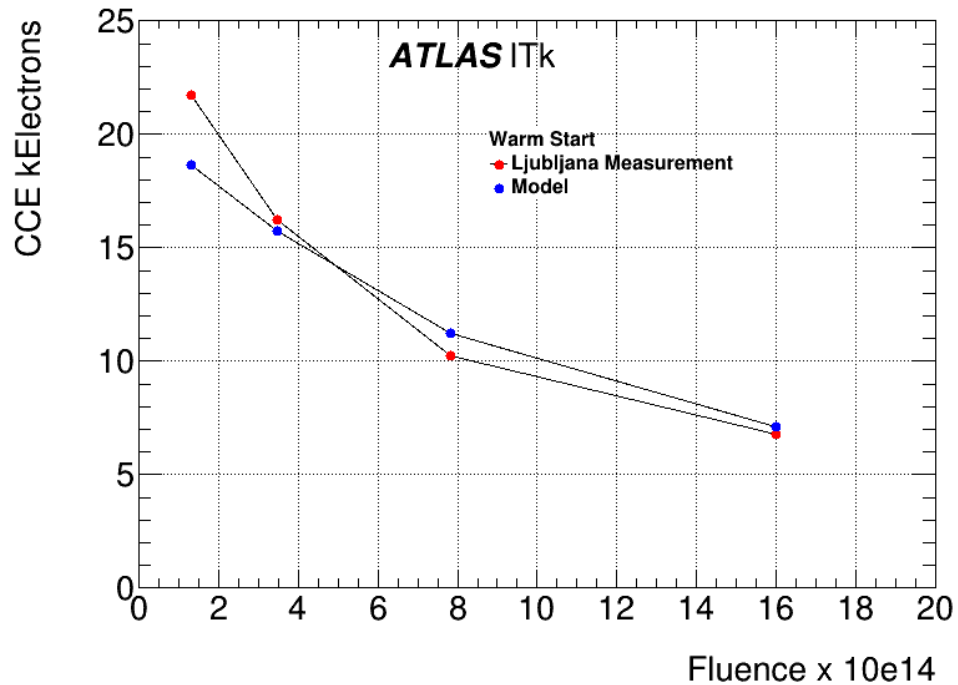
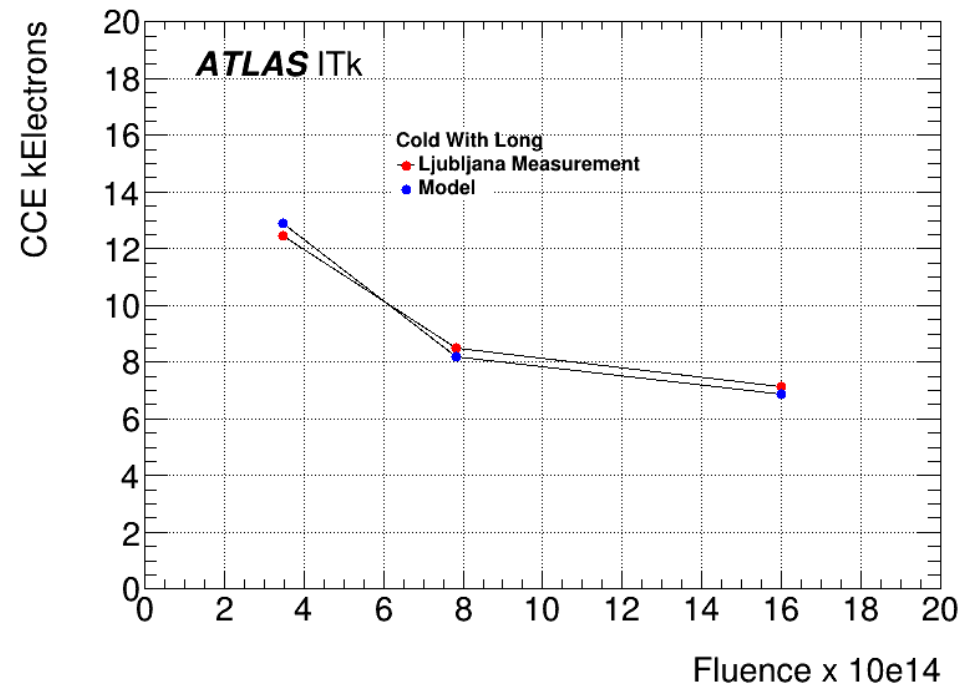
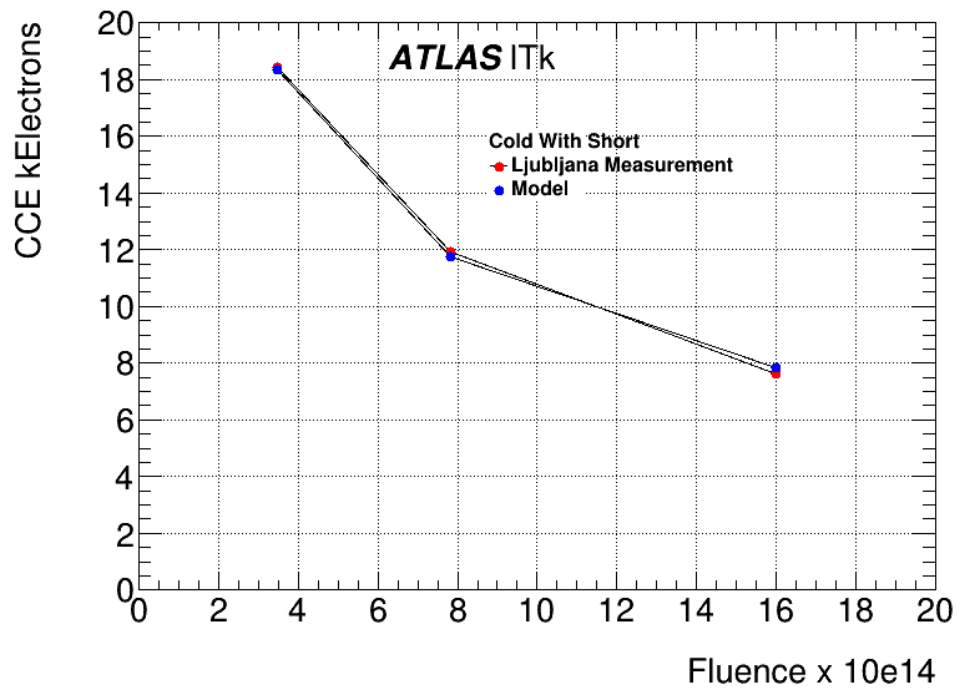
- 2) A staging scenario where the pixel installation was delayed until Long Shutdown#5 (LS5), but the Strips were installed in LS4, run cold, and then warmed up for 100 days in LS5

- 3) A scheduled maintenance of the CO₂ cooling system, during which the ITk is warmed up for 10 days each year and 40 days in LS4 and LS5

CCE measured using Ljubjana Alibava setup



- In all three scenarios the collected charge remained greater than 6350 electron equiv
- This corresponds to Signal/Noise = 10 , and corresponds to the worst case *viz* detector end-of-life

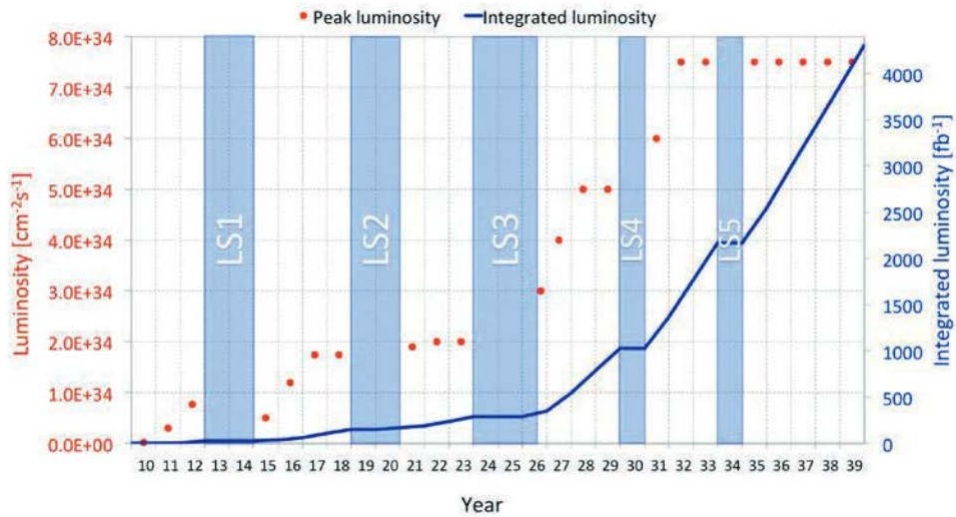


Comparison of model with experiment

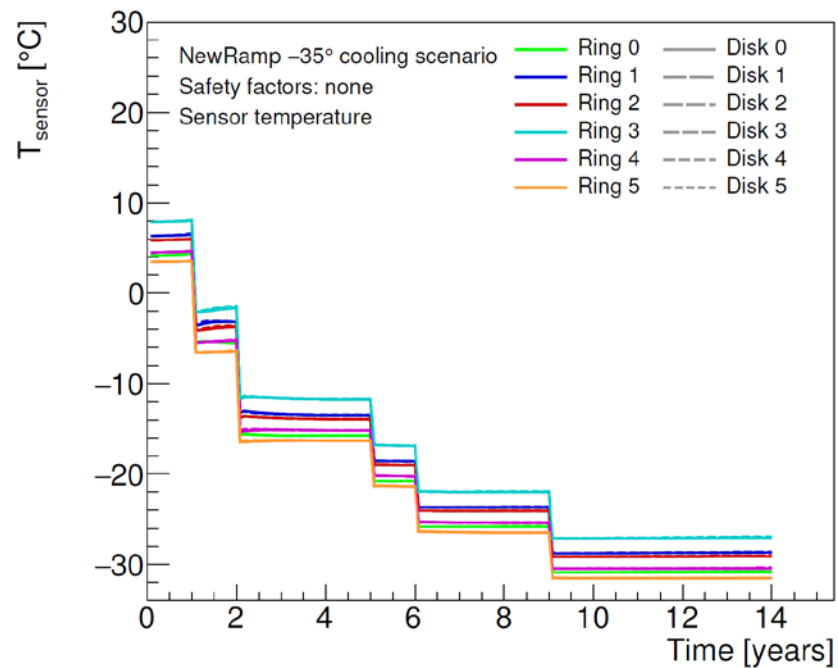
Conclusions

- We have constructed a simple, data driven, model of the dependence of collected charge on annealing time / temperature for the ATLAS18 strip sensors
- It reproduces annealing measurements at end-of-life to better than 5%
- We have used the model in temperature/schedule planning extending over the foreseen lifetime of the ITk
- The model does have shortcomings, viz:
 - Present approximation:
 - Apply fluence as a delta function
 - Run model for time@temp
 - Apply fluence as a delta function
 - Run model for time@temp
 - Force continuity
 - Iterate
 - Empirically this is a good approximation for long cold periods interspersed with short warm ups - See three running scenarios
 - In real running irradiation occurs concurrently with annealing
 - Try to build differential equation with phenomenological parameters

Additional



- Studies are based on luminosities and shutdown periods of the “ultimate HL-LHC parameters” described in CERN-2017-007-M



- Possible running scenarios have included the “warm start” to exploit the TID bump. Start above 0°. As fluence increases run at progressively lower temp, to reduce leakage current.
- Studies have shown that pre-irradiation of ASICs reduced the TID bump by an order of magnitude.
- Pre-irradiation has been included in the ASIC production procedure.
- It could be that the warm start scenario is no longer necessary.

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Alternative Temperature Variation during Running Scenarios

- Irradiated ATLAS 18 miniature R0 sensors at Ljubljana reactor
- Final irradiation corresponds to final integrated luminosity of 4000 fb⁻¹ with a safety factor of 1.5
- Annealing is done at 60°, corrected to simulated temperature using activation energy of 1.07 eV

$$T_{eff}(\theta_{eff}) = T_{ann}(\theta_{ann}) \exp\left(\frac{E_{act}}{k_B} \left(\frac{1}{\theta_{eff}} - \frac{1}{\theta_{ann}}\right)\right)$$

- Cycled repeatedly through- irradiate, anneal, measure CCE for three operation scenarios:
 - Warm start
 - 2 year fluence, anneal 1 year (equiv) 7° then 1 year at -3°.
 - 3 year fluence, then anneal 4 years at -13° .
 - 4 year fluence, then anneal 3 years at -20° .
 - 5 year fluence, then anneal 5 years at -25° .
 - Cold start – short warm ups
 - Operation at -25° , 10 days at room temp during LS4 and LS5
 - Cold start – long warm ups
 - Operation at -25° , 100 days at room temp during LS4 and LS5

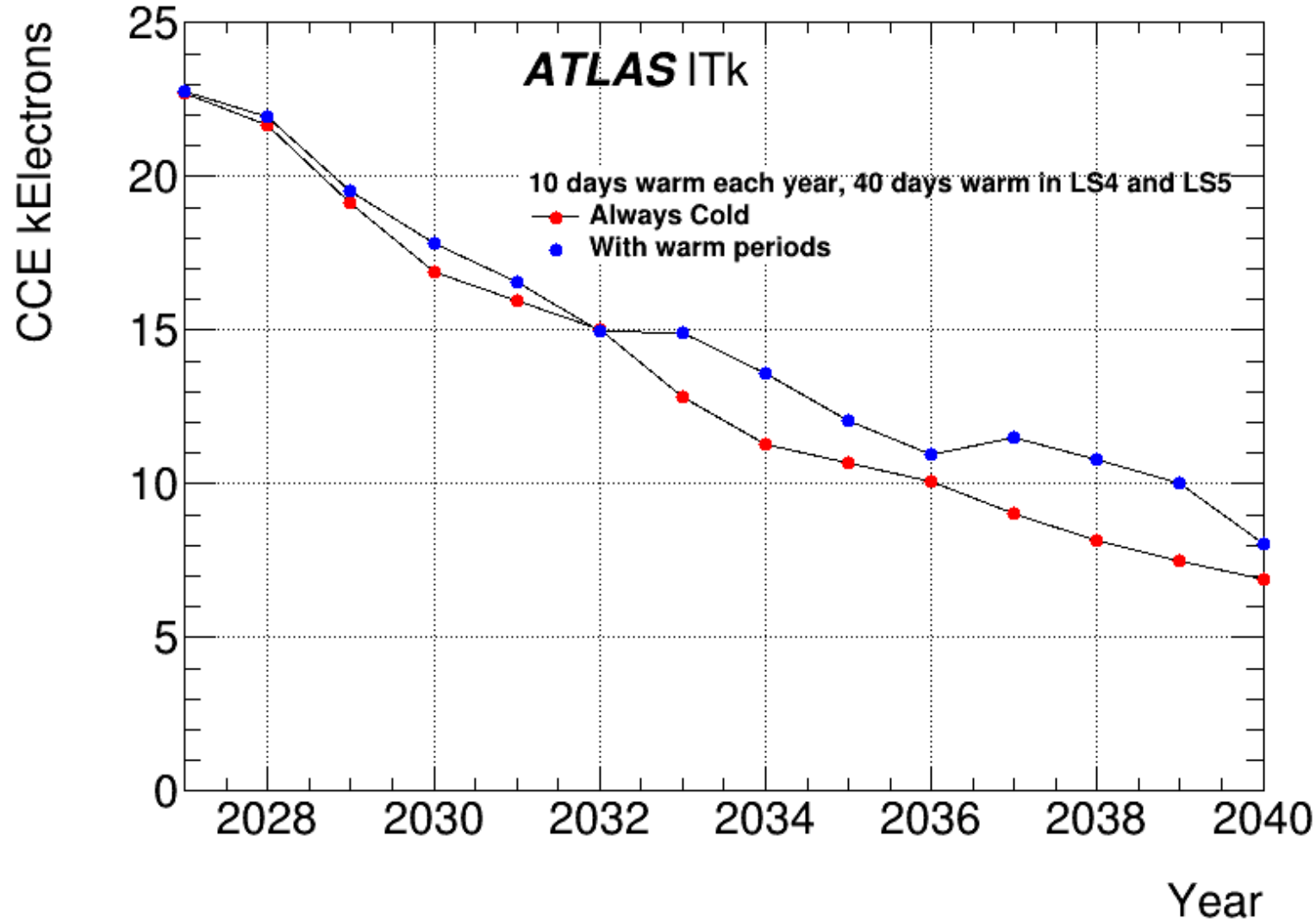
Proposed Staging of Pixels

- Assumed 13 month warmup in LS4, additional 100 days warm in LS5
- Ran Model for two fluence scenarios
 - Used tool https://atlas-service-radsim.web.cern.ch/radsim_noerrs
 - Radius = 40 cm, z = 150. This is inner edge of strip endcap closest to interaction point
 - Phase 2 ITk Step3.1Q6 geometry model
 - Si 1 MeV neutron equivalent (NIEL)
 - GEANT4
 - Twice this fluence – More or less strip “nominal safe”
- In reality neutrons only contribute 50% of fluence
 - Other 50% is protons – which are less damaging – further “safety” factor

Total Fluence	LS4	LS4->LS5	LS5	End of Life
8e14	14.8	14.9	12.9	10.
16e14	11.5	11.6	10.2	6.6

cf. 6.350

Use in Scheduling Studies II – Proposed CO2 Cooling line WarmUp

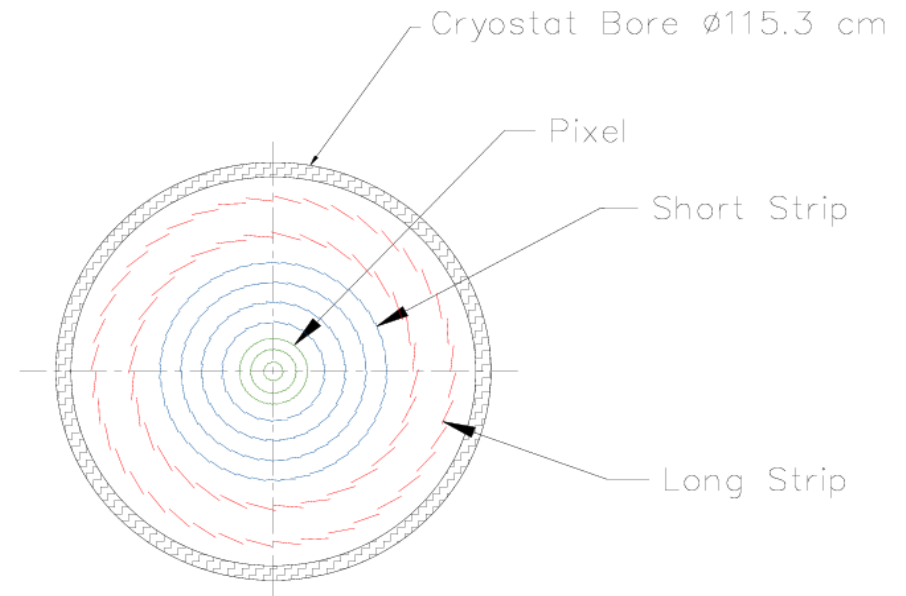
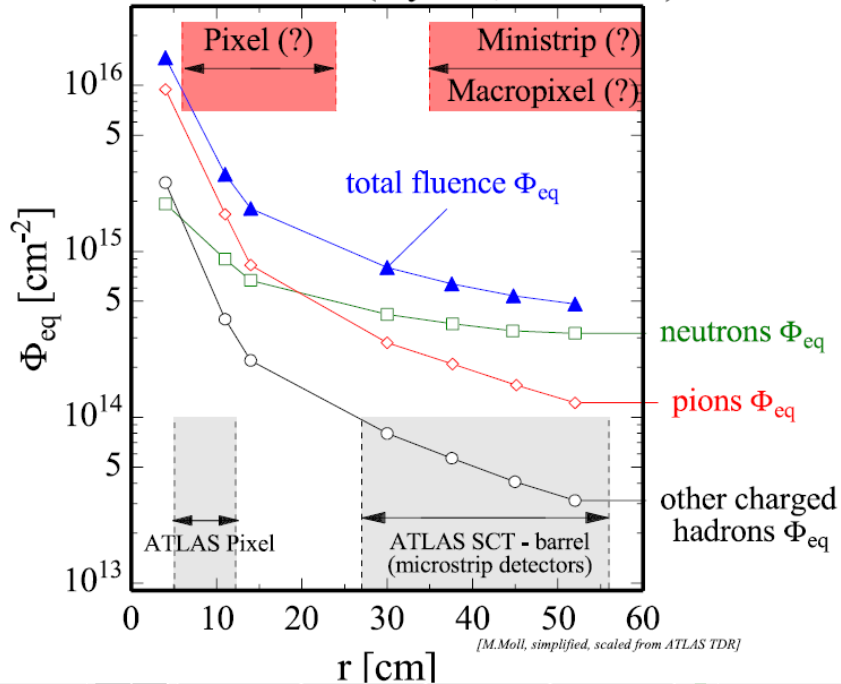


Lines are just root joining the dots

cf. 6.350

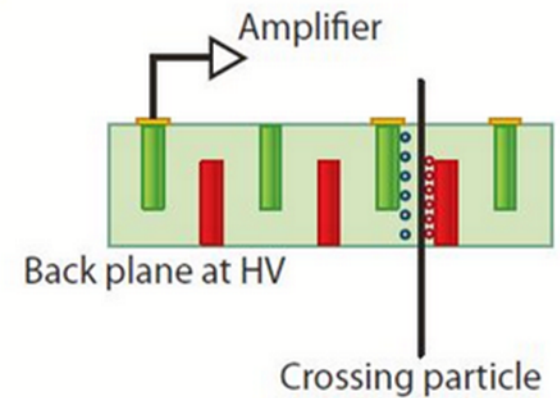
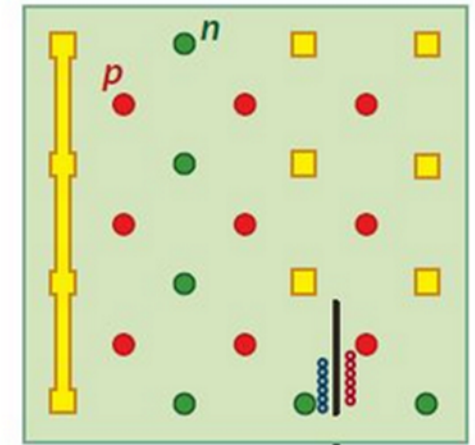
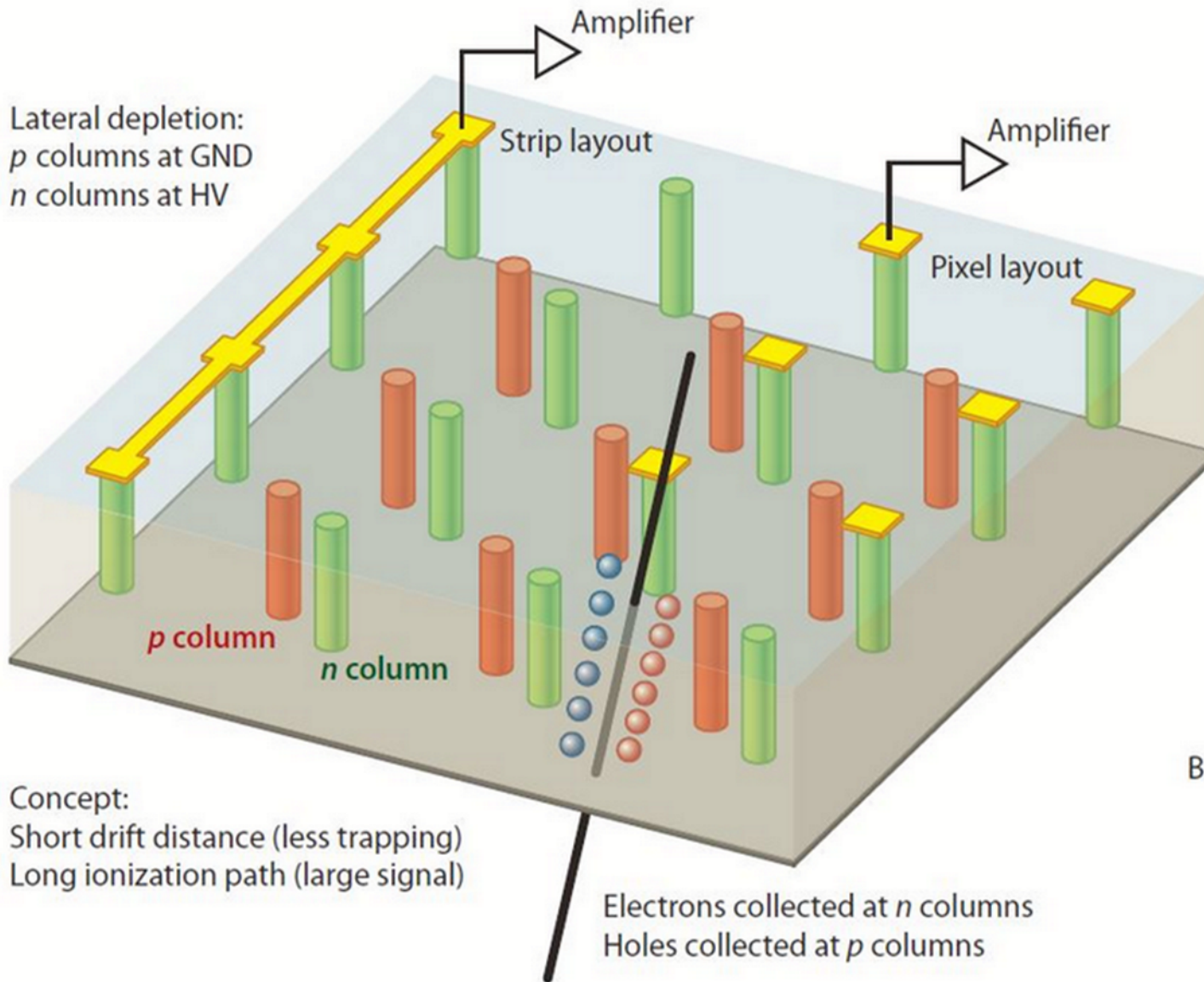
Inner Detector Replacement

SUPER - LHC (5 years, 2500 fb⁻¹)

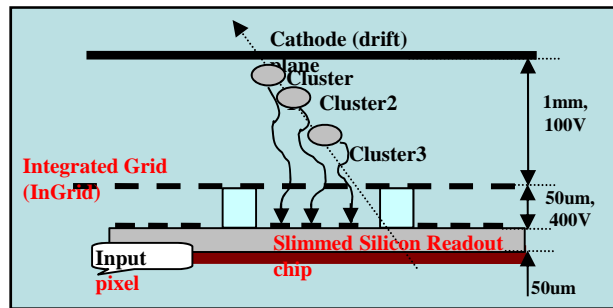
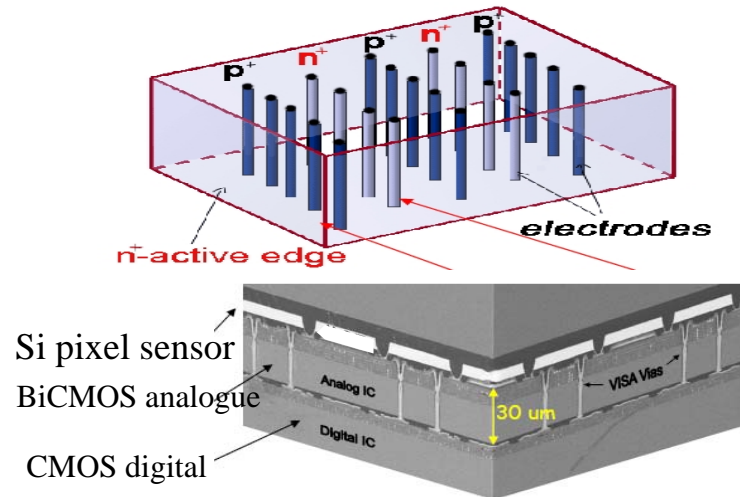


- Order of magnitude increase in Data rates, Occupancy, Irradiation
- No TRT – Si strips
- Pixels moved to larger radius
- New technology for inner layers
- R&D required on sensors, readout, and mechanical engineering

3-d SILICON → SHORTER DRIFT DISTANCE — LESS TRAPPING



Pixel-layer Technologies



- Harsh radiation environment ($R \sim 4\text{cm}$)
 - investigate new technologies

- 3D Si
- Thin silicon + 3D interconnects
- Gas over thin pixel (GOSSIP)

Diamond pixels

- May test in pre-SLHC b-layer replacement (~2012)

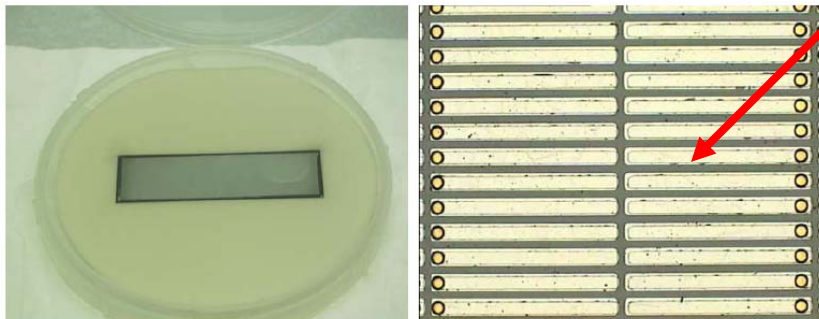


Figure 5: (a) Photograph of the ATLAS pixel diamond mounted in the carrier ready for bump bonding. (b) Zoom view of the pixel pattern after the under-bump metal is deposited.

