

INELASTIC ELECTRON-PROTON SCATTERING

UP TO NOW CONSIDERED — ELASTIC SCATTERING

ROSENBLOTH CROSS SECTION → ELASTIC SCATTERING
→ THE PROTON
REMAINS A PROTON

HAVE ESTABLISHED THAT PROTON HAS STRUCTURE
IN ELASTIC SCATTERING POSSIBLE

$ep \rightarrow ep$ ELASTIC

EXCITE
PROTON
STRUCTURE →

$ep \rightarrow e \Delta^+ \rightarrow p \pi^0$ } INELASTIC
"EXCLUSIVE"

$ep \rightarrow e n \pi^+$ — "

$ep \rightarrow X e$ — INELASTIC
"INCLUSIVE"

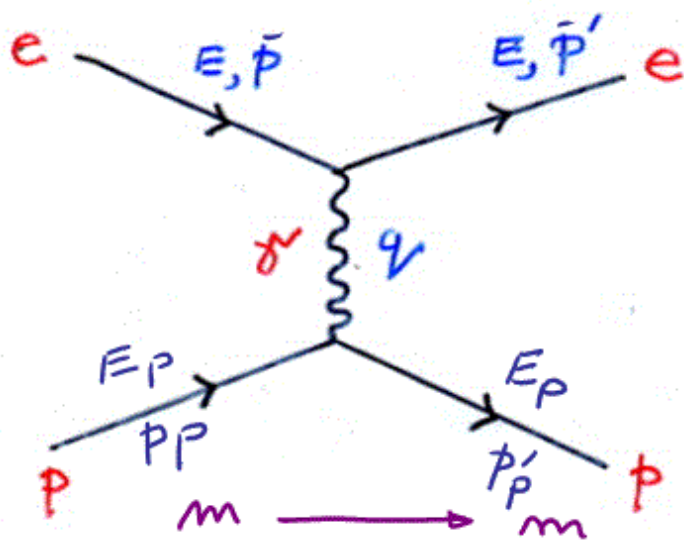
ANY HADRONIC SYSTEM
FROM BREAK UP OF PROTON

JUST MEASURE
ELECTRON

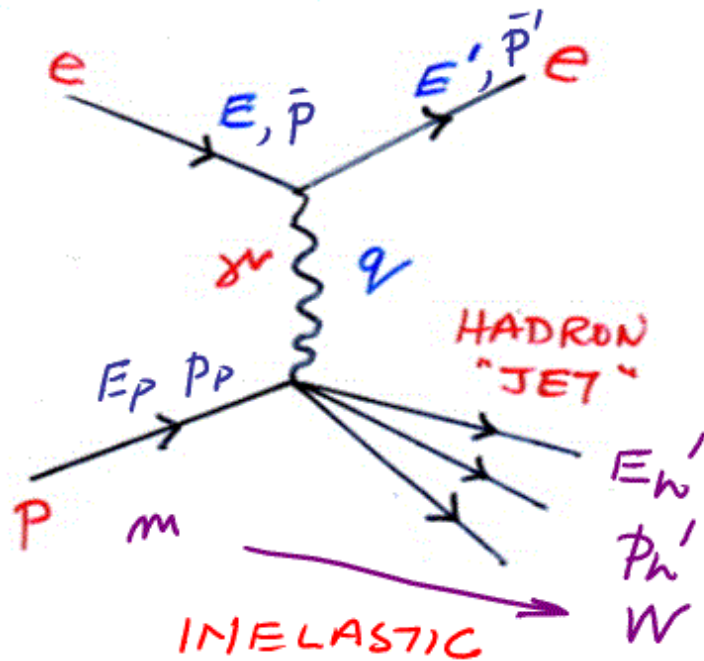
INELASTIC $e p$ SCATTERING

POWERFUL TO LOOK AT PROTON STRUCTURE

NUCLEUS \rightarrow NUCLEONS \rightarrow QUARKS



ELASTIC - TARGET NOT EXCITED / FRAGMENTED



INELASTIC

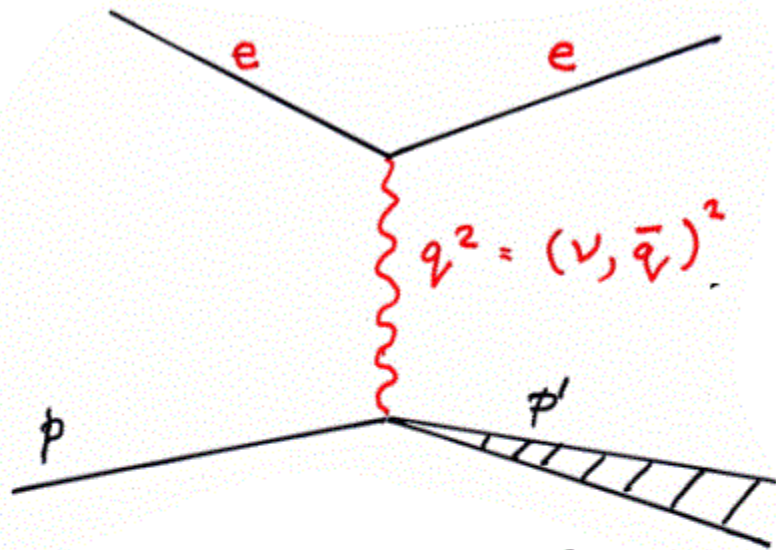
$$V = E - E' \quad \begin{array}{l} \text{ENERGY} \\ \text{TRANSFER} \end{array} - \text{INELASTICITY}$$

$$q = (\nu, (\bar{p} - \bar{p}'))$$

$$V = \frac{|q^2|}{2m_p} \quad \begin{array}{l} \leftarrow \text{4-MOMENTUM} \\ \text{TRANSFER} \\ \leftarrow \text{TARGET} \\ \text{MASS} \end{array}$$

$$q^2 = \nu^2 - p_h'^2$$

ELASTIC & INELASTIC SCATTERING



MASS OF PROTON
ELASTIC SCATTERING

INVARIANT MASS OF
FINAL HADRONIC SYSTEM
INELASTIC SCATTERING

m_p OR W_H

$$q^2 = (p' - p)^2$$

$$q^2 = p'^2 + p^2 - 2p' \cdot p$$

$$= W_H^2 + m_p^2 - 2(\nu + m_p, \bar{p}') \cdot (m_p, 0)$$

$$= W_H^2 - m_p^2 - 2\nu m_p$$

$$W_H^2 = q^2 + m_p^2 + 2\nu m_p$$

INVARIANT SO EVALUATE
IN LAB FRAME

2 INDEPENDENT
VARIABLES FOR
INELASTIC

$$q = (\nu, \bar{q})$$

GENERALLY $W_H^2 = q^2 + m_p^2 + 2V m_p$

FOR ELASTIC SCATTERING $W_H^2 = m_p^2$

$$m_p^2 = q^2 + m_p^2 + 2V m_p$$

$$q^2 = -2V m_p$$

ONLY ONE VARIABLE V

LOOKING BACK AT DIAGRAM

$$q^2 = (V, \bar{q})(V, \bar{q}) = -2V m_p$$

SO $V^2 - \bar{q}^2 = -2V m_p \rightarrow \bar{q}^2 = V^2 + 2V m_p.$

IN LIMIT $V \gg m_p \rightarrow \bar{q}^2 \approx V^2$

THEN 4-MOMENTUM XFER $\rightarrow q = (V, \bar{q}) \approx (V, V)$

FOR HIGH ENERGY
ELASTIC SCATTERING

$$q^2 \approx V^2 - V^2 \approx 0$$

REPRISE ON SCATTERING CROSS SECTIONS

RUTHERFORD: NON RELATIVISTIC, SPINLESS
POINT TARGET & BEAM

$$\frac{d\sigma}{d\Omega}_R = \frac{4m^2 (Z e^2)^2}{q^4} = 1 \text{ FOR ELECTRON}$$

\swarrow 3 MOMENTUM

MOTT: RELATIVISTIC SPIN $\frac{1}{2}$ ELECTRON SCATTERING
OFF SPINLESS POINT TARGET

$$\frac{d\sigma}{d\Omega}_{\text{MOTT}} = \frac{4E^2 (Z e^2)^2}{q^4} \left(1 - \beta^2 \sin^2 \frac{\theta}{2} \right)$$

\swarrow 4-MOMENTUM

FORM FACTOR: ELECTRON SCATTERING FROM AN
EXTENDED TARGET

$$\frac{d\sigma}{d\Omega}_{\text{EXTENDED}} = |F(q^2)|^2 \left(\frac{d\sigma}{d\Omega} \right)_{\text{MOTT}} \text{ POINT}$$

ELASTIC SCATTERING OF ELECTRONS & PROTONS:

$$\left(\frac{d\sigma}{d\Omega}\right)_{Ro} = \left(\frac{d\sigma}{d\Omega}\right)_{MOTZ} \left[\frac{G_E^2 + b G_M^2}{1+b} + 2b G_M^2 \tan^2 \frac{\theta}{2} \right]$$

↳ COULD WRITE $\frac{d\sigma}{dq^2} \rightarrow$ ONE SCATTERING VARIABLE

INELASTIC ELECTRON PROTON SCATTERING

$$\left(\frac{d^2\sigma}{dq^2 d\nu}\right)_{INEL} = \left(\frac{d^2\sigma}{dq^2 d\nu}\right)_{POINT} \left[W_2(q^2, \nu) + 2W_1(q^2, \nu) b \tan^2 \frac{\theta}{2} \right]$$

↑
TWO SCATTERING
VARIABLES

↑ ↗
TWO FORM FACTORS
FUNCTIONS OF TWO VARIABLES
STRUCTURE FUNCTIONS